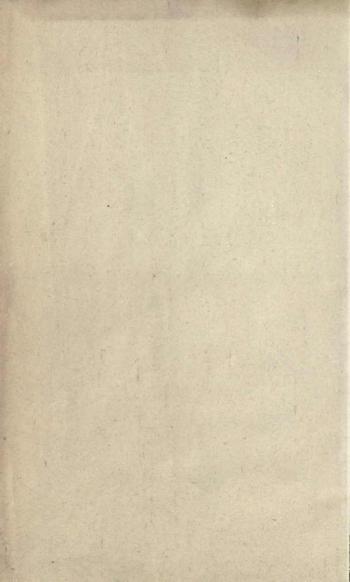


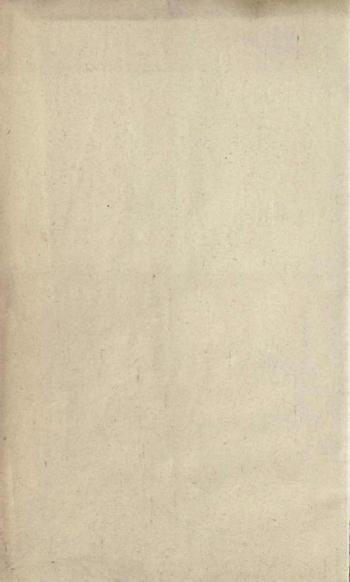
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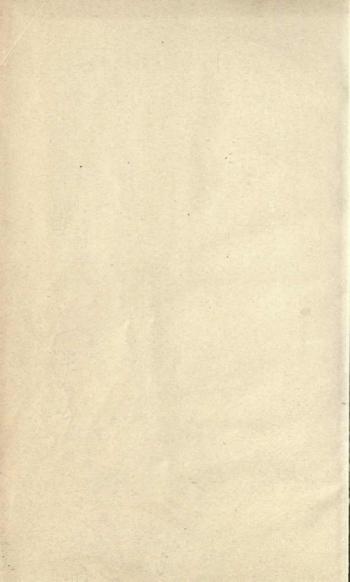


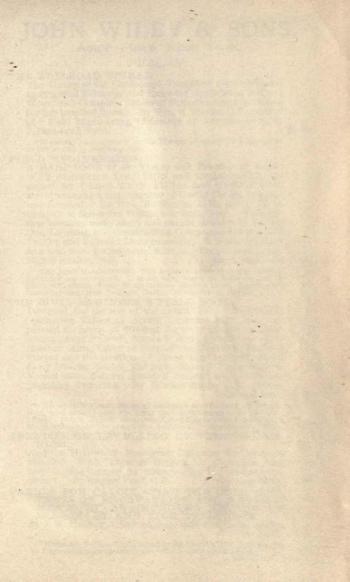


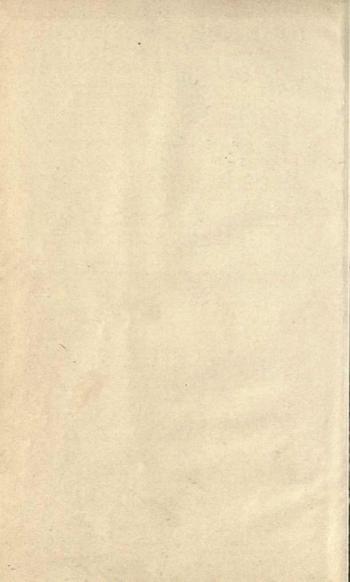












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BY

H. C. GODWIN.



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PREFACE.

On unbern Mathematical Telegrams which I have been bound to

I am publishing the following notes because I think they may possibly supply the want of a Field-book,—a want which I have often felt myself and have often heard expressed—which, while avoiding as much as possible the intricacies of mathematics, would be of more general application than any of the books of this class which I have as yet come across.

The Railroad engineer is rarely an expert mathematician: in fact it has always seemed to me that the time which must necessarily be spent by him in attaining mathematical proficiency might be very much better employed in reading up some of the more practical subjects of his profession. Bearing this in mind, I have endeavored to strip the following pages of all unnecessary mathematical deductions, making it mainly my object to give the results deduced, and yet at the same time giving sufficient explanation to enable any one possessed of the ordinary smattering of mathematics and mechanics to deduce the same results for himself.

I have avoided the insertion of Logarithmic Tables. I am well aware that to some this will appear a serious omission; but considering that this is merely a Field-book, and not a work to be consulted in cases where accuracy in the 6th figure is usually essential, I have deemed that the exclusion of the hundred pages or so which this omission permits, amply compensates for the few seconds of additional labor which the lack of them may occasionally involve. Speaking for myself, as regards Railroad work, I must say that for one time that I work by logarithms I work a hundred times by "naturals;" and I know that most engineers would bear similar testimony.

In the Astronomical problems in the latter part of the book, considerable labor may, of course, be saved by the use of

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ERRATA.

Page 4, line 10. For .27 read 3.7

" 24, " 11. " 12 " 18

" 36, " 16. After them insert say A

" 36, " 24. For 1.59 read 1.84

" 55, bottom line. For ZP read WP

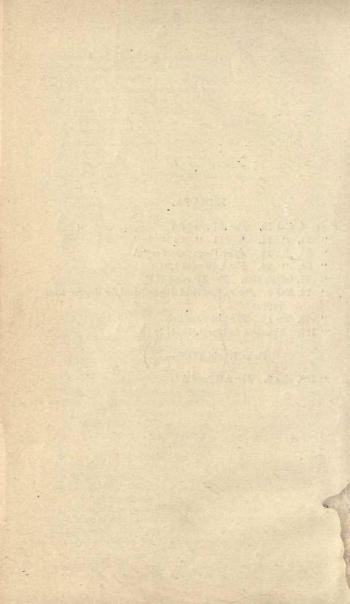
" 72, line 3. For radius read degree, and for degree read radius

" 78, line 17. For abc read acb

" 117, Equation in line 8 should be

$$Bc = R\left(\sin POM - \frac{ab}{2}\right)$$

" 128, line 3. For AB read AD





PART I. RAILROAD LOCATION.

GENERAL CONSIDERATIONS.

1. In the early days of Railroad Building, the Locating Engineer was forced to rely mainly on his individual ability, trusting principally to the correctness of his eye to detect the most suitable route, guided only by the very limited experience of others and his own common-sense. The man who worked his party the hardest, and covered most ground in the day, was in those days, unless any very obvious defects were visible in his work, too often looked upon as the best locator. But the years of experience which have followed have been years of experiment also; and the practice of Railroad Location has by degrees developed into a science, which, though yet far from perfect, forms a most important part of a Modern Engineering Education.

In a Field book of this sort, it is impossible to do more than treat rapidly a few of the leading questions which the subject involves, and formulate, where possible, rules for guidance in

the field.

A knowledge of the principles of Railroad Location must be backed up by experience in Railroad Construction. For, in order to locate well, a man must have fairly accurate ideas of the suitability and cost of the various works which his location involves. The best location for a certain road is not that which enables the traffic to be carried on with the least amount of work, or which gives the lowest Operating Expenses, but that which, in a given time, renders the

a maximum. Thus we see that more or less accurate estimates of the probable Receipts and Operating Expenses are of the utmost importance before starting the location; and it is only when these are arrived at that the amount which we are entitled to expend on construction can be fixed.

2. Before considering the Financial side of the question, however, we will glance hurriedly over some of the principal Mechanical Problems which occur in dealing with the motion of trains, for, without some slight knowledge of Railroad Dynamics, an intelligent application of the Laws of Location is impossible.

TRAIN RESISTANCES.

The Resistance due to the motion of a train on a straight level track—excluding for the present the Inertia of the train—may be regarded as being the sum of the three following com-

ponents:

3. ROLLING RESISTANCE, which is composed of the frictional resistance at the journals and that at the wheels at the points of contact with the rails: these two may for ordinary purposes be classed together under the head of Rolling Resistance. Its magnitude depends largely upon the surface-bearing at the journals; the coefficient of friction decreasing as the load per unit-surface on the journals increases, so that the resistance is relatively higher in the case of Empty Cars than with Loaded ones; being at ordinary speeds about 6 lbs. per ton (2000 lbs.) of weight of train in the former case, while with Passenger Coaches or Loaded Cars it only amounts to about 4 lbs. By referring to the Diagram of Resistances, p. 6, we see that at the point of starting the Rolling Resistance is very high, being then about 20 lbs. per ton, but that at a velocity of about ten miles per hour it reaches its minimum value, and from that point increases constantly by a trifling amount through the successive higher velocities. The Initial Resistance depends largely on the length of time the train has been standing, a stop of only a few seconds causing a resistance of about one half that given in the Diagram. Since, however, there is always more or less "give" about the couplings, no two cars at the same instant offer their maximum resistance, the front end of a long train being well under way before any motion at all is transmitted to the rear. Thus the pull on the

draw-bar is not in reality so excessive as it at first appears; for if we take the whole train into consideration, the resistance at the start may be set down as about 12 lbs. instead of 20 lbs. per ton, as in the case of a single car.

The Line of Rolling Resistance starts in the Diagram from the line of the 1 p. c. grade; thus indicating that a train left standing with the brakes off on this grade, is just on the point of starting on its own account. On any grade lighter than this, a train will usually require considerable force to set it in motion. By increasing the diameters of the wheels we slightly decrease the resistance to rolling.

- 4. RESISTANCE DUE TO OSCILLATION AND CONCUSSION.—The amount of this we obtain approximately by assuming that it equals .005 lb. per ton at 1 mile per hour, and increases as the square of the velocity. Thus, e.g., at 40 m. p. h. it equals 8 lbs. per ton. The longer the train, however, the less this resistance amounts to per ton, for each car is more or less steadied by the force which is transmitted through it to the adjoining one; thus it is usually much more considerable in the rear than in the centre or forward end of the train. It is produced in a great measure by the inequality in elevation of the two rails on an imperfect track, and thus is often found to diminish on curves where the difference in elevation of the rails is not exactly suited to the speed at which the train is travelling, since it is then subjected to a lateral thrust which prevents the oscillations being so great as they otherwise would be.
 - 5. ATMOSPHERIC RESISTANCE.—This is due to two causes:
 - (a) The opposition offered by the particles of air in the direct path of the engine, while being thrust forwards and sideways by the advancing train, together with the "suction" caused by the rear car; and—
- (b) The frictional resistance of the air against the surface of the train, corresponding to the "skin resistance" in the case of ships. The former (a) amounts to about 0.3 lb. per train running through still air at a velocity of 1 mile per hour, and increases as the square of the speed: thus, e.g., at 40 m. p. h. it amounts to about 480 lbs. Probably in ordinary trains not more than one third of this resistance causes additional strain on the draw-bar, because the greater part of it is taken and overcome by the engine itself. As regards the latter

resistance, (b) it may be ascertained with tolerable accuracy by allowing 0.03 lb. per car at a speed of 1 mile per hour, and considering it to increase as the square of the velocity. Thus, if we have a train composed of 10 loaded box-cars (see Sec. 13) hauled by an engine which, together with its tender, weighs 60 tons, the total atmospheric resistance in lbs. at 40 m. p. h. =480+480=960 lbs. (assuming that the allowance already given for the engine includes the surface resistance as well); and since the weight of the train-inclusive of engine and tender—equals about 260 tons, this is equivalent to about 37 3.7 lbs. per ton of entire train. Suppose, in the above example, we have a Head-wind blowing at the rate of 20 m. p. h., we may then consider the atmospheric resistance as being that due to a train velocity of 60 m. p. h. But if this wind were blowing in the same direction in which the train is going, then the resistance caused by it would be equal to that caused by a train velocity of 20 m. p. h. in still air.

A Side-wind adds very considerably to the ordinary atmospheric resistances by increasing the frictional resistance at the rails, owing to the flanges of the wheels being pressed against the inner side of the leeward rail.

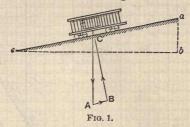
The above resistances are peculiar to all trains at all times; the two following, however, are accidental, and dependent on circumstances.

6. RESISTANCE TO CURVATURE.—The many causes which combine to make up this resistance, and the share which each has in forming the result as a whole, have been but vaguely determined by experiment: it is known, however, that at speeds not exceeding about 5 miles per hour, it amounts to about 2 lbs. per ton per degree of curvature, and that it decreases as the speed increases, as shown in Diagram I, till at 70 miles per hour it does not probably amount to more than \(\frac{1}{3}\) lb. per ton. Thus, e.g., on a 5° curve it amounts at a velocity of 35 m. p. h. to about 2 lbs. per ton.

The use of Transition curves (page 100) is found to decrease it materially.

7. RESISTANCE DUE TO GRAVITY.—This resistance may be termed a "mathematical" one, whereas the previous ones have been based entirely on experiment; for though the coefficient of gravity is itself a quantity derived from experiment, it is merely the ratio of the inclined component AB

(Fig. 1) to the force of gravity AC, which enters into the question; or, what is the same thing, the ratio of ab to ac.



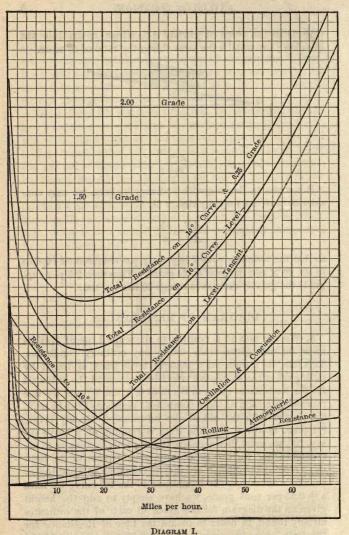
But since, in dealing with ordinary inclines, we may consider ac=cb, we may say that

$$\frac{AB}{AC} = \frac{ab}{cb},$$

so that the resistance caused by gravity per ton (2000 lbs.) equals in lbs. $20 \times rate$ per cent of the grade. Thus on a 2.5 p. c. upgrade the gravity resistance equals 50 lbs. per ton.

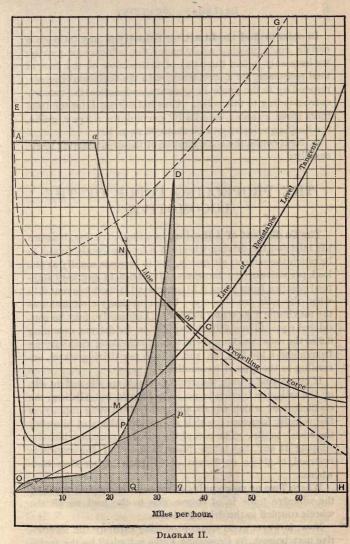
DIAGRAM OF RESISTANCES.

8. We are now in a position to draw the Line of Resistance for any given train under any ordinary conditions. This line, for a train on a straight level track, is found by setting-off at the successive velocities the sum of the ordinates for the Resistances given in Sections 3, 4, and 5; and the line representing each of these component resistances can be readily plotted with the aid of the information already given. Suppose, however, that the train is running on a curve of, say, 10°, we must then measure the respective ordinates to the resistance line for the 10° curve, and add these to the ordinates already obtained. We then get the Line of Total Resistance on a 10° curve. If in addition to the 10° curve we have a + 0.25 per cent grade, we have simply to add the height given on the diagram for this grade to each of the ordinates already found, in order to obtain the Line of Resistance for the train on a 10° curve and a +0.25 p. c. grade. If the train were descending the grade, it would be necessary to subtract the last ordinate instead of adding it.



TRAIN RESISTANCES IN LBS. PER TON.

Engine and Tender weigh 60 tons. 10 Loaded Box-Cars, each weighing 20 tons.



PROPELLING FORCE OF LOCOMOTIVE IN LBS. PER TON. Locomotive 500 I. H. P. Engine and Tender = 60 tons. f=0.2 10 Cars, 20 tons each.

In order to find the Limiting Velocity of any train on a certain grade, moving solely under the influence of gravity, we have only to find the point of intersection of the line of total resistance, for a level track, with the horizontal line corresponding to the grade in question, and notice the velocity corresponding to this point. Thus in Diagram I, for the train there given, running round a 10° curve down a 2 p. c. grade, the limiting velocity will be about 63 m. p. h.

9. Next comes the consideration of the counteracting force, namely:

THE PROPELLING FORCE OF THE LOCOMOTIVE.

The Coefficient of Adhesion, i.e., Static friction, between the rails and the driving wheels of a locomotive, is found to be much the same at all speeds, but to increase rapidly as the load per unit-surface increases. It varies in ordinary Railroad practice from about 0.33 when sand is used to about 0.18 when the rails are slippery. Under ordinary circumstances the maximum Propelling Force of a Locomotive may be considered equal to one fifth the weight on its drivers, assuming 0.2 as the usual working coefficient of adhesion; thus varying from about a ton to a ton and a half per driving-wheel, according to the type of locomotive.

If on starting a train the driving-wheels are allowed to slip on the rails, the friction is no longer Static but Sliding, the coefficient of which equals about 0.1, decreasing rapidly as the velocity increases; which shows the fallacy of allowing the wheels to slip. The part of the rail, however, on which the slipping, if any, has taken place is found, if the engine is reversed, to give a coefficient of adhesion higher than elsewhere.

Where Two or more pairs of wheels are coupled together, the adhesive force is, of course, due to the load on all the wheels coupled to the driving-wheels.

Now, however great steam-producing capacity the locomotive may possess, its Propelling Force is limited by the coefficient of adhesion; and though it can expend its full power in spinning the wheels around, the portion of this power which can be utilized for propelling the train is limited by the amount expressed in Indicated Horse-Power:

I. H. P. = $5.9 \ WfV$,

where W = total weight in tons (2000 lbs.) on the drivers,

f = coefficient of adhesion,

V = velocity in miles per hour.

This formula allows 10 p. c. for overcoming the Internal Resistances in the engine itself (see page 11). The friction at the journals of the driving-wheels, however, is not included among these, but is allowed for in the ordinary Rolling Resistance already dealt with. Thus if we take the weight on each driving-wheel as 6 tons, and f=0.2, the above formula becomes

I. H. P. = 7NV (nearly),

where N = the number of driving-wheels.

Thus, e.g., if, in an ordinary locomotive with four driving-wheels, we have the production of steam equivalent to 400 I. H. P., we see that it is unable to utilize its full power for propelling purposes until it attains the speed of about 14 miles per hour, at which point any slight increase in pressure would cause the wheels to slip. Thus up to a certain speed the propelling power of an engine is limited by the weight on its drivers, but remains more or less constant until that speed is attained, after which, instead of being limited by the adhesion of the wheels, it is mainly a question of the steam-producing power of the boiler,

In ordinary practice, 1 square foot of Grate-surface is able, at ordinary speeds, to maintain the production of steam equivalent to 24 I. H. P.: so that if we know the total grate-surface of an engine and the load on its drivers,—assuming it to be tolerably well-proportioned in its various parts,—we can form a fair idea of its tractive power. The usual allowance of grate-surface varies from about 15 square feet in Passenger Engines to double this amount in some of the Heavy Freight Engines: thus the power of an ordinary Passenger Engine, when working under ordinary conditions, equals about 360 I. H. P., and in the case of a heavy Freight Engine about 720 I. H. P. Both these classes of engines can, and often do, maintain very much higher powers than these, but to work very considerably above them over a long run is a severe tax on the economy of the engine.

DIAGRAM OF PROPELLING FORCE.

10. In order to ascertain the probable effect of a given locomotive on a certain train on various grades and curves, it is best to draw the Line of Propelling Force of the Engine—i.e., the Line of Tractive Power exerted at the point of contact of the driving-wheels with the rails—in lbs. per ton (2000 lbs.), of the weight of the engine and train.

Suppose, as in Diagram II, we wish to find the effect of a locomotive capable of maintaining a working power of 500 I. H. P. having four drivers with 6 tons on each; and let the engine with its tender weigh 60 tons, and the train be the same as that for which the Lines of Resistance are given in Diagram I, namely, 10 loaded box cars, each weighing 20 tons—f being taken as 0.2. We then have a fair example of the working of a Light Freight Engine.

Draw the Line of Propelling Force as follows:

Make
$$OA = \frac{2000 \, Wf}{\text{Tot. Weight of Train}} = 36.9 \, \text{lbs. per ton.}$$

Then draw
$$Aa = \frac{\text{I. H. P.}}{5.9 \, Wf} = 17.6$$
 miles per hour,

which (according to Sec. 9) gives the velocity above which slipping cannot occur. Now the theoretic curve of Propelling Force will be a hyperbola, drawn through a (AO and OH being its asymptotes). This curve may be drawn by offsets from OA thus: At a distance along OA from O equal to $\frac{1}{2}OA$, the offset equals 4Aa; at a distance equal to $\frac{1}{2}OA$, the offset equals 2Aa, and so on; the offset varying inversely as its perpendicular distance from O. Then O, the point of intersection of the Line of Propelling Force with the Line of Resistance, gives the **Limiting Speed** at which the engine can haul the train, under the conditions for which the line of resistance is drawn,—in this case, on a straight level track.

Then, taking any ordinate such as *NMPQ*, the part *NM* included between the Line of Propelling Force and the Line of Resistance gives that portion of the propelling force of the engine in lbs. per ton (2000 lbs.) which goes to overcome the Inertia of the train at the speed indicated.

But this Line of Propelling Force assumes—as we mentioned before—that 10 per cent of the I. H. P. is absorbed in

overcoming the Internal Frictional Resistances of the engine itself—exclusive of the resistance at the journals—independent of the velocity. At low speeds this allowance is considerably too much, but at high velocities it is insufficient; for ordinary speeds, however, it will not be far from correct. The journal-friction forms probably about one third of the whole: the friction of the piston, slide-valve, valve-gear, and cross-heads also contribute considerably to the total. Very little is known as to what allowance ought to be made to cover these resistances,—in fact it is so much a matter of lubrication and mechanical detail that no general formula could be applied,—but undoubtedly they increase with the velocity, and are higher in an engine hauling a heavy train than in an engine running light.

Also we have Back-pressure of the steam in the cylinders, Wire-drawing, and various other causes entering into the question at high speeds which also tend to lessen the effective

Horse-power. - See Note A, Appendix.

11. Now since the loss of power due to these causes depends largely on the rotary velocity of the Driving-wheels, in the case of two engines both developing the same I. H. P. at the same speed,—the cylinders being suitably proportioned, -the engine with the larger wheels will have a great advantage over the other at high speeds, although at low speeds the engine with the smaller wheels will have the best of it. At low speeds—since the initial pressure in the cylinders then differs but little from the boiler-pressure and the back-pressure is practically nothing-an engine with several small drivers will of course have an enormous advantage over an engine of the same I. H. P. with only a single pair of large drivers on account of its being able to utilize so much more of its power, by reason of its higher adhesive qualities. For instance, it would probably tax the engine with large drivers severely to start a train which the other engine could handle with ease; but when the speed reached, say, thirty miles per hour, the engine with the large drivers could work it much more easily and economically than the engine with the small ones. Thus where high velocities are required, -whether on heavy grades or not, provided the weight on the drivers is sufficient, -if the cylinders, etc., are suitably proportioned, the wheels of large diameter are decidedly the best.

Mr. Wellington states that in the case of ordinary Passenger Engines and trains of medium length, 50 per cent of the I. H. P. is consumed in the locomotive itself, overcoming its various resistances—atmospheric, rolling, internal, etc.,—so that only one half of the Horse-power produced is transmitted through the draw-bar.

From the foregoing it appears that a closer approximation to the true line of propelling force at high velocities may be found by drawing it as shown by the dotted line in Diagram II, somewhat below the theoretic line already drawn. The intersection of this line with OH (produced) gives the maximum speed of the engine if unopposed by any external resistances,—i.e., if running free as a stationary engine,—10 per cent only of the power developed being absorbed in overcoming internal resistances.

It must be remembered that the Line of Propelling Force shown in the Diagram is at all points the maximum which can be obtained without exceeding the I. H. P. stated; but by taking a comparatively low value of f, and a high allowance for the internal frictional resistances of the engine at low speeds, we obtain by the method given probably as correct results as can be obtained by any mathematical process.

12. If we require to know what I. H. P. an Engine must develop to haul a certain train at a given velocity V, we can find it at once theoretically by multiplying the total weight of the engine and train in tons (2000 lbs.) by the resistance in lbs. per ton (taken from Diagram I) and multiplying the product by .003V (V being in miles per hour). with the train given in Diagram II, we should need an engine capable of developing about 950 I. H. P. in order to haul it at a speed of 50 miles per hour. The I. H. P. exerted increases nearly as V^3 , and the tractive force nearly as V^2 . The total amount of steam used theoretically, on a run, is nearly proportional to V^2 . The most economical speed, as regards fuel, at which a train can be run-provided the engine is of a power suitable to the weight of the train-is found by experiment to be about 18 miles per hour, and not, as might be expected from Diagram I, at about 8 miles per hour. This is due mainly to the saving in heat owing to the engine being a shorter time on the trip, and also on account of the smaller effect produced by variations in grade at the higher

velocity. To ascertain the Limiting Grade which it is possible to work, we find from the diagrams that an engine and tender weighing together 60 tons, with 24 tons on the drivers, can under ordinary conditions just make head-way up a 12-per-cent grade; and that it is just all two engines of the above description can do to haul a passenger coach up a 10-per-cent grade.

13. The following may be taken as fair examples of the

WEIGHT OF AMERICAN ROLLING-STOCK:

Type.	No. of Drivers.	Weight in tons on each Driver.	Weight in tons, engine and tender, with fuel and water.
Heavy Passenger Engine	4	51/6	55
Consolidation Engine	8	6	75
Decapod Engine	10	7	95

(1 ton = 2000 lbs.)

Box car, empty, weig	ht 10 tons. }	Length	34 feet.
Flat " empty, "	8 "	"	34 "
Passenger car, empty, loaded,	weight 20 tons 25 "	"	50 "
Drawing room car,	" 35 " ;	"	50 to 60 feet.
Sleeping-car, weight,	30 to 45 "	"	50 to 70 "

RESISTANCE DUE TO INERTIA.

14. We are now able to calculate with a fair amount of precision the Propelling Force of an engine and the Total Resistance opposed to it at any given speed. The Difference between these two, such as is represented by NM, in Diagram II, gives the force in lbs. per ton which goes to overcome the inertia of the train: if the Propelling Force be the greater, increasing the velocity; but if the Resistance be the greater, decreasing it.

We will first consider the subject on the assumption that the accelerating force remains constant at all speeds, and that there are no frictional resistances.

It is found by experiment that a force of 1 lb. acting on a weight of 32.2 lbs. (which is perfectly free to move in the direction in which the force is acting) will, after acting on it for 1 second, give it a velocity of 1 foot per second; and that the velocity at all points increases in proportion to the interval of

time during which the force acts: also, that for a given force, the velocity of a body (after it has been acted on by the force for a certain interval of time) is inversely proportional to the weight of the body. Thus the value of the Accelerating Force in lbs. per ton of train equals

$$\frac{1.518\,V}{t}$$

where t = time in minutes during which force acts, and V = velocity in miles per hour acquired in time t.

But this formula takes no account of the force necessary to cause the wheels to rotate; it only allows for motion in the direction in which the force acts. In order to obtain the additional force required to overcome the Rotative Energy of the Wheels, we may imagine the whole weight of each wheel concentrated at a point distant from its axis by an amount equal to the Radius of Gyration of the wheel. For ordinary rolling-stock we may say that this distance equals 0.75 of the radius of the wheel; and the velocity with which a point so situated rotates round the axis equals 0.75 the velocity of the train. Now the ratio of the weight of the wheels to the total weight of a train of medium length varies from about 0.1 to 0.25, according to whether the cars are loaded or empty, the proportion in the case of Passenger Cars being about the same as with Loaded Freight Cars. Therefore the Total Force necessary to overcome the entire Inertia of the train varies from about

$$F = \frac{1.6 V}{t}$$
 to $\frac{1.7 V}{t}$,

where F = constant accelerating force in lbs. per ton (2000 lbs.) of train.

The former value is applicable to Loaded and the latter to Empty cars.

As regards the distance covered by the train from the starting-point to the point at which it attains the velocity V, it can be found by the formula

$$S = 44Vt$$

where S = distance in feet.

15. Now the force required to stop a train travelling with a certain velocity, in a given time, equals the force which is necessary to give it that velocity in the same time; so that the

formula given above for F applies to the resistance caused by the Application of Brakes, as well as to the Propelling power of the engine. Now, since,—as in the case of the driving—wheels of a locomotive,—as soon as slipping begins, the adhesion at the rails decreases rapidly, therefore, in applying the brakes, the pressure should be such that the wheels will just roll on the rails; i.e., the resistance on the brakes must not be allowed to exceed the resistance at the rails, but should be as near to this limit as possible. If the pressure on the brakes could be adjusted so as to effect this in practice, we should have an efficiency for the brakes equal to the coefficient of adhesion, which we have already considered under ordinary circumstances to equal 0.2.

But it is found that with **Automatic Brakes** we cannot generally rely on a greater efficiency than 0.12, which is equal to a value of F (if the brakes are applied to the whole train) of 240 lbs. Thus the brakes may be said to offer a resistance equivalent to a 12 p. c. grade.

In the case of Hand Brakes it usually takes about four times as great a distance in which to stop a train when they are used, as with Automatic ones applied to the whole train.

Suppose under the above assumption we have a passenger-train running at a speed of 60 miles per hour. It steam is shut off at the same instant that the brakes are applied automatically—with an efficiency of 0.12—to three quarters of the weight of the train, the retarding value of F would equal $.75 \times 240 = 180$ lbs. per ton, and thus by our previous formula gives a value for t = 0.53 minutes, from which we can obtain S = 1400 feet. Had the train being going at only 30 m. p. h. instead of 60, it could have been pulled up in one half the time and one quarter the distance it required to stop it when running at 60 m. p. h. Thus in order to stop a train going at 60 m. p. h., we must apply four times the amount of brake-resistance which would be required to stop it if going at 30 m. p. h. in the same time.

16. So far we have dealt only with a change of velocity from Rest to V, or from V to Rest. Suppose, however, in the former case that the train, instead of being at rest, before the accelerating force F is applied, has an Initial Velocity (v). The formulæ given in section 14 then become changed, F in

this case varying from about

$$F = \frac{1.6 (V - v)}{t}$$
 to $\frac{1.7 (V - v)}{t}$,

and

$$S = 44 (V + v)t$$
.

And just as the previous formulæ applied to either an accelerating or retarding force, so these apply equally well to the Propelling Force of the Locomotive or the Resistance of the Brakes.

As an Example, suppose we take a Passenger-train running at 50 miles per hour. The value of F necessary to reduce this speed to 30 m. p. h. in one minute $=1.6\times20=32$ lbs. per ton, which gives a resistance equivalent to a+1.6 p. c. grade. Problems such as the above, where the value of F is assumed constant, where no account is taken of the frictional resistances, and in which the question of the time t is not directly involved, may often be solved more simply still by means of the Table of Equivalent Heights given below.

HEIGHT CORRESPONDING TO VELOCITY.

17. In the above example of the train running at 60 m. p. h. being brought to a stand-still, if the brakes had been applied to the whole train with an efficiency of 240 lbs. per ton, it would have been stopped in a distance of about 1056 ft.; or, putting it in another way, the train could have run up a 12 p. c. grade for a distance of 1056 feet before stopping, showing that it had—stored up in it—the Energy necessary to raise itself vertically through a height of about 127 feet. In a similar way—without going into the subjects of Kinetic and Potential Energy—every velocity may be shown to have a corresponding vertical height.

Now about 5.6 p. c. of this rise, in the case of trains, is due to the Rotative Energy of the wheels (when dealing with loaded cars) and the remainder is simply the height from which a body must fall under the influence of a force equal to its own weight,—i.e., gravity,—in order to obtain the velocity in question. But since this Rotative Energy is taken account of in the previous formulæ, we can, by finding the value of S when F = 2000, obtain for any given velocity the corresponding vertical height.

In this way the following table has been calculated for Passenger or Loaded Freight Cars.

For a train of Empty Freight or Flat Cars, 6 p. c. should be added to the heights given.

TABLE OF HEIGHTS IN FEET CORRESPONDING TO VELOCITY IN MILES PER HOUR.

	Vel.	0	1	2	3	4	5	6	7	8	9
-	10	3.5	4.3	5.1	5.9	6.9	7.9	9.0	10.2	11.4	12.7
1	20	14.1	15.5	17.0	18.6	20.2	22.0	23.8	25.7	27.6	29.6
	30	31.7	33.8	36.0	38.3	40.7	43.1	45.6	48.2	50.8	53.5
1	40	56.3	59:2	62.1	65.1	68.2	71.3	74.5	77.8	81.2	84.6
	50	88.0	91.5	95.1	98.9	102.7	106.5	110.4	114.4	118.4	122.5
-	60	126.7	131.0	135.3	139.7	144.2	148.7	153.3	158.0		167.6
1	70	172.5	177.4	182.5	187.6	192.8	198.0	203.3	208.7	214.2	

Now if we have a Passenger train running at a speed of 20 m. p. h., and we wish to know what its velocity will be after descending 1000 feet of a 3 p. c. grade—ignoring as before frictional resistances—we can find it at once from the Table, thus: Its velocity at the foot of the grade will be that due to the height corresponding to a velocity of 20 m. p. h. + 30 feet = 44.1 feet, which corresponds with the velocity required, namely, 35.4 miles per hour. Or, suppose we wish to know what rate of grade would be required to decrease the speed of the above train from 40 m. p. h. to 25 m. p. h. in a distance of 1000 ft.: we have

Height corresponding to 40 m. p. h. = 56.3 feet
"
" 25" = 22.0"

Difference = 34.3 feet.

Thus it is a 3.43 p. c. grade that would be required.

18. So far we have dealt only with the Inertia of the train on the supposition that the propelling force of the engine is constant at all speeds, and that there are no frictional resistances. A method much in use in practice which partially corrects for both these fallacies is that of allowing for the mean frictional resistance and the mean propelling force of the engine, and then, by the aid of formulæ similar in effect to those given above, obtaining approximate values of S.

19. But this method of averaging gives very unreliable results when dealing with any but comparatively low velocities, so that the following Graphic Method, which is extremely

simple, is in most cases preferable, since the correctness of the results obtained by it depends almost solely on the care employed in working it.

Let the Lines of Resistance and Propelling Force be drawn as in Diagram II.

Take any ordinate NQ, and make $PQ = \frac{OQ}{NM}$.*

Similarly take other ordinates, and thus fix other positions of the point P.

Draw the curve *OPD* through these points. Then, if (as in Diag. II) 1 inch vertical = 10 lbs., and 1 inch horizontal = 20 miles per hour, the area (shown shaded in Diag. II) enclosed by the curve *OPD*, the line *OH*, and the ordinate corresponding to any given velocity gives the distance covered while attaining that velocity, using as a scale 1 square inch = 1 linear mile. (See Note B, Appendix.) And as a consequence of this, assuming, e.g., the train has an Initial velocity of 20 miles per hour, and a final velocity of 34 miles per hour, the area between the ordinates of 20 and 34 m. p. h. gives the distance traversed while the speed is being raised from the lower velocity to the higher.

By the ordinary method of averaging, at a speed of 34 m. p. h. the distance would be represented by the area Opq, instead of the shaded portion. This shows the little dependence to be placed on the averaging process, when dealing with

speeds which approach the limit.

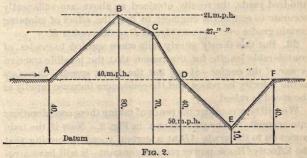
But there is a correction to apply to this if we wish to allow for the Rotative Energy of the wheels; and this, as we have already seen, varies from about 6 to 12 p. c. of the total energy of the train; so that in the case of Passenger or Loaded Cars 6 p. c. should be added to the distance as obtained above, and in the case of Empty Cars 12 p. c.

20. This method may be applied to a variety of problems in Railroad Dynamics: thus, for example, suppose we have a train travelling at 60 m. p. h., and we wish to know how far it will run if the brakes are suddenly applied, causing an additional resistance of 20 lbs. per ton—of entire train. Then the line of total resistance will be given by the dotted line EG (Diag. II), and the value of MN at any given speed will equal the entire ordinate from OH to the curve EG, for the

^{*} All measured in inches on the diagram,

line of propelling force then coincides with OH—i.e., equals zero. Or, conversely, if the train be pulled up in any known distance, we can by two or three trials ascertain the efficiency of the brakes. If in dealing with such problems as these we have in the course of the distance travelled various rates of grade and curves of different "degree," we can, without serious error, draw our line of resistance for the mean grade and the mean degree of curvature.

21. We are now able to ascertain the effects of various amounts of Rise and Fall on the velocity of a train. In the first place, we will go back to our former assumption that the engine exerts the same tractive force at all speeds, and that there are practically no frictional resistances. Of course this is a thoroughly erroneous supposition, but by adopting it we simplify matters very considerably, and yet at the same time are able to obtain results which, for practical purposes, are sufficiently correct when we limit their application to comparatively short distances.



In Fig. 2 let ABCDEF represent the grades on a limited portion of a certain road, theu—under the assumption already made—if we have a train running along the level towards A at a uniform speed of 40 miles per hour, we obtain from the Table of Equivalent Heights in Sec. 17—

Vel. Head in ft. at A = 56, because V = 40 m. p. h.

- " B = 56 40 = 16; ... Vat B = 21 m. p. h." C = 16 + 10 = 26; ... " C = 27"
 " D = 26 + 30 = 56; ... " D = 40".
- " E = 56 + 30 = 86; ... " E = 50 " F = 86 30 = 56; ... " F = 40 "

By determining the speed at a few such points as these, and drawing through them the dotted lines as in Fig. 2, we have practically a **Profile of Velocities**, from which we can read approximately the speeds at different points on the grade.

22. In such a case as the above the strain on the draw-bar of the engine would at all points be constant, and the amount of work done in transporting the train from A to F would—ignoring the difference in distance, which of course in practice amounts to nothing—be the same whether the train went along the grade ABEF, or along a level grade ADF.

Now the effect of running over such a ridge as ABD is to lower the average speed: thus if running from A to D on the level, the train would arrive at D much sooner than by way of ABD. Again, in running over the grade DEF, its average velocity would be much higher than along the level DE. Thus the ridge ABD is detrimental to high speeds, but the depression DEF tends to raise the average velocity. In dealing with cases where the distance AD or DF does not exceed a few hundred yards, the results obtained as above are sufficiently accurate to enable the engineer to find the effect of adopting certain grades over such a ridge as D or depression E.

23. But this theory utterly fails when applied to grades of considerable length, for the reason that the possible tractive power of the engine—at any but the lower speeds—decreases as the velocity increases, and the resistances increase rapidly as the speed is raised.

We will now consider the result of taking these considerations into account in the case shown in Fig. 2. Now if the train comes on to the grade AB at a certain speed—assuming that the Effective Horse-power remains constant—it will have a velocity at B appreciably greater than that which we should obtain for it at that point by means of the Table of Equivalent Heights. So also at D it will have a velocity greater than it had at A, although by the Table the velocity at A and D should be the same. The reason of this is, that the increase in the accelerating force is more than in proportion to the increase in the total propelling force, being due to a decrease in the resistances as well as to the reduction in speed. Similar reasoning applies to the down-grades BC and CD, so that by the time the train has got to D the total amount of work done on the higher grade is relatively less than what it would have been along

the level AD, owing to the reduced frictional resistances. Thus the train is travelling faster at D than it was at A, although it has lost time on the way. Similarly, in the case of crossing a depression such as E, the amount of work done will be greater by the lower route than along the level, and the train will thus have at F a velocity less than it had at D, although it will have made better time between D and F by way of E, than along the level DF.

But although the train arrives at D with a higher velocity than if it had proceeded along the level, yet this increase in velocity only partially makes up for the time lost between A and D. So also the decrease in speed at F does not entirely counteract the gain in time made along DEF.

The amounts by which the velocities at D and F actually differ from those obtained by the Table, depends mainly in practice on the distance between A and D, or D and F. The greater these distances are, the less reliance is to be placed on the Table; so much so in fact in dealing with long grades, as to render the energy of the train itself—considered as a store of available tractive power—practically worthless.

24. It is usual for Railroad Companies to adopt a certain rate of grade which is not-except where Pusher-grades are used-to be exceeded. This is usually termed the Maximum or Ruling Grade, and is selected with due consideration to the tractive power of the locomotives to be employed. the probable amount of traffic, the weight of trains to be hauled, and the speed required to be maintained. It is also selected in most cases so as to admit of a train starting on the grade, if by any chance it should have had to pull up. Also, it should be such that the locomotive employed can haul the train over it, altogether independent of the Momentum-or more correctly Energy-of the train. By means of Diagram II we can readily select the most suitable Maximum Grade by drawing the line of resistance—for a level track—and the line of propelling force suitable for the locomotives to be employed; the length of the ordinate NM, when scaled off, gives the equivalent resistance in lbs. per ton of the maximum grade. Thus, in the case of the example given in Diagram II, if the speed required to be maintained on the grade equals 24 miles per hour,—since NM represents to scale about 17 lbs. per ton,—the maximum grade will equal

0.85 p. c. Had the required speed been only 10 miles per hour, we might then have used a 1.6 p. c. grade. But probably in neither of these cases could the train start on the grade. and in order to allow for this, we must assume that the line of resistance at no point dips below 15 lbs. per ton,-i.e., 12 lbs., in accordance with Sec. 3, and a small margin of 3 lbs. to overcome the Inertia of the train. - Thus, allowing for stoppages, if a speed of 24 m. p. h. is to be maintained in the case shown in Diagram II, the maximum grade must not exceed 0.55 p. c.; but if 10 m. p. h. only is required, then-including allowance for stoppage—the maximum grade may be 1.1 p. c. But we must remember that where the velocity required to be maintained on the maximum grade exceeds that given by Aa, in Sec. 10, some allowance should be made for the probable increase in boiler-pressure after the train has come to a stand-still; which means that on starting, the I. H. P. of the engine may be placed considerably above its normal working power.

25. Without going into the question of the Economy of the Steam-engine, we may say that a Locomotive works with its greatest efficiency when the boiler-pressure remains constant and the engine is running at a uniform velocity. Thus fluctuations in speed or variations in the opposing resistances are more or less detrimental to the working of the locomotive.

As a consequence of this, if a certain elevation has to be attained, in order to make the work as easy on the engine as possible, the grade should be such as to render the sum of the resistances opposed at all points as nearly constant as possible. Thus, if the alignment be straight, the rate of grade should be uniform; but if curves or other irregularities occur, they should be compensated for, so that a constant resistance may be maintained.

26. Compensation for Curvature.—From Diagram I we see that at 10 miles per hour the resistance for each degree of curvature is about 1 lb. per ton, i.e., equivalent to a + 0.5 p. c. grade, and that at about 30 m. p. h. it is about half this. The rate, however, usually adopted is .03 p. c., which is suitable to a speed of about 25 m. p. h. Thus, if the equivalent grade on a tangent is 1.5 p. c., we must reduce it on a 3° curve to 1.41 -p. c. in order that the resistance may remain constant.

27. Compensation for Brakes, etc.—A point to be remembered in running a long uniform grade which does not approach the maximum is to consider at what points the train will be required to slacken or increase its speed. For example, suppose on such a grade we have a sharp curve around which the speed is not to exceed 20 miles per hour, but that on the tangent at either end of it a speed of 40 m. p. h. can be maintained. By means of the Table of Equivalent Heights we can adapt the Energy of the train so that the velocity will be reduced without the application of the brakes, and that when the curve is passed the speed of the train can be more readily increased from 20 to 40 m. p. h. But in doing this we have to be careful that at the lower end of the curve we do not increase the grade so as to tax the engine too severely. At all such points as crossings, where short stoppages are required, attention should be paid to this, for by so doing we can at times save something even in the cost of construction, besides saving considerably in fuel and in wear and tear to the Rolling-stock.

28. But though the operating-expenses may be reduced to a minimum by the use of Long uniform (equivalent) grades, the amount necessarily expended on their construction may be too great to warrant adopting them. In such cases Broken Grades have then to be used.

Now we have already seen how to obtain the effect of undulations on the velocity and the work done, so that we can in any particular case determine for ourselves what will be the result of selecting a certain arrangement of grades. The following "pointers," however, deduced from what has already been said, may come in handy.

- 1. A Rise from the uniform grade is detrimental to fast traffic, and though there is a saving in actual work done on it, there is probably no saving in the consumption of fuel.
- 2. A Depression from the uniform grade tends to increase the mean velocity, but at the cost of a considerable amount of extra fuel.
- 3. Breaks in the grade which—from the point where the broken grade leaves the uniform one to the point where they next intersect—do not exceed, say, 1000 to 2000 feet, may be regarded as "Momentum Grades," and accordingly are not so injurious as longer breaks where the Initial Energy of the

train is small compared with the Total Energy to be expended on them.

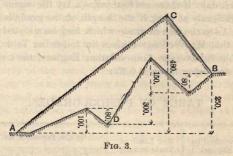
- 4. The nearer the uniform grade approaches the "Maximum grade," the more injurious do any breaks become; and the only point in connection with the "Maximum grade," where an increase in the rate is allowable, is the insertion of a "Momentum grade" at its lower end.
- 5. Breaks in a grade are more injurious to slow than to fast traffic—as may be seen from the Table of Equivalent Heights—e.g., an increase in elevation of 20 feet reduces the velocity from 30 to miles per hour, while a velocity of 60 m. p. h. is only reduced to about 55 miles per hour.
- 6. Be careful in inserting Momentum grades that they will not be such as to cause the velocity at any point to exceed the safe limit. A difference in elevation of about 30 feet between the Broken and the Uniform grade should generally be taken as a limit.
- 29. Another point to be considered, which we have not yet referred to, is the increase in Liability to Danger of Breaking-train and Derailment to which an undulating grade gives rise. For, suppose in Fig. 2 we have a train running up the grade from A to B: as soon as the engine is over the summit the pull on the draw-bar becomes enormously increased, and similarly with the car-couplings throughout the entire train; so that, unless the greatest care is taken in applying the brakes, the train runs a very great risk of being broken in two. Similarly, in such a hollow as E, the cars near the centre of the train are liable to get terribly jammed together, thereby greatly increasing the chances of Derailment.

Vertical curves reduce these dangers considerably, but not entirely.

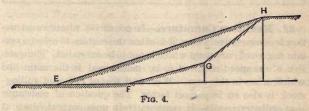
It must be remembered that it is not in the least necessary that one of the grades should be an up-grade and the other a down-grade: it is the difference in the rate of grade that has to be looked out for. (See Sec. 100.)

30. In Fig. 3, let ACB and ADB represent two different routes between A and B, the total Rise and Fall between the two points in each case being the same. The amount of work done in hauling the train from A to B by way of C will, supposing we are dealing with grades so long that the ques-

tion of "Momentum Grades" may be ignored, be then practically the same as by way of D. Similarly, if such a point as H in Fig. 4 has to be reached, the work done in hauling the train along the uniform grade EH will be practically the same as by way of FG. It is not the amount of work done on the grades themselves that has to be considered, but the amount of extra work which is uselessly done by a heavy engine hauling a large surplus of dead-weight (due to its own size) over



grades where a lighter engine could have hauled the train equally well. If each of the divisions EF, FG, and GH were a suitable length for one engine to work, the lower route would then be as economical probably as regards Operating Expenses as the higher. Besides this, we have the increased



consumption of fuel, before referred to, which always accompanies variations in grade.

If we make each of the divisions along the lower route from E to H of such a length as to keep the engine employed on each fairly busy,—using a different engine on each division,—the lower route is then as economical as can be wished for, but otherwise the upper route has the advantage.

31. Now the average length of an Engine-stage may be considered to be about 100 miles, which is of course too long to enable us to work the lower route in the manner described above. We may often, however, by adopting a Pusher-grade, even at a point where at first it appears unnecessary, make a decided improvement in the economy of our grades. The length of this grade, if the Pusher is to be kept steadily employed, depends of course on the number of trains to be taken up it each day: if there are four trains a day the engine will be kept sufficiently at work if the length of the grade is only 12 miles. As to the rate of grade which may be adopted in such cases as this, Mr. Wellington gives the following Table, which is suitable for average Consolidation Engines, the coefficient of adhesion being taken at 0.25:

TABLE OF PUSHER-GRADES.

Grade worked by	Net Load of	GRADE POSS	IBLE WITH-
one Engine.	Train in tons.	1 Pusher.	2 Pushers.
Level.	2675	0.38	0.74
0.2	1758	0.75	1.26
0.5 1.0	1147 711	1.30 2.16	2.01 3.13
1.5	504	2.96	4.13
2.0	383	3.72	5.03

32. Maximum Curvature.—In countries where construction is comparatively easy, it is often the custom to select a certain degree of curvature which is not to be exceeded. The question of the speed required to be maintained is the main one which arises in this case. Wear and tear of rails and rolling-stock is also an important factor. The question of resistance—at ordinary speeds—is comparatively unimportant, since at a speed of 25 miles per hour a 10° curve only offers the resistance of about a 0.3 p. c. grade. In rough country it is impossible to fix a "maximum," for the additional cost of construction which the adoption of a limiting-grade might involve would perhaps be an inconceivably greater consideration than the loss of a few seconds—or possibly minutes—in time. As regards the question of the Safe Speed on Curves, it is diffi-

cult to lay down any law, but it is supposed to vary inversely as the square root of the radius. Thus if we assume that 40 miles per hour is a safe speed on a 2° curve, the speed should be limited to 20 m. p. h. on an 8° curve and to 14 m. p. h. on a 16° curve. The chances of derailment and the wear and tear of rolling-stock and rails are decreased materially by the use of Transition curves. (See Sec. 96)

- 33. It is almost unnecessary to refer to the subject of Reverse Curves. In Station-yards, where the speeds are insignificant, their use is sometimes advisable; but on the Main Track an intervening tangent of at least 200 feet in length should be regarded as an absolute necessity. A fault much more frequently found is the insertion of a short tangent between two curves of the same direction. Getting on to a tangent from a curve is as hard work as getting on to a curve from a tangent; and since it is at the P. C. and P. T. that the curve gives its maximum resistance, the curves should at least be compounded so as to make the radius of curvature at all points as uniform as possible, for in each case the total amount of curvature will be the same. Another point to be remembered-though it is not often that it can be applied-is, that a road which has its curves at points where the speed is comparatively low has a decided advantage over one in which the curves are located at places where a high speed is required to be maintained. Thus, if a certain amount of curvature has to be got in, in such a place as DEF in Fig. 2, it should be arranged if possible so that the curvature at D and F will be sharper than at E. Curvature should also be avoided as much as possible at all points where a stoppage is required, for on starting, the resistance due to the curvature is a great consideration, and, as we saw in Sec. 6 and Diagram I, will probably make it as difficult for the train to start as a decided up-grade.
- 34. We have now dealt in a more or less superficial way with most of the mechanical problems which arise in connection with railroad trains; but it is convenient, for the sake of more readily comparing the value of the various resistances to passenger and freight trains at average speeds, to tabulate their mean values (as given by Prof. Jameson) as follows:

TABLE SHOWING COMPARATIVE VALUES OF RESISTANCES
AS REGARDS WORK DONE.

Items.	Distance.	Curvature.	Rise and Fall.
1 mile	5280 feet.	600°	25.0 feet. 0.041 "
1 foot Rise and Fall	211.2 "	240	1.0 "

"Rise and Fall" of course means in one direction only, and is so stated in order to take account of the Rise when running in the opposite direction. Thus in Fig. 3 the total Rise and Fall between A and B by either route equals 710 feet.

COST OF OPERATING.

35. The expense involved in overcoming the resistances referred to in Sec. 34 is not proportional to the amount of work which is performed on account of them. For instance, it is found by experience that hauling a train over one mile of level track costs on an average about the same as 150 feet of rise and fall,—not of 25 feet, as given in the last table. Similarly, with curvature, the operating of one mile of level track is found to cost the same as about 900° of curvature (not 600°); so that as regards operating-expenses the table given in Sec. 34 becomes—

Items.	Distance.	Curvature.	Rise and Fall.
1 mile	5280 feet. 5.86 "	900°	150 feet. 0.166 "
1 foot Rise and Fall.	35.2 "	60	1.0 "

As soon, then, as we know the expense of operating one mile of level track, we can by means of this table find the probable cost of working any certain grade or any given amount of curvature.

36. Taking \$1.00—it is probably nearer 90 cts.—as the average cost of operating one mile of level track on American Railroads for each train that runs over it (and returns) each day, we can make this our unit of operating expenses and

term it the cost of one Train-mile. The items which go to make up the expense of the train-mile are as follow:

Motive Power.... {
 Oil, Fuel, Waste.
 Driver, Fireman.
 Repairs.

Train Expenses... {
 Train Hands.
 Repairs and Renewals to Cars.

Road Repairs Track, Road-bed, Structures.

General.... {
 Stations, Terminal, Taxes.
 Repairs and Renewals.

Taking, then, \$1.00 as the cost per train-mile, and assuming the interest on the amount capitalized at 6 p. c., we obtain the following table:

Unit.	Value per annum per daily train.	Amount Capitalized.
1 mile	\$350	\$5,833.33
1 foot	0.066	1.10
1º Curvature	0.39	6,50
1 foot Rise and Fall	2.33	38.88

This assumes that each "daily" train only runs 350 days in the year, which makes a sort of allowance for Sundays, "specials." etc.

37. From the above we see that if we have ten trains making the round-trip every day, we are entitled to spend \$58,333 extra on the construction of a certain route, if by so doing we can save a mile of level track; so also we should be entitled to spend \$388 in the reduction of a foot of rise and fall. Thus with 10 daily trains we might safely expend $2 \times $388 = 776 in lowering (only one foot) such a summit as C in Fig. 3; but if C had been the terminus of the line AC we ought only to spend \$388 in lowering it one foot.

Suppose again we have two routes to select from, one of which would probably cost \$40,000 more than the other, but would shorten the distance by one mile and would save a rise and fall of 100 feet. Then if there are only likely to be three trains running—including returning—each day, we are not entitled to spend more than $(\$5833 + \$3888) \times 3 = \$29,163$ to save the above distance and rise and fall; therefore it would probably be injudicious to adopt the more expensive route.

38. As regards the cost of operating Pusher grades, we find that a Pusher kept pretty busy costs on an average about \$280 per mile of incline per annum—i.e., \$140 per mile run—"all that the engine fails to do below 100 miles per day may be assumed to cost from ½ to ½ as much as if it had been run, and is so much added to the cost of what is run." Thus on a 5-mile incline, with only 4 trains to be taken up it each day, the probable annual expense of the Pusher will be found thus:

Work done,
$$4 \times 5 \times $280 = $5,600$$

Work not done, $30 \times \frac{$280}{4} = 2,100$
Total..... $$7,700$

Had we been able to reach the summit without adopting a Pusher-grade—supposing the total rise and fall to be 1000 feet—the cost of "Rise and Fall" would have been for the 4 daily trains $4 \times 1000 \times \$2.33 = \9320 , representing a difference in the operating-expenses of \$1620 per annum, which at 6 p. c. would have warranted our expending \$27,000 more on the route which involved the Pusher-grade, assuming curvature and distance to be the same in both cases.

39. To test the merits of different routes as regards operating-expenses, we may express them in terms of their Equivalent Lengths (L) in miles thus:

$$L = l + \frac{H}{150} + \frac{C}{900},$$

where

l =actual length in miles, H =total rise and fall in feet, C =total curvature in degrees.

40. As regards the increase in operating-expenses caused by any slight increase in distance, such as is the result of changes in the alignment, it is not usually the case that the cost per train-mile for any small additional distance is as high as the rate already given; for many of the items, such as station and terminal expenses, which go to make up the average cost per train-mile, are not affected by an addition in distance which does not exceed 2 or 3 p. c. of the total length of the road. Thus, in selecting the choice of two routes, the engineer

should not necessarily take the average cost per train-mile as his standard by which to find the probable difference in the operating-expenses, but in most cases may consider about 50 cents per train-mile an amply sufficient allowance for that portion of the longer route which is in excess of the other, when that excess does not exceed the above amount.

41. In order to approximate as closely as possible to the probable cost per train-mile on any projected road, the engineer must judge by the results on other roads where the conditions are more or less similar. Where changes are to be made in the alignment of a road already in operation, the value of the proposed improvements can then be found with considerable accuracy, since the cost per train-mile is then known.

RECEIPTS.

42. The Receipts usually vary from about 1.5 to 2.0 the cost of operating; and it is not often that the locating-engineer has it in his power to affect them in any way. He may, however, by carrying the location by a slightly more circuitous route than he would otherwise have adopted, catch the traffic of some outlying village. Mr. Wellington on this subject says: "When the question comes up of lengthening the line to secure way-business, we may almost say that where there seems any room for doubt, it will almost always be policy to do so. Extra business to a railroad—the engineer will rarely err in thinking—is almost always clear profit. Of Passenger business this is literally true until the increase becomes considerable; of Freight business it is so nearly true that 80 or 90 per cent at least of the way-rate is clear profit over the usual cost of any particular shipment."

Thus, suppose we are projecting a line between two points 100 miles apart, and that half-way between them lies a small town 10 miles off the direct route. The additional distance involved in running through it is about 2 miles. Suppose, as is a reasonable estimate, the average payment per head of population is \$13 per annum. Then, if there are likely to be 5 daily trains, we may put the extra cost of the two miles, including the interest on the capital spent on their construction, at about \$2000 per annum. Therefore, looking at the matter

only from this point of view, if the place contains, or is likely to contain before long, only about 150 people, it would probably be wise to locate the road through it.

COST OF CONSTRUCTION.

43. This is a subject which had almost better be omitted, for the range of prices is so great in different parts of the country, that values given to suit one place may be entirely misleading when applied to another place a few hundred miles off. I have, however, endeavored to strike the average prices as nearly as possible, and with these remarks they must be taken for what they are worth. They show more or less the relative cost of various works, and in this way may sometimes be of service.

First we have the following lot common to all track:

Steel rails per ton (2000 lbs.)\$25	00	to	\$45	00	
Angle-bars, per lb	02	66		03	
Bolts, "	03	66		05	
Spikes, "	02	66		04	
Ties (in place), each	20	66		50	
BallastGravel, p. cu. yd	25	66		75	
" Broken Stone, p. cu. yd	75	66	1	50	
Track-laying per mile	00	46	500	00	

Then we have the following, according to circumstances:

Solid Rock, per cu. yd				\$ 2	00
Loose Rock or Hard Pan, per cu. yd		35	66		75
Earth, per cu. yd		10	66		50
1st Class Masonry, per cu. yd	10	00	66	30	00
2d " " "	7	00	66	10	00
3d " " "	5	00	66	7	00
Dry rubble "	2	00	66	5	00
Riprap, per cu. yd	.1	00	66	2	00
Iron erected in bridge-work, per lb		04	66		08
Timber in Trestles, per M	25	00	66	45	00
" " Culverts, "	15	00	66	25	00
" " Log Culverts, per M	10	00	66	20	00
Piling driven, per lin. ft		25	66		75
Grubbing, per Station	12	00	66	20	00
Clearing, per acre	20	00	86	30	00
Overhaul, p. cu. yd. per Sta		01	66		02
Fencing per mile of track	300	00	66	800	00
Telegraph line—Single wire				250	00

By taking the mean prices of the first set, we obtain for an average mile of standard-gauge track (10 p. c. short rails) the following cost:

103 tons Steel rails (65 lbs. p. yd.)	.\$3,862	00
710 Angle-bars, 20 lbs. each	355	00
1420 Bolts, 7 kegs, 200 lbs. each	56	00
5670 lbs. Spikes, 38 kegs, 150 lbs. each	171	00
2640 Ties	924	00
Ballast, 3667 cu. yds. Gravel	1,834	00
Track-laying	375	00
Total	.\$7,577	00

Besides these we have, of course, Right of Way, Engineering, Law, and a variety of Incidental expenses.

As regards the cost of trestlework, we find that for Low Pile Trestles—say 20 ft. high—assuming piling to cost 50 cents per lin. ft. driven, and the superstructure \$20 per M., the cost will usually be about \$6 per foot run.

For a Wooden Trestle 50 feet high at \$25 per M., the cost, if resting on piles or sills, will usually be about \$10 per foot run; but if 100 feet high, \$20 to \$25 per foot run.

The cost of Iron Trestlework varies so enormously according to the design, that it is impossible to lay down any figures which might be generally applicable. Assuming, however, that the total weight of iron in the trestle equals the total weight of wood in an equally strong wooden trestle, the cost, at 5 cents per lb., would be about double that of a wooden one. These figures are of course exclusive of Masonry foundations, and are for single-track.

As regards the cost of trusses, a Wooden Howe Truss—single-track, of 100 ft. span, Lumber at \$15 per M.—costs, framed, somewhere about \$2000; and an Iron Truss of the same span, at 5 cents per lb, costs about \$5000. The cost in both cases varies pretty much as the square of the span. Erecting usually costs from \$5 to \$10 per lin. foot.

As regards the cost of tunnelling, we may say it varies from \$2.50 to \$7.50 per cu. yd.; so that for a single-track tunnel we may consider the price per foot run to vary from about \$30 to \$80, including masonry. The cost of sinking a shaft or driving a heading is considerably higher in proportion than this.

For more on the subject of the Cost of Grading, see Sec. 124, Part II.

INSTRUMENTS.

44. The principal Instruments ordinarily used on Railroad Location are: The Transit, Compass, Level, and Hand Level; and we will consider them in the order here given. (For Instruments used on exploratory-work, see Secs. 141 to 158.)

THE TRANSIT.

Before proceeding with the adjustments of the Transit, it should be seen that the object-glass is screwed firmly home, and a short scratch made on the ring of the glass and continued on to the slide, so that, should the glass be taken out or work loose, it may be screwed up to exactly the same position it was in before. If this is not done, and the glass happens to be badly centred,—i.e., its optical axis does not lie in the centre of the telescope-tube,—if by any chance the glass is moved, the Line of Collimation will also be thrown out of adjustment.

The following are the usual adjustments for a Transit:

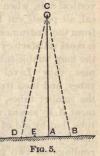
A. To make the vertical axis truly vertical by means of the small bubble-tubes. Turn the vernier-plate until each of the tubes is parallel to a pair of opposite plate-screws. Bring both bubbles to the centres of the tubes. Then turn the instrument through about 180°. If the bubbles are still in the centre, the adjustment of the small tubes is correct; but if not, correct for half the error in each case by means of the adjusting screws at the ends of the tubes. This adjustment should then be correct; if not, repeat the process until it is.

B. To set the cross-hairs truly vertical and horizontal.—After levelling up, test the vertical hair along its whole length on some fixed point, and if not correct, loosen the capstan-headed screws and move the diaphragm around. The horizontal hair may be tested in a similar way.

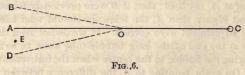
C. To make the horizontal axis of the telescope truly horizontal.—Level up the instrument and point the telescope to some object C, as in Fig. 5, at an altitude, if possible, of not less than 45° . Mark the point A where this vertical plane strikes the ground. "Reverse" the instrument, and

if on pointing to C and then reducing to the ground we again

strike A, this adjustment is correct. But suppose the first time the "vertical" plane had struck the ground at B, and then on reversing, instead of striking B again, it cuts through some point D. Mark a point E between D and B, distant from D by one quarter of DB. Then by means of the screws under one of the pivots of the horizontal axis bring the intersection of the cross-hairs to strike the point E. This adjustment should then be correct.



D. To make the line of collimation perpendicular to the horizontal axis.—Having levelled up the instrument at O, in Fig. 6, point the telescope to some object C. Turn the telescope over and mark the point A, at a distance AO



equal to about OC, where it strikes the ground in the opposite direction. By making AO = OC we then obtain a correct adjustment for the line of collimation, even though the object-slide is defective; that is the only reason for making AO and OC about the same length. Reverse, and again point to C; if on turning the telescope over once more it again strikes A, this adjustment is correct. But if instead of intersecting A it cuts through some other point D, then mark a point E between D and B, distant from D by one quarter of DB, and by means of the capstan-headed screws move the diaphragm so as to bring the intersection of the cross-hairs to coincide with E. This adjustment should then be correct. This is liable to throw out adjustment B slightly, so watch that at the same time.

E. To make the long bubble-tube parallel to the line of collimation.—Level up the instrument and clamp the vertical arc. By means of the tangent-screw of the vertical arc bring the bubble to the centre of the tube. Then if the

small bubble-tubes were sufficiently sensitive to render the vertical axis, when the instrument is levelled up, truly vertical, all points cut by the line of collimation equally distant from the instrument would have the same elevation. But it is more satisfactory to obtain a truly vertical axis by means of the long bubble-tube itself, on account of its greater sensitiveness; thus: Level up as accurately as possible by the small tubes, and then treat the long bubble-tube as if it were one of the smaller tubes, putting it into a temporary state of adjustment A, by means, not of the screws at the ends of the bubbletube, but by aid of the tangent-screw of the vertical arc, and then by its means obtain a truly vertical axis. Then take the readings on two points A and B equally distant from the instrument and in opposite directions; next move the transit to a point about in the same straight line as A and B, but at as short a distance beyond either of them as the instrument can be focussed to read and level up by the small tubes. Take the reading at A, say 3.43; then if B were previously found to be 1.84 feet higher than A, the telescope should read 1.59 on B if this adjustment were correct. If we do not read this, the screws at the end of the long bubble-tube must be so altered as to bring the bubble to the centre when the instrument reads 1.59. On again pointing to A, the difference between A and B should then be almost 1.59. If it is not quite 1.59, proceed as before until the adjustment is correct.

By moving the instrument into the same line as A and B, as above, we avoid the necessity of levelling up this vertical axis again by means of the long bubble-tube.

Besides the above adjustments, some instruments have a means of *Centring the Eye-piece* and also of *Adjusting the Object-Slide*. (See Note C, Appendix.)

45. Remarks.—Another way of performing adjustment \mathcal{C} is by means of an object and its reflection in still water, or even in a plate of syrup. A star at night does well for this, but it is advisable to select one as nearly east or west as possible, as its motion in azimuth is then a minimum.

If at any time adjustment C is not correct, we can obtain true results by "reversing," as in Fig. 5, and remembering that half-way between the two points so found is the correct point.

This latter remark applies also to adjustment D. It is a good plan to reverse on a back-sight every few sights, as it

takes practically no extra time and at once detects if anything is wrong. By taking a point half-way between two points, as D and B in Fig. 6, we can do good work with an instrument in which this adjustment is very far from correct.

As regards adjustment E:—If we had a level handy, it is much more convenient to level two points with it; or if there is a sheet of still water at hand, two pegs driven down to its surface do equally well. To ascertain the *Index-error* of the vertical circle in instruments where it cannot be corrected for instrumentally, set the vertical axis truly vertical, as explained under adjustment E, then level up the telescope and observe the readings on the vertical arc. If they are at zero, there is no index-error; but if not, the difference between the readings and zero is the index-error.

If the transit has a Striding-level attached, adjustment C may then be more accurately performed by means of it-whether the striding-level is in adjustment itself or not, for it is only the difference of the readings that is required. To make adjustment C then proceed thus: Level up by the small bubbletubes and point the telescope towards the north; take the readings of the bubble on the glass, both at its east and west end; then reverse the striding-level, end for end, and take the readings a second time: one quarter of the difference between the sum of the two east readings and the sum of the two west readings equals the number of divisions on the tube that the bubble must be moved by means of the pivot-screws in order to make the "horizontal axis" level, that end being too high the sum of whose readings is the greater. If the striding-level is in adjustment, we have only to screw up the "horizontal axis" so as to agree with it. We can, of course, adjust the striding-level by placing it on the pivots already levelled, and bringing the bubble to the centre of the tube.

Lighting the cross-hairs, when the instrument has no lantern attached, can be effected by fastening a piece of bright tin—or even white paper—over and partly in front of the object-glass, so as to east the reflection of a light on the ground into the tube of the telescope; but the reflector must not obstruct more than half of the field of the object-glass. A piece of tin or paper with a ½-inch hole in the centre of it, fastened at a suitable angle over the object-glass, answers very well.

In moving the diaphragm when the telescope has an invert-

ing eye-piece, it has to go in the opposite direction to what appears to be the right one.

If working with an instrument the graduation of which is faulty, read each angle in different parts of the circle. The graduations can always be tested by reading with both verniers on various parts of the circle. In observing an angle, if we take the mean result obtained by both verniers, we eliminate errors due to eccentricity of the vertical axis and the graduated circle, as well as reduce the errors of graduation.

When great accuracy is required in reading an angle the best method to use is Borda's Repetition, which slightly reduces the errors of observation, while it diminishes those of graduation in inverse order to the number of times the angle is repeated. The process is thus: Clamp the vernier-plate to zero, and read the angle by both verniers according to the usual method. Then, keeping the vernier-plate clamped, point the telescope again to the first object, and proceed as before through any number of repetitions. At the end of the final angle read the verniers, adding 360° for each complete revolution which has been made, and divide the total angular measurement by the number of times the angle was repeated. The quotient is the required angle. In this way, provided there is no play about the tangent-screws, an angle can be read with confidence to a few seconds by a very inferior instrument.

In ordinary work, if sure of the correct centring of the vertical axis and also of the graduation itself, there is no need to read by both verniers; but it is advisable to read always by the same vernier if only one is used.

An instrument correct according to the adjustments given above gives correct results when dealing with objects distant from it by the amount OC in Fig. 6, but if there is defective centring of the object-slide—not to be confounded with eccentricity of the optical axis of the object-glass—it will not give correct results in dealing with objects at distances from it greater or less than OC. This can always be tested by ranging points in a "straight" line for a thousand feet or so, beginning as near to the instrument as the focus will permit. Then, if, on ranging the same points in again from the other end, they do not coincide, one half the difference between the points is the error in alignment. In this way, even with a bad instrument, a straight line can be run. We can of course also run a straight

line with an instrument which has a defective object-slide, if in proper adjustment, by taking back-sights and fore-sights equal in length to OC, Fig. 6, so that then the object-slide will occupy the same position as it did when the line of collimation was adjusted.

If the object-slide works correctly, then, although the object-glass may be badly centred,—i.e., its optical axis will not coincide with the centre of the telescope-tube,—if the line of collimation is in correct adjustment for *one* distance it will give correct results at *all* distances.

Parallax is caused by the focus of the object-glass and that of the eye-piece not coinciding at the cross-hairs. To correct for it, shift the eye-piece in and out until the cross-hairs are seen distinctly. Then point the telescope to some distant object and move the object-glass in and out until the image of the object is seen sharp and clear, coinciding apparently with the cross-hairs.

STADIA.

46. Transits used on location should be fitted with adjustable stadia-hairs. These are usually adjusted to read 1 foot on a rod at a distance from the centre of the instrument equal to (100 feet + distance from object-glass in its mean position to the centre of the instrument + focal length of the object-glass), usually making a distance in all of about 101.25 feet. And since the stadia-hairs should be placed so as to be equidistant from the ordinary horizontal hair, at a distance of 101.25 feet the distance read between each pair of adjacent hairs should be 0.50 feet.

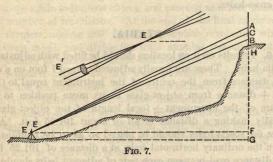
If the hairs are not adjustable, but are fastened to the ordinary diaphragm, then the measurements on the rod must be regulated to suit the hairs, remembering that the apex of the angle subtended by the distance read on the rod is not at the centre of the instrument, but at a point in front of the object-glass by a distance equal to the focal distance of the object glass, which is usually 1.25 feet in front of the centre of the instrument.

If the hairs are unadjustable, and we wish to use an ordinary levelling-rod to read on, then suppose at 101.25 feet we read 0.88 feet between the stadia-hairs, we must divide every reading in feet by 0.88 in order to obtain the distance in terms of

100 feet. Thus if at a certain point we read 4.40 on the rod, the distance will be 500 feet, or 501.25 feet from the centre of the instrument. To find the focal-length of the object-glass, focus it for a distant object; the distance from the cross-hairs to the object-glass then equals the focal-length.

On sloping ground, if the rodman is careful about holding the rod perpendicular to the line of sight, swaying it slowly to and fro so as to permit of the minimum reading being taken, then if the centre hair reads somewhere about 5 feet on the rod (i.e., the height of the instrument above the ground) we have only to multiply the distance as read on the incline by the cosine of the inclination, in order to obtain the true horizontal distance.

But if really correct work is wanted, it is best to have a bubble-tube attached to the rod so that it can be held vertically, and then correct for the inclination as follows:



In Fig. 7 the distance

$EF = AB \cos^2 FEC$.

EF being in terms of 100 feet, and FEC being the angle of inclination as measured to C, the ordinary horizontal hair of the instrument, assuming that the stadia-hairs are equidistant from C, and that 1 foot on the rod corresponds with 100 feet in distance.

In order to reduce this to the centre of the instrument, we should of course add to EF the amount $1.25 \times \cos FEC$, but for ordinary inclinations we may assume this correction to equal 1 foot. Thus, if $FEC=30^\circ$, and AB=6.00, then

E'F=1 ft. $+(6\times.75)=451$ feet. To obtain the height HG in Fig. 7, the best way is to make CH on the rod equal to the height of the point E above the ground, say 5 feet. Then

$HG = EF \tan FEC$.

Thus in the above example HG=260 feet. The following table gives the VALUES OF COS^2 FEC, where FEC is the inclination angle:

INCLINA- TION.	0′	10′	20′	30′	40'	50′
0°	1.0000	1.0000	1.0000	.9999	.9999	.9998
1	.9997	.9996	.9995	.9993	.9992	.9990
2	.9988	.9986	.9983	.9981	.9978	,9976
3	.9973	.9969	.9966	.9963	.9959	.995
4	.9951	.9947	9943	.9938	.9934	.9929
5	.9924	.9919	.9914	.9908	.9902	.989
6	.9891	.9885	.9878	.9872	.9865	.9858
7	.9851	.9844	.9837	.9830	.9822	.9814
8	.9806	.9798	.9790	.9782	.9773	.976
9	.9755	.9746	.9737	.9728	.9718	.9708
10	9698	.9688	.9678	.9668	.9657	.964
11°	.9636	.9625	.9614	.9603	,9591	.9580
12	.9568.	.9556	.9544	.9532	.9519	.950
13	.9494	.9481	.9468	.9455	.9442	.942
14	.9415	.9401	.9387	.9373	.9359	.934
15	.9330	.9315	.9301	.9286	.9271	.9250
16	.9240	.9225	.9209	.9193	.9177	.916
17	.9145	.9129	.9112	.9096	.9079	.906
18	.9045	.9028	.9011	.8993	.8976	.895
19	8940	.8922	.8904	.8886	.8867	.884
20	.8830	.8811	.8793	.8774	.8754	.873
21°	.8716	.8696	.8677	.8657	8637	.861
22	.8597	.8576	.8556	.8536	.8515	.849
23	.8473	.8452	.8431	.8410	.8389	.836
24	.8346	.8324	.8302	.8280	.8258	.823
25	.8214	.8192	.8169	.8147	.8124	.810
26	.8078	.8055	.8032	.8009	.7986	.796
27	.7939	.7915	.7892	.7868	.7844	.782
28	.7796	.7772	.7747	.7723	.7699	.767
29	.7650	.7625	.7600	.7575	.7550	.752
30	.7500	.7475	.7449	.7424	.7398	.737
312	.7347	.7322	.7296	.7270	.7244	.721
32	.7192	.7166	7139	.7113	.7087	.706
33	.7034	.7007	.6980	.6954	.6927	.690
34	.6873	.6846	.6819	.6792	.6765	.673
35	.6710	.6683	.6655	.6628	.6600	.657
36	.6545	.6517	.6490	.6462	.6434	.640
37	.6378	.6350	.6322	.6294	.6266	.623
38	.6210	.6181	.6153	.6125	.6096	.606
39 40	.6039	.6011	.5982	.5954	.5925	.589
40	.5868	.5839	.5811	.5782	.5753	.572

THE COMPASS.

47. The adjustments of the Compass are as follows:

A. To make the needle swing horizontally.—Level the compass, then by means of the slide-piece on the needle regulate its centre of gravity so that it will swing horizontally.

B. To straighten the needle.—See if both ends of the needle point to exactly opposite graduations while the compass is being turned completely around. If so, the needle is straight and the pivot is properly centred. But if not, the error will arise from either one or both of these not being correct. Turn the compass until some graduation, say 90°, comes precisely to the northern end of the needle. Mark the place where the southern end of the needle then points. Take off the needle and bend it until its southern end points half-way between 90° and the point already marked, while its northern end is kept at the opposite 90° by slightly moving the compass around. The needle will then be straight, although it will not intersect opposite degrees on account of the eccentricity of the pivot.

C. To centre the pivot.—Turn the compass around until a place is found where the opposite ends of the needle cut opposite degrees. Then turn the compass quarter-way around, or through 90°. If the needle then cuts opposite degrees, the pivot is in adjustment; but if not, bend the pivot until it does. The needle should then cut opposite degrees while being

turned completely around.

Remarks.—If the magnetism of the needle gets weak, it may be renewed as follows: Cover the needle with a thin film of oil, and then with the north pole—the end marked with a line across it—of an ordinary magnet rub the south end of the needle, beginning at the centre and working outwards towards the end; similarly rub the north end of the needle with the south pole of the magnet. After doing this a few times the magnetism should be sufficiently restored.

Reading both ends of the needle corrects for eccentricity of the pivot if the needle is straight; it also of course reduces the

errors of graduation.

Should the glass cover become electrified, as it will if but slightly rubbed, so that the needle sticks to the under side of it and will not "traverse" properly, touching the glass in

several places with the moistened finger, or breathing on it, will remove the electricity.

A compass when left standing for any considerable time should always have its needle free, in order to prevent loss of magnetic power. Of course when carried it should always be clamped.

In taking a compass-reading, not only must all iron and steel substances be kept well away, but metal magnifiers of all sorts are liable to cause a slight deflection, owing to the possibility of impurity in the material of which they are composed. Magnifiers coated with nickel are especially bad, since nickel itself is a decidedly magnetic metal.

Since the magnetic attraction varies in different places, adjustment A, if correct in one place, will probably want looking to if the instrument is taken anywhere else.

MAGNETIC VARIATION.

48. By referring to the Chart of Magnetic Variation, we see that in North America the variation is both towards the east and the west. The "line of no variation" which separates these two divisions is found to be constantly shifting westwards at an average rate of about 4' per annum. This causes a gradual increase in all variations to the west, and a corresponding decrease in all variations to the east; and changes similar to these are going on all over the globe. Besides this secular variation we have diurnal and annual variations, but for practical field purposes these latter may be ignored. The former of them is such that the needle attains its extreme westerly position at about 2 P.M. each day, and its extreme easterly position at about 8 A.M.; while the latter shows itself generally by a slight increase in variations west, and decrease in variations east, during the summer.

The chart here given is more as a matter of interest than for any real use in the field. If the variation at any place is wanted accurately, usually the only satisfactory way is to take it directly by observation, as shown in Sec. 57. For very rough work, however, an *idea* of the amount of variation can be obtained from the chart by interpolating by eye.

The "lines of no variation" are shown thicker than the others.

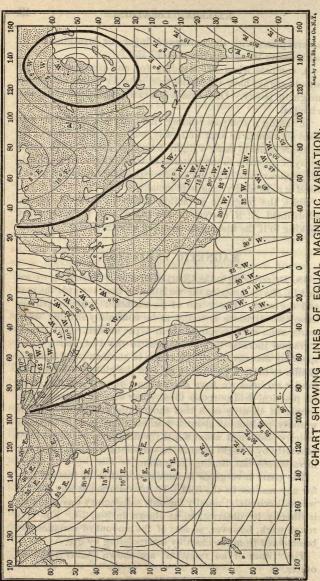


CHART SHOWING LINES OF EQUAL MAGNETIC VARIATION.

THE LEVEL.

49. We will first take the DUMPY LEVEL, which usually needs only two adjustments.

A. To make the bubble-tube perpendicular to the vertical axis.—This is done in just the same way as with one of the small bubble-tubes in adjustment A of the transit.

B. To make the line of collimation parallel to the bubble-tube.—This is done in a similar way to the adjustment of the long bubble-tube of a transit, already described, except that in this case it is the line of collimation that has to be made parallel to the bubble-tube, so that now it is the cross-hairs that have to be moved. In this case of course there is no necessity to set up the instrument "in about the same line as A and B" as there was in the case of the transit.

Another way of performing this adjustment is by the method of "reciprocal observations," as given for the Handlevel in Sec. 52.

The remarks which applied to the telescope of a transit apply with equal force to the telescope of a level; more especially the remark on the running of a straight line if the object-slide is badly centred. If the level has a means of adjusting the eye-piece and object-slide, see Note C, Appendix.

50: The Y Level has three adjustments as follows:

- A. To make the line of collimation coincide with the axis of the telescope.—Open the clips of the Y's. To adjust the vertical hair, mark the intersection of the cross-hairs on some fixed object, and revolve the telescope in its Y's so that the level will be upside down; and then if the intersection falls to one side of the object, one half the error must be corrected for by the capstan-headed screws. To adjust the horizontal hair, turn the telescope over as before, and if the intersection of the hairs strikes above or below the object, correct as before for one half the error.
- B. To make the bubble-tube parallel to the line of collimation.—This adjustment consists of two parts. First, bring the bubble to the centre and then revolve the telescope in its Y's through about 20°; if the bubble then runs to one end, half the error must be corrected for by the horizontal screws at the end of the tube, raising or lowering as may be required.

For the second part of this adjustment, place the telescope over a pair of opposite levelling-screws, open the clips, and bring the bubble to the centre of the tube. Reverse the telescope end for end in its Y's; if the bubble is not then in the centre, one half the error must be corrected for by the vertical screws at the end of the bubble-tube. On levelling-up and again reversing, this adjustment should be found to be correct.

C. To make the axis of the telescope perpendicular to the vertical axis.—Level up. Place the telescope over a pair of opposite levelling-screws. Swing the telescope half-way round on its vertical axis. If then the bubble has left the centre, bring it half-way back by means of the large capstan-headed nuts of the Y's. Then place the telescope over the other pair of levelling-screws, and if necessary proceed as before. This adjustment should then be correct.

Remarks.—As with the transit, if the object-slide of a level is defective the line of collimation when adjusted is only correct for back-sights and fore-sights of equal length with the distance of the object on which the line of collimation was adjusted.

In levelling, whenever possible, keep the fore-sights and back-sights of equal length: if so, accurate work can be done with an instrument thoroughly out of adjustment, for then the actual height of the instrument itself is of no importance. If, as in levelling uphill, it is necessary to take extremely short fore-sights, they should be counteracted by short back-sights—if not at the time, as soon afterwards as possible.

51. There is no need to allow for CURVATURE OF THE EARTH OR REFRACTION in sights under 700 feet, and then, if taking fore-sights and back-sights of about the same length, the corrections would counteract each other; so that it is only in taking an extremely long fore-sight or back-sight, which is not counteracted by a more or less equal sight in the opposite direction, that we need apply corrections for curvature or refraction.

For CURVATURE the correction in feet amounts to

$0.67L^{2}$,

where L = length of sight in miles, and is to be subtracted from the reading on the rod: this being simply the tangential

offset for a curve—see Sec. 78—with radius equal that of the earth.

For REFRACTION, on an average, it amounts in feet to

$0.1L^{2}$,

which is an experimental quantity, and is to be added to the reading on the rod. So that, taking the two together, we may say that the correction in feet amounts to

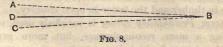
$0.57L^{2}$,

and is to be subtracted from the reading on the rod, the elevation as taken or given by the level being always too low. This is equivalent to about .0002 ft. at 100 feet; so that, since it increases as the square of the distance at say, 1200 feet, it will equal .0002 \times 12 2 = .03 foot. The following table gives the Joint corrections for curvature and refraction, worked out by the above formula, and is useful in ascertaining the elevation of the surrounding country:

Distance in Miles.	Correction in Ft.	Distance in Miles.	Correction in Ft
1	0.57	30	513
5	14.25	40	912
10	57.0	50	1,425
15 20 25	128 228	60	2,052
20	228	80	3,648
25	356	100	5,700

Thus from the table, if the level gives a point on a distant mountain, say 30 miles off, the elevation of that point will be equal to the elevation of the instrument + 513 feet.

52. The Hand-Level.—The only adjustment necessary as a rule with this instrument is to make the line of collimation parallel to the bubble-tube. To do this, sight from a point A to a point B, as in Fig. 8, and then back again from B to A.



If the level is in adjustment the two sights should coincide at A. But suppose C is the point struck instead of A; then D,

a point half-way between A and C, will be on a level with B: therefore the hair must be adjusted on the line BD. A handier way is of course to adjust it by means of another level, or a sheet of water.

THE SURVEY.

53. The object of the following notes is not to show the mode of conducting location,—which of course can only be picked up by actual experience in the field,—but merely to give solutions of the various mathematical and instrumental problems which arise in the course of the work.

In the case of Exploratory Surveys, the instruments used and the problems which arise being usually entirely different from those which come into question in ordinary location, they will be considered separately in Part III.

A Reconnoissance survey, as generally understood, may also be classed with the above, or it may take the form of a rough preliminary survey, a compass perhaps being substituted for the ordinary transit. As regards Compass-surveys, there is among engineers a strong prejudice against them, but in a country tolerably free from local attraction a compass-line is surely correct enough for preliminary work; for though by it accuracy cannot be obtained at any one point, its errors are not accumulative, but in a great measure counteract each other, so that the line as a whole should give very fair results. Another method of performing rough work is the Stadia process, by means of which very good results have often been obtained, the engineering staff consisting merely of an engineer and a rodman, the only instruments used being a rod and a small transit with bubble-tube and stadia attachment. Comparing compass and stadia work, the former is usually more suitable in timber and the latter in open country.

The term *Preliminary survey* is variously used, sometimes indicating a mere reconnoissance, but more generally a survey the object of which is to obtain accurate topography, in order by its means to select the final location. As regards the degree of accuracy to be employed in preliminary work, it of course depends in what way the results are to be

used; but it is generally best to run the transit-line of the "preliminary" with as much accuracy as is attainable under the circumstances. If this is done we then have a line on which we can at all points depend, and which we can use as a base for other lines, knowing, if we branch off from it at one point, the exact course we must make to strike it again at any given station. We will therefore suppose in the following notes that the final location is to be selected by the aid of an accurately run preliminary line, topography having been taken on either side of the transit line to a distance of from, say, 100 to 600 feet, according to the nature of the ground.

On Preliminary Surveys, by means of a hand-level and prismatic-compass, the engineer-in-charge, keeping ahead of the party, is generally able to ascertain approximately where the line will go, and then the transit-man has merely to follow more or less the route indicated, being guided by the consideration of running the line as much as possible to a constant rate of grade. If the line, however, is being run to the maximum grade-or any other rate of grade which it is the wish of the engineer to maintain-along a continuous transverse slope, such as a mountain-side, the transit-man can choose the line tolerably well for himself, since he only has to select his stations so as to maintain the required rate, which he can do by means of the vertical arc. But in selecting these points he has to bear in mind the probable amount of curvature which there will be between the station where the instrument is standing and the place at which the front picket is to be set, and allow for it in setting the picket. (See Sec. 26.) Thus, suppose he is running the line to a 1.5 p. c. grade, and that he estimates the distance to the picket to be about 500 feet, and the probable total curvature in that distance to be 15°, then the grade-angle, instead of being 51½', as in the following table, will be 481. If he has stadia-hairs in his instrument,—as he ought to have,—he can read off the distance with sufficient accuracy on the picket itself, and in this way form his estimates more closely. The difference in distance along the straight course and along the probable location must also be allowed for where the deviation is great. The following is a

TABLE OF GRADES AND GRADE-ANGLES.

Feet per Station.	Feet per Mile.	Inclina- tion.	Feet per Station.	Feet per Mile,	Inclina-	Feet per Station.	Feet per Mile.	Inclina-
		0 / //		1000	0 / //			0 / //
.01	.528	21	.51	26.928	17 32	1.01	53.328	31 43
.02	1.056	41	.52	27.456	17 53	1.02	53.856	35 04
.03	1.584 2.112	1 02 1 23	.58	27.984 28.512	18 13 18 34	1.03	54.384 54.912	35 24 35 45
.05	2,640	1 43	.55	29.040	18 54	1.05	55.440	36 05
.06	3.168	2 04	.56	29.568	19 15	1.06	55.968	36 26
.07	3.696	2 24	.57	30.096	19 36	1.07	56.496	36 47
.08	4.224 4.752	2 45 3 06	.58	30.624 31.152	19 56 20 17	1.08	57.024 57.552	37 08 37 28
.10	5.280	3 26	.60	31.680	20 38	1.10	58.080	87 49
.11	5,808	3 47	.61	32,208	20 58	1.11	58,608	38 09
.12	6.336	4 08	.62	32.736	21 19	1.12	59.136	38 30
.13	6.864	4 28	.63	33 264	. 21 39	1.13	59.664	38 51
.14	7.392 7.920	4 49 5 09	.64	33.792 34.320	22 00 22 21	1.14	60.192 60.720	39 11 39 32
116	8.448	5 30	.66	34.848	22 41	1.16	61.248	39 53
.17	8.976	5 51	.67	35.376	23 02	1.17	61.776	40 13
.18	9.504	6 11	.68	35.904	23 23 23 43	1.18	62.304 62.832	40 84 40 54
.19	10.032 10.560	6 32 6 53	.69	36.432 36.960	23 45 24 04	1.19 1.20	63.360	40 54
TER.	B. ZIELIZI LI	77 19	.71	37.488	24 24	1.21	63.888	41 35
.21	11.088 11.616	7.13	72	38.016	24 45	1.22	64.416	41 56
.23	12.144 12.672	7 54	.73	38.544	25 06	1 99	64.944	42 17
.24	12.672	8 15	.74	39.072	25 26	1.24	65.472	42 38 42 58
.25	13.200	8 36 8 56	.75 .76	39.600 40.128	25 47 26 08	1.25 1.26	66.000 66.528	43 19
27	13.728 14.256	9 17	.77	40.656	26 28	1.27	67.056	43 39
.28	14.784	9 38	.78	41 184	26 49	1.28	67.584	44 00
.29	15.312 15.840	9 58 10 19	.79	41.712 42.240	27 09 27 30	1.29	68.112 68.640	44 21 44 41
100	Total Control	et de puis	.81	42,768	27 51	1.31	69.168	45 02
.31	16.368 16.896	10 39 11 00	.82	43.296	28 11	1.32	69.696	45 23
.33	17.424	11 21	.83	43.824	28 32	1.33	70.224	45 43
.34	17.424 17.952	11 41	.84	44.352	28 53	1.34 1.35	70.752	46 04 46 24
.35	18.480 19.008	12 02 12 23	.85	44.880 45.408	29 13 29 34	1.35	71.280 71.808	46 45
.37	19.536	12 43	.87	45.936	29 54	1.37	72.336	47 06
.38	20.064	13 04	.88	46 464	30 15	1.38	72.864	47 26
.39	20.592 21.120	13 24 13 45	.89	46.992 47.520	30 36 30 57	1.39	73.392 73.920	47 47 48 08
	7 3 10 27	77.0	13.				74.448	48 28
.41	21.648 22.176	14 06 14 26	.91	48.048 48.576	31 17 31 38	1.41	74.976	48 49
.43	22.176 22.704	14 47	.93	49.104	31 58	1.43	75.504	49 09
.44	23,232 23,760	15 08	.94	49.632	32 19 32 39	1.44	76.032 76.560	49 30 49 51
.45	23,760 24,288	15 28 15 49	.95 .96	50.160 50.688	33 00	1.45	77.088	50 11
47	24.816	16 09	.97	51.216	33 21	1.47	77.616	50 32
.48	25.344	16 30	.98	51.744 52.272	33 41	1.48	78.144	50 52
.49	25.872 26.400	16 51 17 11	1.00	52.272 52.800	34 02 34 23	1.49	78.672 79.200	51 13 51 34
.00	20.400	11 11	1.00	0.000	04 20	1.00	10.200	01 01

TABLE OF GRADES AND GRADE-ANGLES .- Continued.

Feet per Station.	Feet per Mile.	Inclina- tion.	Feet per Station.	Feet per Mile.	Inclina- tion.	Feet per Station	Feet per Mile.	Inclina- tion.
111	PART AND A	0 1 11	Deli	Tarri Sub	0 / //	(d)	Dr. Ngut N	0 / 1/
1.51	79.728	51 54	1.91	100.848	1 05 39	3.55	187.440	2 01 59
1.52	80.256	52 15	1.92	101.376	1 06 00	3.60	190.080	2 03 42
1.53 1.54	80.784 81.312	52 36 52 56	1.93	101.904 102.432	1 06 20	3.70	192.720 195.360	2 05 25 2 07 08
1.55	81.840	53 17	1.95	102.452	1 07 02	3.75	198.000	2 08 51
1.56	82.368	53 37	1.96	103.488	1 07 22	3,80	200.640	2 10 34
1.57	82.896	53 58	1.97	104,016	1 07 43	3.85	203.280	2 12 17
1.58	83.424	54 19	1.98	104.544	1 08 04	3.90	205.920	2 14 00
1.59	83.952	54 39	1.99	105.072	1 08 24	3.95	208.560	2 15 43
1.60	84.480	55 00	2.00	105.600	1 08 45	4.00	211.200	2 17 26
1.61	85,008	55 21	2.05	108.240	1 10 28	4.10	216.480	2 20 52
1.62	85.536	55 41	2.10	110.880	1 12 11	4.20	221.760	2 24 18
1.63	86 064	56 02	2.15	113.520	1 13 54	4.30	227.040	2 27 44
1.64	86.592	56 22	2.20	116.160	1 15 37	4.40	232.320	2 31 10
1.65	87.120	56 43	2.25	118.800	1 17 20	4.50	237.600	2 34 36
1.66	87.648 88.176	57 04 57 24	2.30	121.440 124.080	1 19 03	4.60	242.880 248.160	2 38 01 2 41 27
1.68	88.704	57 45	2.40	126.720	1 22 29	4.80	253.440	2 44 53
1.69	89.232	58 06	2.45	129.360	1 24 12	4.90	258.720	2 48 19
1.70	89.760	58 26	2.50	132.000	1 25 56	5.00	264.000	2 51 45
1.71	90,288	58 47	2.55	134.640	1 27 39	5.10	269,280	2 55 10
1.72	90.816	59 07	2.60	137.280	1 29 22	5.20	274.560	2 58 36
1.73	91,344	59 28	2.65	139.920	1 31 05	5.30	279.840	3 05 09
1.74	91.872	59 49	2.70	142.560	1 32 48	5.40	285.120	3 05 27
1.75	92.400 92.928	1 00 09	2.75 2.80	145.200 147.840	1 34 31 1 36 14	5.50	290.400 295.680	3 08 53 3 12 19
.77	93.456	1 00 50	2.85	150.480	1 37 57	5.70	300.960	3 15 44
78	93.984	1 01 11	2.90	153.120	1 39 40	5.80	306.240	3 19 10
1.79	94.512	1 01 32	2.95	155.760	1 41 23	5.90	311.520	3 22 36
1 80	95.040	1 01 52	3.00	158.400	1 43 06	6.00	316,800	3 26 01
1.81	95.568	1 02 13	3.05	161.040	1 44 49	6.10	322.080	3 29 27
1.82	96.096	1 02 34	3.10	163.680	1 46 32	6.20	327.360	3 32 52
1.83 1.84	96.624	1 02 54	3.15	166.320	1 48 15 1 49 58	6.30	332.640	3 36 18
1.85	97.152 97.680	1 03 15 1 03 35	3.25	168.960 171.600	1 49 58	6.40	337.920 343.200	3 39 43 3 43 08
1.86	98.208	1 03 56	3.30	174 240	1 53 24	3.60	348.480	3 46 34
1 87	98.736	1 04 17	3.35	176.880	1 55 07	6.70	353.760	3 49 59
1.88	99.264	1 04 37	3.40	179.520	1 56 50	6 80	359.040	3 53 24
1.89	99.792	1 04 58	3.45	182.160	1 58 33	6.90	364.320	3 56 50
1.90	100.320	1 05 19	3.50	184.800	2 00 16	7.00	369.600	4 00 15

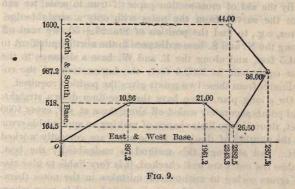
When the running is tolerably easy, instead of taking a series of short courses, it is often better to insert a curve at once, selecting one which is likely—as near as can be guessed—to coincide with the probable final location; for in this way truer results can be arrived at than by a series of independent courses.

54. As regards the Instrument-work itself, the method of reading angles as so much "to the right" or "to the left" is

decidedly feeble. The best way is to start with the verniers reading zero when the telescope is pointing towards the magnetic, or still better, the true north; then the first angle read is the magnetic (or true) bearing of the first course. On moving the instrument up to the front picket, the horizontal circle should be kept clamped, and the reading of the vernier again, when the instrument is next set up, constitutes a check on the former reading; for though there will probably have been some slipping of the plates, owing to the shaking while being carried from one station to the other, an error of a degree or so is easily detected. When the telescope is pointed to the backsight the verniers should then read the same as they did at the other end of the line, and thus for the next course, on turning through the required angle, it will be its bearing-magnetic or true as the case may be-that is read. The compass-reading should also be taken for each course, at each end of the course, which thus forms an additional check on the work, and also detects local attraction. For if, when the instrument is set up, the needle does not on any course read the bearing corresponding with the vernier reading (if the zero corresponds with the magnetic north) or does not give the difference in the readings equal to the "variation," if the zero corresponds with the true north, if the work is correct, the cause is either the change in variation, or local attraction, or both these causes combined. If the instrument is a good one there is no need to read by more than one vernier. (See Sec. 45.) But it should usually be the same vernier that is read, and that vernier will then always be on the same side of the transit-line. If, however, the line of collimation, from some cause or other, such as a defective object-slide which cannot be remedied in the field, is unreliable, the error can be counteracted to a large extent by taking the bearings with the same vernier on opposite sides of the line at alternate stations.

55. With the bearings taken as above, or in fact taken in any way, the most satisfactory method of plotting the work is by means of LATITUDES AND DEPARTURES. This method involves a little extra work, but its advantages over the ordinary protractor method—or even the method of "chords" or "natural tangents"—are so great as to make the few minutes extra time taken in preparing the notes time well spent. The main advantage of this method is that an error

made in plotting one station is not transmitted to the next, as in the ordinary methods, for each station is plotted entirely independent of the previous one; and thus of course we can plot any one part of the location on the plan in its right position, without having to work through from the beginning. Again, if we know the position of the point we are making for, we can, without keeping a continuous plot of the work, tell at any station how much we are off our direct route, and what course we ought to steer to strike the point we are making for. The method of keeping and plotting the notes is best shown as follows:



Suppose Fig. 9 represents the first five courses of a preliminary line, the notes for these courses will then be kept thus:

Sta.	Dist.	Read.	Bearing.	Lat.	Dep.	Total Lat.	Total Dep.
0 10.30 21.00 26.50 36.00 44.00	550 950 800	60° 90° 130° 30° -40°	N. 60° E. E. S. 50° E. N. 30° E. N. 40° W.	518 0 -353.5 822.7 612.8	897.2 1064. 421.3 475. -514.2	518. 518. 164.5 987.2 1600.	897.2 1961.2 2382.5 2857.5 2343.3

Readings which give a westerly course should be considered negative; so also should latitudes *south* and departures *west*, as shown above. Then

Latitude for any Sta. = Distance × Cosine of Bearing,

Departure " = " × Sine " "

and

Total Latitude for any Sta. =

Total Latitude for preceding Sta. + Lat. for preceding Sta.

Total Departure for any Sta. =

Total Departure for preceding Sta. + Dep. for preceding Sta.

The term "Latitude" is an abbreviation of "Difference of

Latitude." The terms "Cosines" and "Sines" are more appropriate when the bearings are kept with no particular reference to the true or magnetic meridian.

By the aid of cross-section paper (if true to scale) we can plot the survey from the notes with only a straight-edge. Thus, e.g., to find the position of Sta. 26 + 50, we read off along the N. and S. base a distance to the north equivalent to 164.5 feet, and along the E. and W. base a distance to the east equivalent to 2382.5 feet; the intersection of the coordinates from these two points gives the position required.

On a long plan, if we have the base-lines drawn straight, and points accurately scaled off along them at, say, every 1000 feet, there is very little chance of making an appreciable error in the plotting of the plan if the notes are correctly worked out. But although this method is undoubtedly the best, unless the notes are well checked, it is very liable to give rise to errors owing to arithmetical mistakes in the notes themselves. But where good work is wanted, and in cases where probably the method of plotting by "chords" or "natural tangents" would otherwise have been used, the method of Latitudes and Departures, well checked, gives far better results, and probably takes no longer than the other ways.

56. The only way in which to feel sure that there are no appreciable mistakes in the transit-work is to check the bearing of the alignment every now and again by an observation for azimuth. This should be done, if possible, before starting the survey, or in any case as soon after as possible, and the notes then already taken reduced to their true bearings. By taking the magnetic pole as the standard of our bearings, we have no means of applying an accurate check to the work at a later period; but if we start with the vernier at zero, when the telescope is pointing to the true north, we can then check our course at any time on the survey.

Engineers generally fight rather shy of anything in connection with astronomical work; but considering that it is almost as easy to check the alignment by means of a star as by any known point on the Earth's surface,—and usually much more accurate,—it is a great pity that observations for azimuth are not used more frequently than they are. It is so much more satisfactory for the transit-man himself to know if he is doing good work; and considering that the transit-line is usually taken as the basis of all the plans to be afterwards constructed, every possible means of checking the work should be used.

57. The handiest methods of obtaining the true north are the following, one of which is applicable in most northern latitudes about every 6 hours, and can be applied without any

knowledge at all of astronomical work:

A. By a Maximum Elongation.—In Fig. 10 let

Z represent the zenith,

P " the pole,

S "the Pole-star (Polaris). Then the small circle round the pole shows the path and direction of the star's motion, the time taken in making the circuit being nearly 24 hours. Now the radius of this small circle in angular measure is only about equal to 14° (or 2½ diameters of the sun), so that the apparent motion of the pole-star in azimuth (i.e., horizontally) will, when due east or west, be nothing at all, and for several minutes together when about east or west the

Fig. 10 let

motion will be inappreciable to ordinary railroad transits. Thus if we know about what time the star will be at its east or west elongation,—i.e., due east or due west,—and also the amount in azimuth by which when at those points it will be distant from the pole, we can, by setting the telescope on the star when at either of its elongations and applying the required correction in azimuth, obtain the direction of the true north. The following table shows approximately the times at which the elongations will occur. The amount of the correction in azimuth, which really equals the angle WZP (or EZP), may be found by solving the spherical right-angled triangle WPZ, the angle at W being 90°, the side ZP being equal to 90°—the

W

"declination" of the star. For Declinations of Stars see Table in Sec. 213. Thus we have

Sin azimuth = cos (dec.) sec (lat.),

PZ being the complement of the latitude of the place of observation. Thus suppose in latitude 50° N., in January 1889, we have the telescope clamped on Polaris at its eastern elongation, the vernier reading $2^{\circ}.05'$; then the sine of the azimuth correction = .0349, which gives a value for the correction of $2^{\circ}.00$, so that the telescope will be pointing due north when the vernier is set to read $0^{\circ}.05'$. (See note D, Appendix.)

TIMES OF ELONGATIONS OF POLARIS.

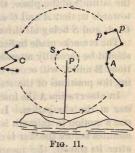
Month.	1st	Day.	11th	Day.	21st Day.		
Month.	Eastern.	Western.	Eastern.	Western.	Eastern.	Western.	
The Party	h m.	h. m.	h. m.	h. m.	h. m.	h. m.	
Jan	0.39 P.M.			11.47 P.M.	11.20 A.M.	11.08 P.M	
Feb	10.36 A.M.		9.57 "	9.45 "	9.18 "	9.06 "	
Mar	8.46 "	8.34 "	8.07 "	7.55 "	7.27 "	7.16 "	
April	6.44 "	6.32 "	6 05 "	5.53 "	5.26 "	5.14 "	
May	4.46 "	4.34 "	4.07 "	3.55 "	3.28 "	3.16 "	
June	2.45 "	2.33 "	2.05 "	1.54 "	1.26 "	1.14 "	
July	0.47 "	0.35 "	0.04 "	11.56 A.M.	11.25 P.M.	11.17 A.M	
Aug	10.42 P.M.	10.34 A.M.	10.03 P.M.	9.55 "	9.23 "	9 15 "	
Sep	8.40 "	8.32 "	8.01 "	7.53 "	7.21 "	7.13 "	
Oct	6.42 "	6.34 "	6.03 "	5.55 "	5.24 "	5.16 "	
Nov		4.33 "	4.01 "	3.53 "	3.22 "	3.14 "	
Dec	2.42 "	2.34 "	2.03 "	1.55 "	1.24 "	1.16 "	

Although the hour-angles from which the above times are calculated vary year by year and in different latitudes, they may be considered to be sufficiently correct between the years 1890 and 1900, and between latitudes 25° and 65° N. Where extreme accuracy is wanted, the time of observation may be calculated as in note D, Appendix. The above times increase by about 4 minutes every 10 years. But as these elongations occur only at intervals of 12 hours, more or less, it is well to have some other means of obtaining the true north, which can be used when the above method is inapplicable. The two following are similar to one another in principle, but occur about 12 hours apart, and from 5 to 7 hours from the time of the elongations given above.

B. In Fig. 11 let P be the pole and S the Pole-star, and let A

represent Alioth (ϵ Ursæ Majoris), and C represent the star "Gamma" (γ) Cassiopeia. The arrows and dotted lines show

the paths and the directions of the motion of the three stars. The positions of the stars in the figure are those which they would occupy about the time of the western elongation of Polaris; but since the complete circuit occupies about 24 hours, we see that in about 6 hours C will be about vertically under C. When this occurs (i.e., when C and C are in the same vertical plane), clamp the tele-



scope on Polaris, and wait through an interval of time which is to be found from the interval of 29 minutes 30 seconds for Jan. 1, 1889, by applying for any later date an annual correction of + 19 seconds. After the lapse of this interval Polaris will be due north.

C. The third method consists in making use of Alioth in a similar manner to that in which we have just made use of γ Cassiopeia. But in this case, when Alioth is vertically below Polaris, Polaris will be nearly at its upper "culmination" (or "transit," as its passage across the meridian is called), but this makes no difference in the mode of procedure. The interval to wait when using Alioth was, on Jan. 1, 1889, about 27 minutes, and increases annually by 17 seconds. To calculate the above intervals, see note E, Appendix; but for ordinary work the figures given above are sufficiently correct as far north as 70°, and as far south as A or Care visible at their lower culminations. The altitude at which C or A will be above the horizon when due north equals about

Latitude of the place - 30°;

so that observations B and D cannot practically be used farther south than latitude 35° N. If, however, the instrument has a reflecting eye-piece, if either observation B or C is needed farther south than these limits, A and C can be used at their upper culminations, which will take place near the zenith, the intervals of time and modes of procedure will be the same as for the lower culminations.

To obtain the azimuth of Polaris at any time see Sec. 202.

There can be no difficulty about finding these stars if it is remembered that the altitude of the pole-star is about equal to the latitude of the place; that the "pointers" pp, Fig. 11, point towards it; that A and C are each about 30° from the pole-star; C, A, and C being all three more or less in a straight line.

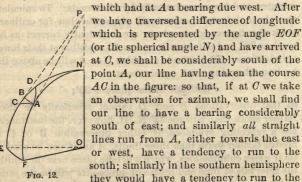
The remarks made in Sec. 45 regarding the vertical axis, etc., should be carefully attended to. The times at which observations $\bf B$ and $\bf C$ will occur can be found near enough by notic-

ing the positions of the stars themselves.

In observation A the instrument should be "reversed" on the star at the elongation. In observations B and C, where the star's motion in azimuth is comparatively rapid, observe, say, 2 minutes before the star is due north, and then again 2 minutes after its transit: the mean result should then be taken. An error of about 2 minutes in time in observations B and C causes an error in azimuth of about 1'. The verticality of the two stars should be also tested by a reversal of the instrument.

58. In checking the line by an azimuth observation as already described, it must be borne in mind that the convergence of the meridians needs a very important correction in the bearings relating to other points east or west of the place where the observation is taken. This may be best shown by means of Fig. 12.

Let ONEF represent a sector of the northern hemisphere, and let A be the point on the earth's surface at which the survey was started, a continuous "straight" line being run



north. Thus in order to run a line from A to a point B, keep-

ing in the same latitude the whole way, it becomes necessary to run it as a curve. (See Sec. 209.)

Now the amount of this increase in bearing from the north is equal to the convergence of the meridians between the two places, so that in the case of A and B the difference in the bearings of the same straight line obtained by observation at each place will be represented by the angle BPA, which for ordinary work we may consider equal to the difference of longitude of the two places multiplied by the sine of their mean latitude. (See note F, Appendix.) Thus if in latitude 40° north we start a straight line from A due west and run it to C through 1° of longitude, the bearing obtained by observation at C should be S. 89°, 21' W. But since it often needs some calculation to ascertain the difference of longitude, we can best proceed in ordinary work by finding from the following table the correction to be applied. Thus if in latitude 50° N. we have run a line which gives a total amount of easting or westing (i.e., Total Departure) equal to 60 miles, the amount of the correction to apply will be

 $60 \times 1' \ 02'' = 1^{\circ} \ 02'.$

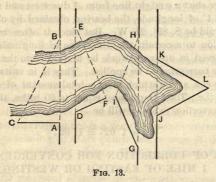
TABLE OF CORRECTION FOR CONVERGENCE FOR 1 MILE OF EASTING OR WESTING.

Lat.	Correction for 1 mile.	Lat.	Correction for 1 mile.	Lat.	Correction for 1 mile.
10°	9".18	270	26".52	44°	50".19
110	10".13	280	27".66	450	52".00
120	11".07	29°	28".85	46°	53".83
13°	12".02	300	30".03	470	55",67
14°	12".98	310	31".26	48°	57".67
15°	13".96	350	32",49	490	59".83
16°	14".93	830	33".83	50°	1' 02".00
170	15".92	34°	35".17	51°	1' 04",17
18°	16".91	35°	36" 50	52°	1' 06" 67
190	17".93	36°	37".83	53°	1' 09",17
20°	18".94	370	39",17	540	1' 11" 67
21°	19".98	38°	40".67	55°	1' 14" .33
220	21".02	39°	42".17	56°	1' 17".17
23°	22".10	40°	43".67	570	1' 20" .00
240	23".1"	410	45".17	580	1' 23".00
25°	24".30	420	46".85	590	1' 26" .25
26°	25".38	430	48".52	60°	1' 30''.00

This shows the necessity, when running a long continuous survey, of referring all bearings to an Initial Meridian, either

at the point from which the survey started, or at a point near its centre. The same remarks of course apply to magnetic courses to a certain extent, but in this latter case, on account of the constantly changing variation, such corrections are hardly practical.

59. When the transit-line crosses a river or ravine or some other obstruction over which it is difficult to obtain direct measurement, the best way to proceed is by *Triangulating*, using whichever of the methods shown in Fig. 13 is most applicable to the case.



The angles at A and F each $=90^{\circ}$, and at J, K, and $L=60^{\circ}$; then

AB = AC an C, $DE = DF ext{ sec } D$, $GH = IG ext{ sin } I ext{ cosec } H$, JK = JL = KL,

where $H = 180^{\circ} - (I + G)$.

If the ground on which we measure our base has a tolerably uniform slope in the direction of the base, it is better to take direct measurement along the surface of the ground and multiply the distance so obtained by the cosine of the inclination to obtain the horizontal distance, than to "break-chain." Whatever difference in elevation there may be between two such points as A and B, if the base measurement is reduced to the horizontal, the distance as calculated for AB, from the angles observed with a transit, will also be the horizontal dis-

tance. If the angles were observed with a sextant, of course this would not be the case. (See Sec. 144.)

If, instead of encountering such obstructions as those given above, an obstacle which we are unable to see across presents itself, such as a huge detached rock on which we cannot set up the instrument, then perhaps as good a way as any to get round it is by offsetting the line so as to run past it on a parallel one, and then on the far side, by equal offsets, getting back on to the former line. If the obstacle, however, is too large to pass it well by this means, we can apply the equilateral triangle JKL (Fig. 13). This latter method is a good one to use whenever practicable: there is no calculation necessary in connection with it, the angles used are those most favorable to exact work, and where the obstacle can be seen over, a check can be applied by observing the angle at K.

After having run the line a certain distance ahead, represented by the amount L, it is often necessary to "back-up" and start the line again from the instrument so as to strike a point a certain distance d on one side of the point where the first line struck; the correction C for this may be found thus:

$$\tan C = \frac{d}{L}.$$

For more on the subject of triangulation, etc., see Part III.

60. The LEVELLER'S WORK on preliminary location consists mainly in taking the elevation at every full station, and at any intermediate points where he may consider it advisable to do so. The best form of keeping notes on such work is the following:

Sta.	B.S.	Int.	F.S.	н.і.	Elevation.
B.M. 195	4.25	4.8	i knije i k	106,60	102.35
+50 196	3.28	7.3	5.61	duxislan	99.3 100.99

in which

or " in any line
$$=$$
 H.I. $-$ F.S. $=$ in same line,

and

H.I. in any line = Elev. + B.S. in preceding line.

The "Intermediate" column is sometimes omitted, but the insertion of it makes it easier to check each page by means of the difference of the sum of the Back-sights and Fore-sights.

To apply this check between two stations, A and B for instance, which have been used as turning-points, add together all the back-sights between A and B (including the B.S. at A, but excluding it at B); then add together all the foresights (excluding the F.S. at A, but including it at B): the difference of these two sums should equal the difference in elevation of A and B. If the sum of the back-sights is greater than the sum of the fore-sights, B is higher than A; but if less, then lower.

The levels should be worked out in the field whenever time permits, for reference on the work. The profile for each day's work should be made out when possible in the evening of the day on which the work was done.

As regards the precision of a line of levels run as above, the probable error is usually assumed to vary as the square root of the distance. The limit on the British Ordnance Survey is 0.01 foot per mile; the U. S. Coast Survey requires a limit of 0.03 per mile. If we assume a limit of 0.05 per mile for rough work, the probable error for any distance equals

0.05 Vmile.

Thus in 100 miles the probable error = 0.50 ft. For more on the subject of levelling see Parts II and III.

61. The TOPOGRAPHER'S WORK consists principally in taking the ground slopes, with more or less accuracy, at every full station and at any intermediate points where he may consider it necessary, by means of which a contour plan may be constructed.

To do this he obtains from the leveller the elevation of each station and *plus* station at which he has taken levels.

There is a variety of methods in use of obtaining the slopes, and the advantage of each depends on the accuracy required, the nature of the country, and the vertical distance apart of the contour-lines.

Where the slopes are steep and accurate work is wanted, a 10-foot slope-rod with clinometer gives very good results, but is a cumbersome sort of instrument to carry about.

Where 5-foot contours are wanted, a hand-level is very con-

venient, since by considering the height of the eye above the ground to be 5 feet, the point corresponding to each contourline is located at once by the level,—5 feet being an easy height to which to accommodate one's self,—and by pacing the distance between these points we have thus simply to enter the distances in the notes through which each contour passes. By taking the alternate points selected in this way, this method is of course equally applicable to 10-foot contours. Fig. 14 shows how this method is worked.

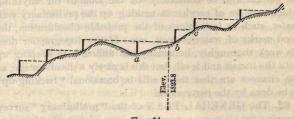


Fig. 14.

Suppose, e.g., that for a certain station the topographer obtains from the leveller the elevation of 1823.8, and that he is taking 5-foot contours. Then, if the ground is as shown in Fig. 14, he proceeds as follows: The contour-line nearest to this elevation is that of 1825 feet, the plane of which passes about 1 ft. above the ground-level at the station, so that by standing at the point a he can estimate with his eye the amount of 1.2 feet, and thus find the point b which corresponds with the contour of 1825. Similarly, standing at b he finds c, and so on up the slope as far as he considers necessary. Then returning to a, he works in the same way on the lower side. the distances are wanted accurately, he should have a man with a tape to assist; but as a rule, pacing, where it is practicable, gives good enough results. The only notes to be kept in this case are the distances out (right or left) to the respective contours

An Abney hand-level (with vertical arc) is also frequently used, and gives good results. All methods, however, which involve taking the angles of the slopes themselves necessitate extra work. One method of reducing this amount of labor is to have a set of scales for the various slopes, each made proportional to the cotangent of the inclination; but by the use

of cross-section paper and a small protractor we can probably do the work equally well and equally fast.

The *stadia* method is often found very convenient for obtaining topography where the above methods would fail to give good results.

But besides taking the contours, the topographer must also take note of the courses of streams, etc., on each side of the line within a distance (usually) of a few hundred feet. The bearings of these he can take with a small prismatic-compass. He should also be constantly on the lookout for anything which may be of service in making up the preliminary estimates, such as indications of the probable classification, the flood-marks of water-courses, etc. If the topographer does his work thoroughly, he usually has difficulty in keeping up with the transit and level; but this is rarely a disadvantage, as the chances are that there will be occasional "backing-up" to be done by the party ahead.

62. The GENERAL PLAN of the "preliminary" survey showing the alignment, topography, etc., is usually plotted to a scale of 400 feet to an inch, as in Figs. 15 and 16, thus agreeing with the horizontal scale of the profile.

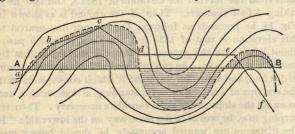


Fig. 15.

In Fig. 15 let abcdef represent a portion of the preliminary line as shown on the general plan, plotted to a scale of 400 feet to the inch; and let the line have been run to a + 1.25 p. c. grade, and the contours be given for every 5 feet vertical. Then if each station at which the instrument was set up was at "grade," the grade-contour will pass through each of these points, but gradually rising from one contour to another, crossing them successively at distances of about 400 feet apart; so that if, as in Fig. 15, station a happens to fall on a contour-line,

the grade-contour will cut the next line above, 400 feet farther on, at e; and since the next station d is only 200 feet from e, it will be situated about half-way between two of the contours.

Now this grade-contour is the line which, if adopted for the final location, would give no cuts or fills at all, so that it is the line which would render the cost of construction a minimum. The judgment of the engineer here comes in to decide how much it is advisable to deviate from this limit. So far the work has been more or less mechanical, for there are usually enough governing-points along the route to decide within two or three hundred feet the course of the preliminary line; but fitting the final location on to the plan is quite another matter. Suppose that the engineer considers that the straight line AB (Fig. 15) is about where the final line should be located. Then the shaded portions in the figure show cuts and fills alternatelyshaded vertically being "cut," and horizontally "fill;" and the points where the line AB intersects the grade-contour will of course be the "grade-points." The amount of centre-cut and centre-fill can be read off at any point-not by scaling, but by counting the number of contour spaces there are between the line AB and the grade-contour. Thus, e.g., at a point in AB opposite c, there are $2\frac{1}{2}$ contour spaces, equivalent to 12½ feet vertical, so that at this point we should have a 12½ft. centre-cut. By taking in this way a few points here and there, the engineer can, by means of Table XIV, form a fair idea of the number of cubic yards in each proposed cut or fill, making allowance of course where the surface-slope is steep, as shown in Sec. 69.

In this way, then, there is no great difficulty in obtaining a line which will make the cuts balance the fills, this being simply a matter of a few trials. Where curvature, however, is involved, it is not so much the question of balance as of the total amount of cut and fill, which needs consideration.

By having the various curves drawn on a horn protractor, or on a piece of tracing cloth, the result of adopting any certain curve can be seen at once by sliding it up and down over the plan.

Then, again, a change of grade for a short distance may appear advisable, which necessitates altering the grade-contour. The question of overhaul, too, has to be considered, and the avoidance as much as possible of long shallow cuts. The

probable classification, too, will of course affect the balance of cuts and fills. The advisability of raising the grade to avoid an expensive rock-cut also needs consideration. A little experience, however, goes a long way, and the engineer usually finds that there is little doubt to a few feet as to where the line ought to go.

63. The main features of the final location having been determined as above, and drawn on the plan, the approximate position of the points of curvature, etc., can be taken off by scale, and the line thus located on the ground; any little alterations being made, the advantages of which have become apparent when the line is seen actually staked out.

A fresh set of levels must of course be taken over the new alignment, and a profile constructed showing the rates of grade, etc., finally adopted.

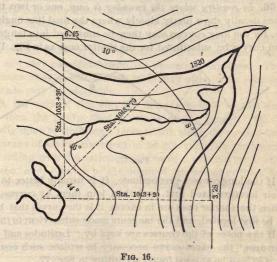
As regards compensating for curvature where transition curves are not used, the rate of grade should be changed at the P.C. and P.T. Many engineers, however, prefer making the change at the nearest "full" station; it makes little difference, however, which way is adopted.

Bench-marks should be given at distances of a third of a mile apart or so, and guard-stakes set solidly beside the hubs. If the location is being "rushed," there is no need to fill in the transition curves, for that can be done equally well by the section-engineer when he takes over the work for construction. When these curves are omitted, however, it should be so shown on the plan, as in Fig. 16.

64. It often happens that after the line is located a considerable distance ahead an alteration in the alignment is deemed advisable, necessitating a shortening or lengthening of a certain portion of the line. This causes a break in the "throughchainage." Such a break as this should, wherever possible, be referred to a point where there is a change of grade, or at least to a point on a tangent, so as to simplify the running of the grades and curves as much as possible. It should be indicated conspicuously in the notes and on the plans and profiles in the form of an equation; the station on the line which comes first being read first. Thus if the left-hand side of the equation is the greater, it means that the line has been lengthened; but if the right-hand side be the greater, it has

been shortened by an amount equal to the difference of the two sides.

suitable only to rolling or mountainous country; but where there is any doubt as to whether or not it is better to take contours, the engineer may generally come to the conclusion that it is better to do so. There is among some engineers an idea that the time spent in taking the topography might have been



better used in running a series of trial lines. Of course in many cases this is true; but it must be remembered that a preliminary line with topography well taken to a distance on either side of, say, 500 feet (as is perfectly feasible in ordinary rolling country) covers a width of 1000 feet so completely, as to render the running of a trial-line within that area entirely needless; and that in order to settle the question absolutely as to the location through, say, a valley half a mile wide, two or at the most three lines run as above are all that can ever be required; while by the method of trial lines how many are needed before the engineer can feel satisfied that he has finally obtained as good a line as can be got? And then it is only the best of the trial-lines that is usually selected, which in all probability will be inferior to the line selected from the contour plan.

Besides this, if topography is taken, the engineer can at any future time show evidence as to the advisability of having adopted the route which he finally selected. It is a duty he owes to himself as well as to the Railway Company to be able to prove that the location has been good, and how is he to do this if he has simply trusted to the correctness of his eye?

66. In country where the running is easy, one or two triallines usually show pretty closely where the final line ought to go, for the long courses may then be converted into tangents, and curves be substituted for the shorter ones as in Fig. 17.

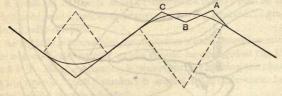


Fig. 17.

If the long courses predominate, it is usually better to get their location fixed first, and then join them by curves; but when the shorter ones are in excess, it is the curves that have to be first located, and the tangents made subservient to them.

If the notes of the courses are kept by "Latitudes and Departures," the exact curve necessary to replace such courses as ABC can be at once found according to Sec. 77.

67. An engineer with a good "eye" can often tell by merely looking over the ground what degree of curve is wanted to fit the surface, i.e., where the difference between a 3° 30′ and a 3° 45′ makes very little difference. Table II, of Tangents and Externals, is a good guide to this in many cases. For instance, by getting into position near the apex of the required curve, the engineer, with the aid of a hand-level and a prismatic compass, can often tell about how far from where he is standing the curve should pass. Thus, suppose he finds the angle of intersection to be about 40°, and that the curve should pass about 120 feet from the apex: he then finds from the Table that for an intersection-angle of 40° a 1° curve gives an external distance of 368 feet, therefore the

degree of curve which he wants will be found by dividing this by 120; thus a 3° 04′ curve will probably suit the case.

Where the APEX of a curve can be located without much trouble it is always better to do so; and of course this applies more especially to places where extreme accuracy in the centreline is of importance; such as where bridge-work or trestling are required in the neighborhood of the curve.

68. The balancing of cuts and fills in comparatively level country is usually unadvisable, partly on account of the extra expense involved by the matter of over-haul, but mainly because, though the dump should be kept as high as possible, cuts in such country, and especially long shallow ones, generally add very considerably to the operating expenses. Thus the amount of borrow in such cases may often with economy be made very considerable.

69. On work of this sort the line is generally located first, and then the grades fixed by means of the profile. This is usually done by straining a piece of silk along the surface-line, by means of which the effect of adopting certain grades corresponding with the various positions of the thread can at once be seen; and, judging by the depth of centre-cut or fill, a fair estimate can thus be made of the amount of excavation and embankment required.

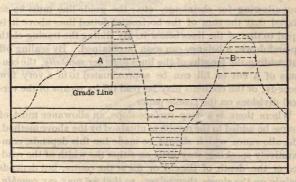


Fig. 18.

Where the work, however, is comparatively heavy, the following method will be found to give considerably better results: Suppose the dotted surface-line in Fig. 18 to be part of a pro-

file on which we want to fix the grades so as to make the cuts and fills balance, and that in this case we wish to make a portion of cut A together with the whole of cut B sufficient to fill the hollow C. On a piece of tracing cloth, say 10 inches long, draw a straight heavy line which is to be the grade-line; then turn to Table XIV, and see what depth of cut is required to give 1000 cubic yards contents in a length of 100 feet. Thus if the cuts are to have a 20-foot base and slopes of 11 to 1, as in Fig. 18, the depth of cut required will be about 8.3 feet. Then draw the parallel line above the grade-line already drawn at this distance from it, according to the vertical scale of the profile (in Fig. 18 taken as 40 feet to an inch); and again above that line draw another, distant from the grade-line by an amount corresponding to the depth of cut required to give 2000 cu. yds. in a length of 100 feet; and then draw a third for 3000 cu. yds., and so on, as many as are required. Similarly, on the lower side of the grade-line draw lines as above, suitable to the required base and slopes of the fill. Place the tracing-cloth over the profile, as in Fig. 18. If then the horizontal scale of the profile is 400 feet to an inch, take a "40" scale, and scale off along the horizontal dotted lines shown in the figure. One division of the scale then corresponds to 100 cu. vds. Thus, in order to make the cuts balance the fills (not allowing for shrinkage, etc.) the grade-line must be so placed that the sum of the horizontal dotted lines above it is equal to that of the lines below it. By sliding the tracing-cloth up and down, a balance can soon be obtained. By scaling off and adding the lengths of the lines together mentally, the contents of a cut or fill can be approximated to in a very few seconds; or the contents may be read off by means of the vertical divisions on the profile paper.

Where there is a steep surface-slope, an allowance must of course be added to the results as obtained by the above method. The allowance which should be made for this depends, comparatively speaking, very little on either the width of the roadbed or the depth of the cut or fill at the centre, but depends mainly on the slopes themselves; so that we may say roughly, that the following corrections are applicable to any ordinary depth of cut (or fill) or width of road-bed.

Thus, if by the above method we make the contents of a certain cut to amount to 20,000 cu. yds., with side slopes of

1 to 1, if the average surface-slope is about 10°, a fair estimate of the contents will be given by 21,000 cu. yds.

Slope Ratio.		Surfac	e-slope.	uly larg
Slope Rano.	5°	10°	15°	20°
1 to 1 1½ to 1	1 p. c. 2 p. c.	5 p. c. 8 p. c.	8 p. c. 20 p. c.	17 p. c. 45 p. c.

As to the effect of *shrinkage*, it may generally be ignored in dealing with the balancing of cuts and fills. (See Sec. 113.) A simple rule in dealing with rock-work is to assume that 100 cu. yds. of rock in excavation make 150 cu. yds. in embankment.

70. It has been assumed so far that in estimating the amount of excavation and embankment the method of centre-heights is used. In the long run the results so obtained may generally be considered to give sufficiently close results for most preliminary estimates. But when the surface-slopes are such as to necessitate continued corrections being applied, the average slopes at the different stations may be jotted down by the leveller when taking the elevations and the quantities worked out according to Mr. Trautwine's method of equivalent level sections, or some similar process.

CURVES.

71. Radius. Degree and Length of Curve.—Railroad curvature in Canada and the United States is expressed in

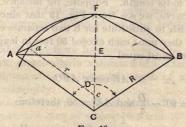


Fig. 19.

terms of the angle ACB, Fig. 19, which subtends a chord, AB,

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100 feet in length; and this angle is called the Degree of the curve, and equals D. description of large degree, D varies very

nearly inversely as the radius R.

To convert D into R, we have in the right-angled triangle AEC

$$\sin\frac{D}{2} = \frac{50}{R}; \quad . \quad . \quad . \quad . \quad (1)$$

and to convert Rinto D this becomes

$$R = 50 \operatorname{cosec} \frac{D}{2}, \dots (2)$$

from which formula Table I has been calculated.

From Equations 1 and 2 we see that R varies inversely as $\frac{D}{2}$, and since it is only when $\frac{D}{2}$ is very small that its sine may be considered to vary as the angle itself, it follows that although we may say that the radius of a 10' curve is one tenth that of a 1' curve, by considering the radius of a 10° curve to be one tenth that of a 1° curve, we should, on accurate work, be led into an appreciable error. Thus by Equation

R of a 1° curve = 5729.65 feet, Rof a 10° curve = 573.69 feet, and instead of 572.96.

72. The general practice of setting out curves on railroad construction is by means of 50-foot Subchords, assuming that the angle subtended by any subchord at the centre C is proportional to its length. Suppose, for instance, we wish to locate a 10° curve, we see from Fig. 19 that since AB = 100feet, if we wish to substitute for it two separate equal chords AF and FB, they must each exceed 50 feet in length, and the length of each must equal

AE cosec AFC.

Now
$$AFC = 90^{\circ} - \frac{D}{4}$$
 and $AE = 50$; therefore

Corrected 50-ft. chord =
$$50 \sec \frac{D}{4}$$
. . . . (3)

Thus, instead of using 50-foot chords it is the lengths given in the following table which must be used in order that two of them may give the same curve for the same deflection-angle as would be given by a 100 foot chord:

VALUES OF CORRECTED 50-FOOT CHORDS.

Deg.	Chord.	Deg.	Chord.	Deg.	Chord.	Deg.	Chord.
10	50.000	6°	50.017	110	50.057	16°	50.122
20	50.001	70	50.024	120	50.068	170	50.138
30	50.004	80	50.031	13°	50.080	180	50.155
40	50.007	. 90	50.039	140	50.093	190	50.172
50	50.012	10°	50.048	15°	50.107	200	50.191

If the above corrections are not applied, the curve that is set out, instead of passing through the point A will pass through α at a distance from F=50 feet, and its radius r will equal cF instead of CF, and

 $cF = 25 \sec CFA;$

therefore

$$r = 25 \operatorname{cosec} \frac{D}{4}$$
. (4)

If we compare this equation with Equation 2, we see that the radius of a curve of any given value of D set out by 50-foot chords, according to the usual method, is exactly equal to half the radius of a curve whose degree $=\frac{D}{2}$ set out by hundred-

foot chords. Thus the radius of a so called 10° curve, if set out by 50-foot chords, actually equals one half the radius of a 5° curve, i.e., 578.14 feet, not 573.69 as intended.

To find the corrected length of any other subchord, see Sec. 76.

The corrections which we have just seen to be necessary to accurate work, practically in a distance of 100 feet amount to nothing at all, but often in the total length of a curve they mount up considerably.

For instance, a 10° curve run in on location with a 100-foot chain, which should then of course be a true 10° curve, cannot be expected to "come out" well when tried on construction with 50-foot chords; for if the curve is 900 feet long and

the instrument work and measurement absolutely correct, it will not close by 0.8 foot.

73. The length of a curve, in terms of 100-foot stations, as measured along 100-foot chords, may be at once found by dividing the total angle (C) at the centre, in degrees, by the degree of the curve. Thus if L = true length of curve,

$$L = \frac{C}{D} = \frac{I}{D} \text{ (nearly)}, \qquad . \qquad . \qquad . \qquad . \qquad (5)$$

where I= angle of intersection. (See Eq. 7.) So that if the angle subtended at the centre of a 10° curve = 40° , the length of the curve along the chords = 400 feet; and this method, on account of its simplicity, is that usually adopted on railroad work for the measurement of curves. But the true length of the curve will of course be greater than this in the same ratio as the arc AFB in Fig. 19 exceeds the 100-foot chord AB. Now the angle at the centre of a circle which is subtended by an arc equal to the radius equals

$$\frac{180^{\circ}}{5} = 57^{\circ}.29578,$$

so that the true length of a curve is given by the equation

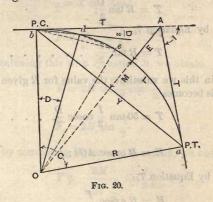
$$L = \frac{CR}{57,2958} = \frac{IR}{57,2958}. \quad . \quad . \quad . \quad . \quad (6)$$

Thus if $C=40^\circ$ and R=573.686 feet (i.e., a 10° curve), L=400.507 feet,—not 400 feet, as in the example above. Had this 10° curve been set out with corrected 50-foot chords, it would have measured (along the chords) 400.38 feet.

Table IV gives the length of arcs of various curves subtended by 100-foot chords, from which the true length of a curve may be at once found.

74. Before proceeding to the more practical problems in connection with the setting out of curves in the field, it will be well to consider a few of the more important equations which form the groundwork on which these problems are built up.

First, as regards the nomenclature of the various parts, as shown in Fig. 20.



P.C. = Point of Curve.

= Beginning of Curve.

P.T. = Point of Tangent.

= End of Curve.

A = Apex.

I = Intersection-angle.

C = Central angle.

L =Length of Curve.

D =Degree of Curve, if bd= 100 feet.

T =Sub-tangent.

E =External distance.

M = Mid-ordinate to Long Chord.

Y =Long Chord.

R = Radius.

These symbols will be maintained throughout this article on curves.

75. Now because Aa and Ab are tangents to the curve at a and b, therefore OaA and ObA must each equal 90° , and the angle aAb at the apex must equal $180^{\circ} - C$; therefore

Again, in the triangle bOd, since the angle at $b = 90^{\circ} - \frac{D}{2}$, therefore the

Tangential Deflect.-Angle for a 100-foot chord $=\frac{D}{2}$. (8)

In the right-angled triangle AOa

$$T=R anrac{C}{2};$$

therefore, by Equation 7,

$$T = R \tan \frac{1}{2} \dots \dots \dots (9)$$

And if in this we substitute the value for R given in Equation 2, this becomes

$$T = 50 \tan \frac{I}{2} \csc \frac{D}{2}$$
 (10)

Again,

$$E = R \operatorname{exsec} A0a;$$

therefore, by Equation 7,

And by combining Equations 9 and 11 we obtain

$$E = T \cot \frac{I}{2} \operatorname{exsec} \frac{I}{2};$$

therefore

$$E = T \tan \frac{I}{A}. \quad . \quad . \quad . \quad . \quad . \quad (12)$$

So also

of the proof
$$M=R$$
 vers $\frac{C}{2}$;

therefore, by Equation 7,

$$M = R \operatorname{vers} \frac{I}{2}$$
 (13)

And by combining Equations 11 and 13, we obtain

$$M = \frac{E}{\text{exsec } \frac{I}{2}} \text{ vers } \frac{I}{2};$$

therefore

$$M = E \cos \frac{I}{2}. \qquad (14)$$

Again, by trigonometry,

$$\frac{Y}{2} = T \cos Aab;$$

therefore

$$Y = 2T \cos \frac{I}{2}. \qquad (15)$$

And combining this with Equation 9, we obtain

$$Y = 2R \tan \frac{I}{2} \cos \frac{I}{2};$$

therefore

$$Y = 2R \sin \frac{1}{2} \cdot \dots \cdot \dots \cdot (16)$$

Again, by combining Equations 13 and 16, we obtain

$$Y = \frac{2M}{\text{vers } \frac{I}{2}} \sin \frac{I}{2};$$

therefore

$$Y = 2M \cot \frac{I}{4}. \qquad (17)$$

The above equations can readily be followed by referring to Secs. 231 and 232.

The following table may be of assistance in selecting quickly the equations required. Thus, suppose we have T and Y given, and want R; we see at once that Equation 15 will give us I; and then, by Equation 9, we can obtain R.

Given.	Required.	Use Eq.	Given.	Required.	Use Eq.
R. L. T. T. L. M. L. L. T. L. L. M. L. L. T. L. L. T. L. L. T. T. L. T. T. E. M. T. T. E. M. T. Y. L. T. T. E. M. T. Y. T. T. E. M. T. Y. T.	DD DD RR RR RR I I I I I I I I I I I I I	1 5 10 2 9 11 13 • 16 5 9 10 11 12 13 14	R, Y Y D, I R, D I, I, E Y I, I, R I, I, R I,	I L L T T T T E E E M M M Y Y Y	16 17 5 9 10 12 15 11 12 14 13 14 17 15 16 17

PROBLEMS IN SIMPLE CURVES

76. To lay out a curve by deflection-angles.—In Fig. 20 we have already seen (Eq. 8) that the angle $Abd = \frac{D}{2}$; but suppose we measure off another 100-foot chord de: then dbe also $=\frac{D}{2}$ (since boe=2D, which makes $Obe=90^{\circ}-D$). Similarly, we might show that for any number of consecutive 100-foot chords the total deflection-angle would, for each one, increase by the amount $\frac{D}{2}$.

But though the Total Deflection-angle from the tangent is proportional to the number of full stations when these are the only points given on the curve, as we have already seen in the case of 50 foot subchords, if we insert intermediate stations without correcting the lengths of the subchords, the degree of the curve increases at once.

In order to find the corrected length of any subchord we may proceed thus: In Fig. 21 let ab represent a hundredfoot chord, then the angle abc = D; and let l represent any
subdivision of it corresponding with the length of any uncorrected subchord: then the corrected length I will be given by I Equation 16, when

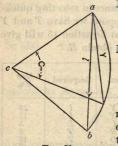


Fig. 21.

C: D = l: 100.

If we then insert this value of C in Equation 16, we obtain

$$Y = 2R \sin \frac{Dl}{200}$$
, . . (18)

Y being the corrected length of the nominal subchord ℓ . In ordinary work, except where a sharp curve is run continuously throughout with subchords, we may ignore this correction.

Not taking the correction into account, the deflection for any subchord is to $\frac{D}{2}$ as the length of the subchord is to 100 feet; so that for any subchord we have

Deflect. in $= 0.3D \times \text{Length of Subchord in feet};$ (19)

and this equation applies to a corrected subchord if we insert in it its uncorrected length.

Thus for a 14-foot subchord on a 3° curve the deflectionangle is 0° 12′.6.

Let us suppose that we are given a 3° Curve to the Right to locate from a P.C. at Sta. 421 + 36, I being equal to 12° 30'.

The length of the curve we find from Equation 5—since this is assumed as the standard method of measurement for railroad curves—to be 416.7 feet, therefore the P.T. will be at Sta. 425 + 52.7; then if we intend to use 50-foot subchords, our notes will be arranged as follows:

3° CURVE TO THE RIGHT.

P.C. = Sta. 421 + 36.0.
P.T. = Sta. 425 + 52.7.

Length of curve = 416.7 feet.

Intersection-angle = 12° 30'.

Subtangent = 209.2 feet.

Station.	Distance.	Deflection.	Index.	Remarks.
421 + 36	the fire office	olish yan e	00 0	P.C.
+ 50 422	14	0° 12′.6	0° 12′.6	SEASON STATE
422	50	0° 45′	0° 57′.6	
+ 50	AND THE PARTY.	EDW RE 40001	1° 42′.6	BORTE 113
423	Interior with	(addition and the	2° 27′.6	
+50	The second second	CONTRACTOR OF THE PARTY OF THE	3° 12′.6	Hub.
424	THE PROPERTY OF	Terral " ow	3° 57′.6	Souther off
+50	66	**	4° 42′.6	
425	and a street be	B bobtovnes	5° 27′.6	butt mitt after
+50	44	44	6° 12′.6	
+52.7	2.7	0° 02′.4	6° 15′	P.T.

The *Index*-reading at any station equals the sum of the *deflections* up to that station; then since the Index-reading at the P.T. is represented by the angle Aba in Fig. 20, and Aba is easily proved equal to $\frac{I}{2}$, therefore the Index-reading at the P.T. must equal half the intersection-angle, thereby giving a check on the calculations.

Having the notes worked out as above, set the transit up at the P.C. as in Fig. 22, and setting the index to zero, clamp the telescope on to a back-sight on the tangent (or on to the apex if it has been put in); then for any station the vernier must read the angle given in the index-column for that station. But suppose that when we have reached Sta. 423 + 50 we are unable to see any farther. Then set a hub (with a tack in it) at that station and a back-sight at the P.C. Set up over the hub,

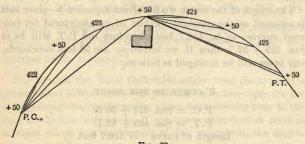


Fig. 22.

and setting the vernier back to zero, clamp the telescope on to the back-sight and turn off the remaining deflections by making the readings for the respective stations the same as those given in the Index-column. Thus:

- (1) When pointing to any station, the vernier must always be set to read the Index-reading for that station.
- (2) When on the tangent at any station, the vernier must always be set to read the Index-reading for that station.

By adhering to these two rules all possibility of error as regards the index-readings is avoided, and with the notes worked out as above we may locate the curve equally well from either end.

In order to find the bearing of the tangent at any station with reference to the tangent at the P.C., we have simply to multiply the index-reading at that station by two. Thus, if in the above example the tangent at the P.C. lies north and south, the bearing of the curve at Sta. 423 + 50 will be N. 6° 25'.2 E.

Usually in locating railroad curves there is no necessity to work out the deflections closer than to the nearer half-minute.

In places where accurate measurement is difficult to obtain, and great exactness is wanted, as in giving centres for piers in the middle of a river, we can often do better work by using Two Transits, one on either side of the stream, and fixing the points by intersection. (See Sec. 163.)

77. To locate a curve when the apex is inaccessible.

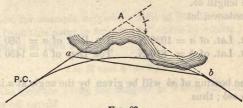


Fig. 23.

—Suppose, as in Fig. 23, we have been unable to locate the apex of a proposed curve, but have connected the two tangents at a and b by the line ab.

Then in the triangle Aab we know the distance ab and the angles at a and b; therefore we have

$$Aa = \frac{ab \sin b}{\sin A},$$

where $A=180^{\circ}-(\alpha+b)$. We can then find the position of the P.C. For example, suppose Aa=.320 feet and $I=40^{\circ}$; then if we wish to connect the two tangents by a 5° curve, since the distance from A to the P.C. is given by Equation 9 (or Table II) = 417.2 feet, therefore the P.C. will be situated 97.2 feet back on the tangent from a.

We can then locate the curve according to Sec. 76.

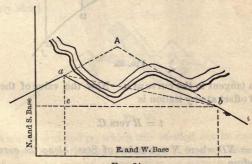


Fig. 24.

But suppose, instead of running a direct line ab, it is more

convenient to run a succession of courses as in Fig. 24. Then, if the position of the stations a and b has been worked out by "Lats, and Deps." we can at once find the angles at a and b and the length ab.

For instance, let

Tot. Lat. of
$$a = 1020$$
 N. Tot. Dep. of $a = 560$ E. Tot. Lat. of $b = 810$ N. Tot. Dep. of $b = 1430$ E.

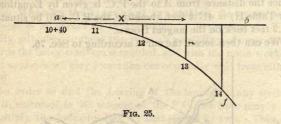
Then the bearing of ab will be given by the angle at a in the triangle aeb; thus

$$\tan a = \frac{1430 - 560}{1020 - 810} = 4.143.$$

Therefore the bearing of $ab = S.76^{\circ}.26'$ E., and the length $ab = (1020 - 810) \sec a = 895.2$. Then if the bearing of the tangent at $a = N.80^{\circ}$ E., and of the tangent at $b = S.60^{\circ}$ E., we have in the triangle Aab, $a = 23^{\circ}.34'$ and $b = 16^{\circ}.26'$ from which we can find the position of the P.C. as above.

If the notes have not been already worked out by Lats. and Deps. the position of b with reference to a can be most easily calculated by taking the tangent at a as the N. and S. base.

78. To locate a curve by offsets from a tangent.—Let



ab be a tangent to the curve at a. Now the value of the tangential offset at any station is

$$t = R \text{ vers } C.$$

But C = ND where N = number of Stas. along the curve to t_i therefore

$$t = R \text{ vers } ND. \dots (20)$$

Similarly, the distance along the tangent from a to the offset t equals

$$X = R \sin ND. \quad . \quad . \quad . \quad (21)$$

Thus, for example, suppose a falls at Sta. 10 + 40, and we wish from this point to set out a 10° curve by offsets from the tangent at a; then at Sta. 11

$$t = R \text{ vers } 6^{\circ} = 3.14 \text{ feet,}$$

and the distance along the tangent at which this offset mustbe set off equals

$$X = R \sin 6^{\circ} = 59.95 \text{ feet.}$$

The values of t at distances along the curves from a, 100 feet apart, are given in Table III, calculated by Equation 20.

A formula that often comes in handy in the field for computing tangential offsets, and which is usually true enough when X does not exceed 150 feet, is

$$t = \frac{X^2}{2R}$$
 (nearly).

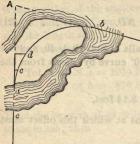
Tangential offsets may often be made use of when, on account of some obstacle or other, the method given in Sec. 76 cannot be used. By offsetting the tangent itself occasionally, as in Fig. 26, we can with ease run a curve past a succession of obstacles, and at the same time keep the offsets comparatively short.



Another occasion on which this method can be used to advantage is when the apex, P.C. and P.T. are inaccessible.

Suppose, by way of example, that we have to locate a 10° curve in a position such as is represented in Fig. 27, the angle

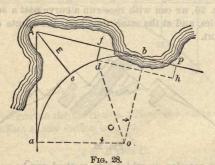
of intersection having been found according to Sec. 77 to be,



say, 90°, and the distance from A to some fixed accessible point e to be 723.7 feet: then ae will equal 150 feet. Suppose we are able to begin running in the curve at c, a point 200 feet along the curve from a: then the offset at c will equal 34.6 feet, at a distance from a along the tangent of 196.2 feet or from e = 346.2feet; and the offset at d. 300 feet along the curve from a,

equals 76.9 feet at a tangential distance of 286.8 feet from a, or from e = 436.8 feet. Thus we have two points c and d fixed on the curve, by means of which we can locate any other part of the curve accessible to them, as shown in Sec. 76.

Or, suppose we have such a case as that shown in Fig. 28, where we have run the curve ab round as far as d, but find that the P.T. is inaccessible, and yet wish to get on to the tangent without adopting the method given in Sec. 77. A convenient method of doing this is to locate the apex A, if accessible, by setting off from e, the middle point of the curve, the external E, found by Equation 11; then we have one point on the tangent Ab.



Again, by running on the curve as far as is possible to d, we can there set the vernier to read the (Index-reading for b+ Diff. of Index between d and b) - 90° and set off df = t,

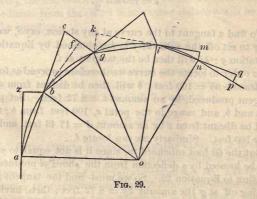
found by Equation 20: thus if the Index-reading for $d = 40^{\circ}$ and for $b = 60^{\circ}$, the vernier must read $60^{\circ} + 20^{\circ} - 90^{\circ} = -10^{\circ}$.

The angle ND in Equation 20 equals of course the angle dob. We thus have a second point f on the tangent Ab, and therefore we have its direction. Then by Equation 9, since Ab = T, we can, by triangulation, find the distance of A from some accessible point p on the tangent; then bp = Ap - T. Or, since by Equation 21, $fb = R \sin dob$ we can triangulate from p to f instead.

If A is inaccessible also, instead of proceeding as in Fig. 27, we might when at d set the vernier to the (Index-reading for b + Diff. in Index between d and b), which will give a line dh parallel to the tangent at b. Thus the vernier must read 80° . We can then set off ph = df, and thus obtain two points f and p in the direction of the tangent Ab; and since we know dh = fp by direct measurement, and fp by calculation, we thus have the distance bp.

Again, if we have an obstacle on the curve itself, we can run a tangent from some point on the curve which will clear it, and so connect the curve at the further side in a similar way to that shown in Fig. 27; or we might run a Long Chord past it and lay it off by ordinates as in Sec. 80.

79. To locate a curve by offsets from the chords produced.—Let it be required to locate a 10° curve an by offsets



from the chords produced, and let, for example, the length of the curve = 360 feet. In Fig. 29—exaggerated for the sake of

clearness—let ab, bg, and gi be 100-foot chords, then if eb is in the same straight line as ab and is equal to bg, the triangle beg is similar to the triangle obg; therefore

$$bg: R = eg.bg.$$

So that, calling the chord bg = c, and the chord deflection eg = d, we have

$$d = \frac{c^2}{R}, \dots \dots \dots \dots (22)$$

but this value of d of course only holds good when the length of the preceding chord (as ab) is equal to c.

Again, if $fg = \frac{1}{2}eg$, then the triangle bfg = the triangle <math>axb, therefore $xb = \frac{1}{2}eg$. Therefore, if t = the tangential offset,

$$t = \frac{c^2}{2R}, \dots \dots \dots \dots (23)$$

a formula (already given in the last section in other terms) which holds good for any lengths of chord, provided the angle at $x = 90^{\circ}$.

When c = 100 feet, we also have the formula

$$t = 100 \sin \frac{D}{2}.$$

To find a tangent to the curve at any station, say i, we have only to set off the value of t = kg, obtained by Equation 23, at station g; ki will then be the tangent at i.

In order to locate the curve we therefore proceed as follows: Measure ab = 100 feet; b will then be distant from ax, the tangent produced, by an amount t = 8.72 feet. Set pickets at a and b, and range in the point e, 100 feet from b; then g will be distant from e by an amount d = 17.43 feet, and from b by 100 feet. Similarly we can locate i.

But the 60-foot subchord in, since it is not equal to gi; cannot be located by a deflection from the chord gi produced, according to Equation 22. So we must find the tangent at i by setting off at g the amount kg = 8.72 feet; then, having obtained the tangent at i, we can calculate the offset mn for the 60-foot chord in (by Equation 23), which equals 3.14 feet, and

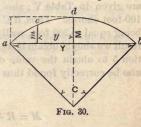
this brings us to the P.T. of the curve. In order to find the direction of the tangent at n we may either set off at i the value of t for the chord in, or we may produce the chord in to q, making nq = in, and then from q set off an offset qp = mn; np will then be the direction of the tangent.

Theoretically, we ought always to make the angle between a tangent and its offset $= 90^{\circ}$, and between a chord produced and its offset $= 90^{\circ} - \frac{1}{2}$ angle subtended by the chord at the centre; but in ordinary work there is no need to be particular about this.

80. To locate a curve by ordinates from a long chord.

—Suppose, as in Fig. 30, we have two stations a and b given, we then have the length of the arc adb, and so we can find C by Equation 5.

Now if d is the middle point on the curve the deflection-offset t from the tangent at d to a = M, the ordinate at d; therefore, by Equation 20,



$$M = R \operatorname{vers} \frac{C}{2}, \ldots (24)$$

M being the *mid-ordinate* to the long chord Y. The length of an ordinate from the chord to any other station e will be given by the equation

$$m = M - R$$
 vers ND , . . . (25)

where N = the number of stations measured along the curve from d to e; and the distance from the centre of the long chord at which m must be set off is given by

$$y = R \sin ND, \quad \dots \quad (26)$$

which is the same as Equation 21 for the value of X in Sec. 78. To take an example: Suppose a is at Station 2+20 and b at Station 6+40, then d will fall at Station 4+30. Let $D=10^\circ$, then $C=42^\circ$; and we can find Y either by direct measurement or by Equation $16=2R\sin 21^\circ=411.2$ feet. Similarly by Equation 23 we find M=38.1 feet,

If we then wish to set off an ordinate to Sta. 3.00, we have N=1.3; therefore $y=R\sin 13^\circ=129.1$ feet, and m, by Equation 24, =38.1-R vers $13^\circ=23.4$ feet.

It is usually unnecessary to calculate the values of y, except perhaps when near the ends of the chord. Thus, in the above example, had we assumed y = 100N = 130 feet, it would practically have made no difference in the position of Sta. 300.

If we have the length of the chord Y given, we may obtain C directly from it by means of Equation 16; or, conversely, when we know C we can obtain Y.

The lengths of Long Chords subtending arcs up to 6 stations are given in Table V; also the length of arcs subtended by 100-foot chords. Thus, if $C=20^\circ$ and $D=10^\circ$; Y instead of being equal to 200 feet, really equals 200.254 feet, which is the result we should obtain if we used Equation 6 instead of Equation 5 to obtain the value of L. The middle ordinate may also be correctly found thus:

$$M = R - \sqrt{R^2 - \frac{Y^2}{4}}, \dots (27)$$

and any other ordinate

$$m = M - R + \sqrt{R^2 - y^2}$$
. . . (28)

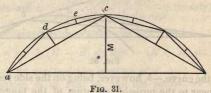
An approximate formula, which is really a corruption of Equation 27, is

$$\mathbf{M} = \frac{Y^2}{8R} \text{ (nearly)}. \qquad . \qquad . \qquad . \qquad . \qquad (29)$$

It is sufficiently true, however, when Y is small, the error on a 20° curve, in the case of a 50-foot chord, only amounting to .002 foot. By comparing Equation 29 with Equation 23, we see that the mid-ordinate to a short chord may be considered equal to one quarter the tangential offset at a distance along the tangent equal to the chord.

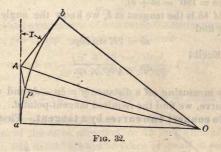
A convenient method of locating small arcs is that shown

in Fig. 31, where, having found M by Equation 24 or 29, the mid-ordinate for the subchord ac may be considered equal to



1M, and the ordinate e of the sub-subchord dc similarly equal to one quarter the ordinate at d.

81. To pass a curve through a fixed point, the angle of intersection being given.-Suppose we first find the



position of the fixed point p (Fig. 32) with reference to Aa in terms of the distance Ap and the angle aAp; then

$$pAO = 90^{\circ} - \left(aAp + \frac{I}{2}\right),$$

and

$$\sin ApO = \sin pAO \sec \frac{I}{2};$$

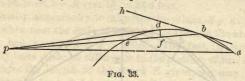
therefore in the triangle ApO we have pO equal

$$R = Ap \sin pAO \operatorname{cosec}(pAO + ApO).$$

ApO always exceeds 90°.

82. To run a tangent from a curve to any fixed point.

Let p (in Fig. 33) be the fixed point, and a and b be any two



points on the curve,—b, however, being on the side remote from p, yet as near to the probable situation of the tangent-point d as is possible. Then taking the chord ab as a base, the length of which is given by Equation 16, observe the angles at a and b in the triangle abp; then

$$bp = ab \sin a \csc apb$$
,

when $apb = 180^{\circ} - (a + b)$.

Now if bh is the tangent at b, we know the angle hbp, and can thus find

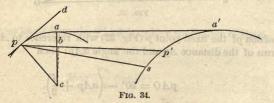
$$eb = 2R \sin hbp.$$

But by Euclid

$$dp = \sqrt{bp \times ep}$$
.

Thus by measuring off a distance bf = bp - dp and offsetting to the curve, we find the required tangent-point d.

83. To connect two curves by a tangent.—First suppose,



as in Fig. 34, that both curves are of the same direction. On the curve of smaller radius R select a point p slightly more remote from the other curve than the tangent-point at a probably is. On the curve of larger radius R' find a point p' which has its tangent parallel to the tangent at p. This may be done by running a trial-line to some station s; and then, by comparing the direction of the tangents at p and s, we find how far along the curve from s, p' will be situated.

Now if pd is the tangent at p, and cb is perpendicular to pp', we have pca = dpp' - acb, and

$$\sin acb = rac{(R'-R) \operatorname{vers} dpp'}{pp' + (R'-R) \sin dpp'}$$
 (nearly),

pp' being obtained by direct measurement; and

$$aa' = pp' + (R' - R)\sin dpp' - (R' - R)\sin acb,$$

from which we can find the position of a'.

But suppose, as in Fig. 35, the two curves are of opposite direction.



Fig. 35.

Then select p on the side of a towards the other curve. Then, as before, pca = dpp' - acb; but in this case

$$\sin acb = \frac{(R' + R) \operatorname{vers} dpp'}{pp' + (R' + R) \sin dpp'} \text{ (nearly),}$$

and

$$aa' = pp' + (R' + R)\sin dpp' - (R' + R)\sin acb.$$

The distance ap should never exceed 100 feet when the curves are of the same direction, or 75 feet when of opposite direction, and should always be taken as small as possible,

84. Given a curve joining two tangents, to change the P.C. so that the curve may end in a parallel tangent.

Let it be required to move the P.C. at a (in Fig. 36) so that the curve ab, instead of ending at b, will end in a parallel tangent, distant from the tangent at b by the amount e.

Then, since it is simply a case of shifting the curve bodily in the direction of the tangent aa', we have

$$aa' = e \operatorname{cosec} I$$
.

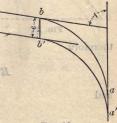


Fig. 36.

Had a'b' been the given curve, and it were required to shift

it outwards to the parallel tangent at b, the same equation of course applies.

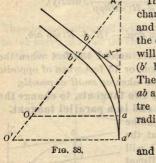
85. Suppose we have such a case as that shown in Fig. 37, where ab is the given curve, and it is required to shift it to parallel tangents at each end, as at a' and b'.



Fig. 37.

Then starting from the tangent at a, we can, as above described, shift the curve from the tangent at b to the tangent at b', and from the tangent at a we can in the same way shift it on to the tangent at a', which gives us the required positions of a' and b'.

86. Given a curve joining two tangents, to change the radius and the P.C. so that the new curve may end in a parallel tangent at a point opposite to the original P.T.



In Fig. 38 let it be required to change the radius of the curve ab and also the position of a, so that the curve, instead of ending in b, will end in a parallel tangent at b' (b' being directly opposite to b). Then if O is the centre of the curve ab and R its radius, and O' the centre of the curve a'b' and R' its radius, by Equation 11,

 $Ab = R \operatorname{exsec} I,$ $Ab' = R' \operatorname{exsec} I;$

therefore

$$R' - R = \frac{bb'}{\text{exsec } I'}$$

and

$$aa' = bb' \cot \frac{I}{2}$$

Had a'b' been the given curve, and it were required to shift

it outwards to the parallel tangent at b, the same equations of

course apply.

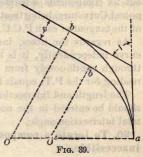
87. Given a curve joining two tangents, to find the radius of another curve which, from the same P.C., will end in a parallel tangent.

Let it be required to change the radius of the curve *ab*, so that it will end in a parallel tan-

gent at b'.

Let O be the centre of the curve ab and R its radius, and O' be the centre of the curve ab' and R' its radius. Then R - R' = OO'; therefore

$$R - R' = \frac{e}{\text{vers } I}$$



Had ab' been the given curve, and it were required to shift it outwards to the parallel tangent at b, the same equation of course applies.

88. Given a curve joining two tangents, to change the radius and position of the P.C. so that the curve may end in the same P.T., but with a given change in direction.

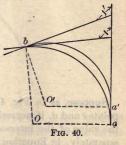
In Fig. 40 let it be required to change the radius and P.C. of the curve ab, so that at b it will have a difference in direction equal to I' - I. Then if O is the centre of the curve ab and R its radius, and O' and R' are the centre and radius of the curve a'b,

$$R \text{ vers } I = R' \text{ vers } I'$$
:

therefore

$$R' = \frac{R \text{ vers } I}{\text{vers } I},$$

and $aa' = R \sin I - R' \sin I'$.



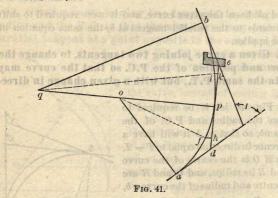
COMPOUND CURVES.

89. A compound curve, being merely a series of two or more simple curves, the manner in which it is located is by setting out its components separately, each P.C.C. (Point of Compound Curvature) being treated as a P.C. or P.T., the direction of the tangent at each P.C.C. being given by its Index-reading.

As regards the notes, instead of keeping them for each curve independently, it is better to carry the Index-reading through continuously from the P.C. to the P.T., so that the reading for the P.T. equals half the *total* intersection-angle.

The length and intersection-angle of *each* component curve should be entered in the notes, and also the total length and total intersection-angle.

90. To locate a compound curve when the P.C.C. is inaccessible.



Suppose, as in Fig. 41, p (the P.C.C.) is inaccessible. The points e and d, if accessible, may then be found by inserting the value of the intersection-angle, in the case of each curve separately, in Equation 9, and thus obtaining for T the distances ad and be.

Then from the tangent de the curve can be located by offsets, as already shown.

If the points d and e are also inaccessible, select in the curve some convenient point f, and from it set off the offset fh =

of vers fop (by Equation 20). Similarly, from a point in the other branch of the curve lay off an offset ik = qi vers iqp. We can then find the position of p by Equation 21; thus:

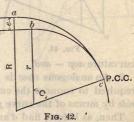
$$hp = of \sin fop.$$

- 91. Given a simple curve ending in a tangent, to connect it with a parallel tangent by means of another curve.
- 1. Let ac in Fig. 42 be the given curve, and be the required curve: then we have

$$\cos C = 1 - \frac{e}{R - r},$$

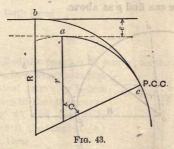
from which we can at once find the P.C.C.

2. Let be the given curve,



and ac the required curve: then since C, the central angle, is the same for both curves, the above equation holds good also in this case.

92. To connect a curve with a tangent by means of another curve of given radius,

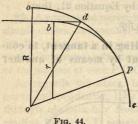


1. Let ac in Fig. 43 be the given curve which it is required to connect with a given tangent at b. Find the point a on the given curve which has its tangent parallel to the given tangent, and measure e: then, since

$$\cos C = 1 - \frac{e}{R - r'}$$

we can thus find the position of the P.C.C.

2. But if the radius of the required curve is less than that of the other curve, then, as in Fig. 44, find the point d_{*}at the



intersection of the tangent at b with the given curve ac, and observe the angle of intersection at d = aod; then

$$\cos aop = \frac{R \cos (aod) - r}{R - r}.$$

Thus p, the P.C.C., will be situated at a distance along the curve from d represented by the

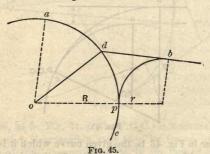
curvature aop - aod.

3. An analogous case is that shown in Fig. 45, where it is required to connect the curve ac with a tangent on the convex side by means of the curve pb.

Then, as before, find d and observe the angle of intersection at d = aod; then

$$\cos(aop) = \frac{R\cos(aod) - r}{R + r},$$

from which we can find p as above.



Suppose in case 3 the point d were found to coincide with a; then we merely have the case of a Y located on the tangent db, in which case the above formula becomes

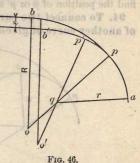
$$\cos(aop) = \frac{R-r}{R+r}.$$

93. Given a compound curve ending in a tangent, to

change the P.C.C. so that the terminal curve may end in a given parallel tangent without changing its radius.

1. In Fig. 46 let the radius of the terminal curve pb be greater than the radius of the other curve-pa; then,

A. If we want to shift the curve inwards to b', then to find p', the new position of the P.C.C., we have



but.

B. If apb' were the given curve, and it were required to shift it outwards to b, then

$$\cos o = \cos o' - \frac{e}{R - r};$$

and since in both cases

$$pqp'=o-o',$$

we can thus find the position of p or p', as the case may be.

2. Suppose, however, the radius of the terminal curve bp is less than the radius of the other curve pa as in Fig. 46, and that it is required to shift the tangent (A) inwards to b: then

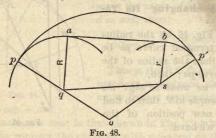
$$\cos o' = \cos o - \frac{e}{R - r}.$$

But (B) if ap'b' were the given Fig. 47. compound curve, and it were required to shift it *outwards*, then

$$\cos o = \cos o' + \frac{e}{R - r}.$$

Then since in both cases (A) and (B) pqp' = o' - o, we can find the position of p or p' as the case may be.

94. To connect two curves, already located, by means of another curve of given radius.



As in Fig. 48, let R be the radius of the easier curve, and r the radius of the sharper curve. Find the tangent ab as shown in Sec. 83, and also the distance ab by direct measurement or calculation; then

$$\tan (aqs) = \frac{ab}{R - r},$$

and

$$qs = ab \csc (aqs)$$
.

Then, since oq = op - R and os = op' - r, where op and op' are each equal to the radius of the required curve, we have the three sides of the triangle oqs, from which we can find the angle oqs (see Sec. 231); and

$$aqp = 180^{\circ} - (oqs + aqs).$$

Thus we can find the position of p.

Similarly, we can find the position of p'; or we can calculate the angle at o, which does equally well.

The radius of the required curve must exceed

$$\frac{qs+R+r}{2}$$

If R=r, then

$$\sin (aqp) = \frac{ab}{2(op - R)}.$$

95. To locate any portion of a compound curve from any station on the curve.

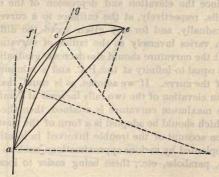


Fig. 49.

Let abce in Fig. 49 be a compound curve, and a any station on the curve, and let it be required to establish the point e; the P.C.C.'s at b and c being inaccessible.

Assume, for the sake of simplicity, that the chords ab, be, and ce are equal, and let the curvature of be equal twice the curvature of ab, and that of ce three times the curvature of ab.

Now if d = the deflection from the tangent at a for Sta. b, then, if ab be produced to f, the angle fbc = d + 2d = 3d. Again, if the chord be produced to g, the angle ecg = 2d + 3d= 5d. Then in the triangle abc, the angle at $b = 180^{\circ} - 3d$: and since the length of the chords can be found by Equation 16 (Sec. 74), we can find the side ac and the angles at a and c. Again, in the triangle ace, the angle at $c = 180^{\circ}$ -(bca + 5d); thus we can find the angle at a. Similarly we can find the angle subtended at a by the chord bc, and thus we have the total deflections to b, c, and e. When the chords are of different lengths, as is of course usually the case in practice, and the curvature varies irregularly, we can by plotting the curves and drawing the tangent at each P.C.C. see at once in each case what the deflection-angle at any P.C.C. will be from the chord produced. The principle will be just the same as in the case above described.

Sec. 96 is an application of this problem.

TRANSITION CURVES.

96. Since the elevation and depression of the outer and inner rails, respectively, at the entrance to a curve must be made gradually, and for any given speed the difference in elevation varies inversely as the radius of curvature, it follows that the curvature should also decrease gradually, having a radius equal to infinity at the P.C. and a minimum at the centre of the curve. If we assume, as is usual, that the difference in elevation of the two rails increase at a uniform rate until the maximum curvature is attained, then the theoretic curve which should be adopted is a form of the elastic curve, which, on account of the trouble involved in locating it, has been supplanted by various approximations, such as the curve of sines, parabolæ, etc.; these being easier to locate in the field.

The use of Transition Curves is found not only to cause less resistance to the passage of trains than a similar curve whose ends are not eased off, but also generally to enable the curves to be fitted better to the ground than in the case of plain circular ones.

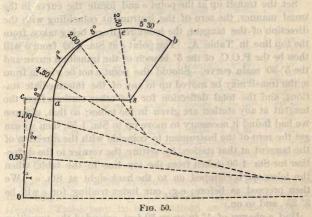
That Transition Curves are of advantage in actual practice is shown by the fact that all Simple Curves at their P.C.'s and P.T.'s have a decided tendency to assume the form of the Elastic Curve; and since this lateral creeping is caused by the pressure of the flanges of the wheels, increased wear and tear to rails and rolling-stock is the result.

It is to be noticed that the easing of curves in many cases involves an increase in curvature at the centre of the curve, but this is usually so slight as to be practically inappreciable, and is much more than compensated for by the reduction of curvature at the ends of the curve. Thus, for example, where a 9° simple curve defines the limit of curvature in the case of uneased curves on any road, by inserting transition curves a 10° curve would be perfectly allowable.

The three following methods of inserting transition curves are simple and easily applied:

97. Method I.—Suppose, as in Fig. 50, that we have a 5° 30′ curve ab, which it is required to ease off by means of a transition curve.

Now if we do not wish to shift the main curve inwards from the tangent at a, it becomes necessary to shift the tangent at a



itself outwards by the amount ac, and also to throw the P.C. at a backwards by the amount ac, so that the point ac becomes the new P.C.

Now

$$ac = Y \sin d - R \text{ vers } C$$

and

$$oc = Y \cos d - R \sin C$$
,

where Y = the long chord to the end of the transition curve; d = the total deflection-angle from Sta. o to the end of the transition curve (given in top line of Tables A and B in this section); C = the total curvature of the transition curve, as represented by the angle esa (values of which are given in Tables A and B); and R = Radius of the main curve.

The values of the first term in each of these equations are also given (i.e., $Y \sin d$ and $Y \cos d$) in Tables A and B.

Suppose we consider that a transition curve which increases its curvature by 1° in every 50 feet (as in Table A) will suit the case in question, then we want 250 feet of such a curve in order that the increase in curvature at no point may exceed 1°, and in that case we find from the above formula that oc = 113.40 feet and ac = 3.06 feet; so that the tangent must be offsetted to the

left a distance of 3.06 feet, and the new P.C. will be situated 113.40 feet back from the original one.

Set the transit up at the point o and locate the curve in the usual manner, the zero of the instrument coinciding with the direction of the tangent, the index readings being taken from the top line in Table A. The point e at Sta. 2.50 from o will then be the P.C.C. of the 5° branch of the transition curve and the 5° 30' main curve. Should the point e not be visible from o, the transit may be moved up to any of the intermediate stations, and the total deflection for the other stations from the tangent at any station are given in the tables; so that, suppose we had found it necessary to move up to Sta. 1.50, then we can get the zero of the instrument to coincide with the direction of the tangent at that station, by setting the vernier to the deflection for Sta. 1.50 (taken from the top line in the table) when the telescope is clamped on to the back-sight at Sta. o. We then proceed as before; e.g., our index-reading for e will be 3° 25', and so on.

Had a change of 1° in every 50 feet extended the transition curve too much, we might have adopted the curve given in Table B.

TABLE A .- CHANGING 1° IN EVERY 50 FEET.

Total Deflections from the Tangent at any Station, and the Values of C, $Y \sin d$, and $Y \cos d$.

0	.50	1.00	1.50	2.00	2.50	3.00
Transit 0° 15' 0° 521 1° 50' 3° 071 4° 45' 6° 421	Transit. 0° 30' 1° 22\frac{1}{2}' 2° 35' 4° 07\frac{1}{2}'	0° 37½' 0° 30' Transit. 0° 45' 1° 52½' 3° 20' 5° 07½'	1° 10′ 1° 07½ 0° 45′ Transit. 1° 00′ 2° 22½′ 4° 05½′	1° 52½' 1° 55' 1° 37½' 1° 00' Transit. 1° 15' 2° 52½'	2° 45′ 2° 52½ 2° 40′ 2° 07½′ 1° 15′ Transit. 1° 30′	3° 47½ 4° 00′ 3° 52½′ 3° 25′ 2° 37½′ 1° 30′ Transit.
C	· 0° 30′	1° 30′	3° 00′	5° 00′	7° 30′	10° 30′
Y sin coin feet		1.09	3.05	6.54	11.98	19.80
Y cos din feet		99.99	149.95	199.81	249.41	298.74

TABLE B.—CHANGING 2° IN EVERY 50 FEET.

					Total Carlo Paris	No. of Contract of the Contract of the
0	.50	1.00	1.50	2.00	2.50	3.00
Transit, 0° 30′ 1° 45′ 3° 40′ 6° 15′ 9° 30′ 13° 25′	0° 30′ Transit. 1° 00′ 2° 45′ 5° 10′ 8° 15′ 12° 00′	1° 15′ 1° 00′ Transit. 1° 30′ 3° 45′ 6° 40′ 10° 15′	2° 20′ 2° 15′ 1° 30′ Transit. 2° 00′ 4° 45′ 8° 10′	3° 45 3° 50 3° 15' 2° 00' Transit. 2° 30' 5° 45'	5° 30′ 5° 45′ 5° 20′ 4° 15′ 2° 30′ Transit. 3° 00′	7° 35′ 8° 00′ 7° 45′ 6° 50′ 5° 15′ 3° 00′ Transit.
C	1° 00′	3° 00′	6° 00′	10° 00′	15° 00′	21° 00′
Y sin d in feet.	0.44	2.18	6.10	13.06	23.89	39.37
Y cos d in feet.	50.00	99.98	149.80	199.32	248.12	295.70

The stations located as above need only be considered as temporary ones, by means of which the true stations may be located. These may be best obtained as follows: Suppose Sta. o falls really at Sta. 304 + 34, then Sta. 304 + 50 can be located by stretching a tape between temporary Stations o and 0.50 and setting off the ordinate M(Equation 24, Sec. 80) 16 feet along it from o, and so on between the different stations. Values of M are given in the following table for a 1° curve. The value of M for any other curve may be considered to vary as the curvature, so that, for example, for a 9° curve the ordinate at any point will be 9 times that given in the table for the corresponding distance.

VALUES OF M FOR 1° CURVE, 50-FT. CHORDS.

Dist. from Temp. Sta.	M in feet.	Dist. from Temp. Sta.	M in feet.	Dist. from Temp. Sta.	M in feet.
2 ft.	.011	10 ft.	.035	18 ft.	.050
6 "	.016	12 "	.040	20 "	.052
8 "	.030	16 "	.048	24 "	.054

The principal objection which can be urged against this curve is its rigidity; this is in a great measure overcome by having the option of the two sets of curves given above, one changing by 1° every 50 feet, and the other by 2°. Generally speaking, the former is adapted to curves not exceeding 7°, and

the latter to curves of from 6° to 14° curvature; while for curves of from 5° to 8° either set may be employed.

Another objection which may be brought against it, and one which is often brought against transition curves generally, is that it is not worth the trouble taken in locating it. As regards this, the use of transition curves, not only theoretically but practically, is found to reduce the resistance of the curve very materially, to lessen the cost of maintenance of way, to reduce the chances of derailment, and considerably to ease the motion of the cars.

There is no need to set out the transition curves during the location, but the tangent in any instance should be run to c (Fig. 50) and the transit then offsetted to a, from which point the main curve can be located. The amount of the offset ac, and the distance oc, should be added to the notes of the curve, and also the distance ae, which represents C. The general plan of the location then shows the curves as in Fig. 16. Then when the engineer takes charge of the work for construction he has simply to "reference" the points o and e, and run in the curve by means of the above table, as easily as he would any simple curve.

98. Method II.—Another form of transition curve is that

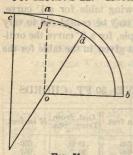


Fig. 51.

shown in Fig. 51. It is especially suitable in cases where it is more convenient to offset the curve than the tangent itself. It practically converts the original simple curve into a 3-centre one, but where the curvature of the main curve is light, it answers the purpose of easing off the curvature at its ends sufficiently in ordinary cases.

In Fig. 51, let r = radius of the original main curve ab.

Offset ab inwards by an amount af = e; then if R = radius of the terminal curve cd, we have

$$\cos fod = 1 - \frac{e}{R - (r - e)},$$

from which we can find the position of d; and

$$ca = R - (r - e) \sin fod$$

from which we can find the position of c. The curve cd can then be best located with a transit from the point c.

A convenient method of applying this principle in practice is to make e = 0.2 foot for every degree of curvature of ab, and to make R = 3(r - e); then if we make fd = 33.9 feet, d is the P.C.C., and

$$ca = 2(r - e)\sin fod,$$

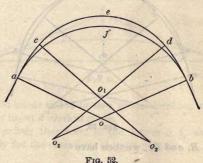
fod being found from the formula

$$\cos fod = 1 - \frac{e}{2(r-e)}.$$

For ordinary curves ca then varies from 75 to 100 feet.

99. Method III.—Another method of substituting a 3-centre curve for a simple one, when we do not wish to change the original tangent-points, is as follows:

In Fig. 52 let o be the centre of the original simple curve afb, the radius of which = R; and let o_1 be the centre of the new main curve ced, whose radius $= R_1$. And let o_2 , o_2 be the centre of the terminal curves ac and db, whose radii $= R_2$.



1. Given R_1 and R_2 . Then

$$\sin\frac{co_1d}{2} = \frac{(R_2 - R)\sin\frac{aob}{2}}{R_2 - R_1},$$

and

$$ao_2c=\frac{aob-co_1d}{2}.$$

Thus we obtain the position of the points c and d.

2. Given R_1 and $ao_2c = bo_2d$.

Then

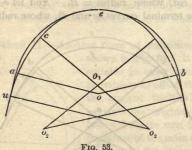
$$R_2=rac{R\,\sinrac{aob}{2}-R_1\,\sinrac{co_1d}{2}}{\sinrac{aob}{2}-\sinrac{co_1d}{2}},$$

The curvature of the arc ced should never exceed that of ab by more than 1° (about 50' excess is usually a suitable amount), and R_2 should equal about 3R.

The distance

$$fe = (R_2 - R_1) \sin ao_2 c \csc \frac{aob}{2} - (R - R_1).$$

Suppose, however, in substituting the 3-centre curve for the simple one, it is advisable for the points e and f to coincide as in Fig. 53.



1. Given R_1 and R_2 , we then have

$$ext{vers } uo_2c = rac{(R-R_1) ext{ vers } rac{aob}{2}}{R_2-R_1}.$$

Then a must be put back on the tangent to u, and

$$au = (R - R_1) \text{ vers } \frac{aob}{2} \left(\cot \frac{uo_2c}{2} - \cot \frac{aob}{4} \right).$$

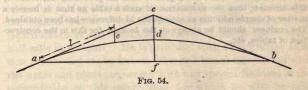
2. Given R_1 and uo_2c , we then have

$$R_2 = R_1 + \frac{(R-R_1) \operatorname{vers} \frac{aob}{2}}{\operatorname{vers} uo_2 c},$$

au being found as above.

VERTICAL CURVES.

100. We have already considered the dangers which arise from sudden changes of grade (see Sec. 29). Where these changes are considerable, amounting to, say, 0.5 p. c. in the difference of grade, it is advisable to round off the angle at the junction of the two grades by means of vertical curves. On bridge-work this should be more especially attended to. Theoretically, the curve which should be applied is a parabola, and this happens also to be the simplest form of curve to insert in practice.



In Fig. 54 let ac and cb be two grades between which it is required to insert a vertical curve.

Now cf = 2cd; therefore, if the letters a, b, and c stand respectively for the elevations at those points,

$$cd = \frac{c}{2} - \frac{a+b}{4},$$

and the correction e at any other point is given by the equation

$$e = \frac{cd \cdot l^2}{(ac)^2}.$$

ac and cb are usually made about 200 feet each.

Vertical curves are not usually inserted during location, or even shown on the location profile; but the corrections for them should be worked out before the cross-sectioning begins, and the grade as shown on the construction profile should be the corrected grade.

ownedness bound as above.

Note.-In dealing with deflection-angles and offsets of curves, the engineer-entirely ignorant of the Differential Calculus-may often save himself a considerable amount of labor by making use of the principle of Successive Differences, an application of which is given in Sec. 203, Part III. Thus, e.g., the deflection-angles given in Tables A and B, Sec. 97, may be calculated up to 300 feet merely by the application of the 2d differences, and may be extended considerably beyond that amount by using the 3d differences. More especially is this method applicable in calculating offsets to a curve which may be considered to vary as the Square of the tangential distance, for then their 2d differences will be constant. As an example of this, the values of $(H-H')^2 \frac{sL}{27\times 6}$, given in Sec. 130,—varying as the square of (H-H'),—have for their 2d difference 1.852, which does not change; therefore the differences of the differences of the values in the table increase regularly, the difference between any two values being greater than the preceding difference by this amount; thus the calculation of such a table as that is merely a matter of simple addition as soon as the 2d difference has been obtained. The engineer should be always on the lookout for this in the construction of tables, etc.

required formed a vertical edges.

Now of = 2nd, therefore, If the letters a, b, and a stand, respectively for the elevations at those polyte, b.

Part II.

he hads some describe tudication of the amount of flow or all

CONSTRUCTION.

101. THE Field-work of engineering during Construction may be divided into two parts, the first (A) dealing with the setting out of the work, and the second (B) with the estimating of the labor and material employed in its execution; and in this order it will be well to consider the subject.

A. THE SETTING OUT OF WORK.

102. An engineer, when given a subdivision of a road to look after during its construction, often finds merely the centreline staked out at every 100 feet,—with hubs indicated by Guard-stakes at the transit stations,—and bench-marks every half-mile or so apart. He is provided with a copy of the location profile and of the transit-notes and bench-marks, and with the notes and plans connected with any special features in the construction on his subdivision for which he will be held responsible—such as plans of bridge-sites, culverts, etc.

If in a timber country, the first thing he has to do is to see to the Clearing of the Right of Way, which he does by marking out the limits—if the clearing is to be carried to the full width—by blazing the trees at distances of a hundred feet or so apart on either side of the centre-line, and inscribing the letter C.

While the clearing is being done, he usually has time to examine the country along the line with an eye to the location of culverts and the size of openings necessary, and to make a closer examination of the probable classification of the cuts than the location party probably had the opportunity of doing.

103. In order to obtain a correct idea as to what size of openings may be necessary, he is guided by the flood-marks

along the water-courses; and if there is any doubt about these in the neighborhood of the line, he must follow them up until he finds some definite indication of the amount of flow, or else forms a more or less accurate estimate of it for himself, by an examination of its source.

In selecting the points for culverts and the sizes required, the engineer must bear in mind the effect of drainage upon the natural well-defined water-courses: for instance, water that before the construction of ditches ran more or less broadcast over the country,—as is frequently the case in low marshy land,—thereby perhaps in a dry season showing no indications of its existence at another time of the year, or which in a wet season may be simply indicated by a saturation of the soil, may, when conducted by ditches to the mouth of a culvert, present a very decided reality.

Often too, by cutting a small ditch, two streams can be brought together at a less cost than would be involved by the construction of two separate culverts. For a masonry culvert is an expensive article in the first place, and the usual substitute—a timber one—a still more expensive article in the long run. When the dump is low, open wooden culverts are the best to use as temporary expedients, for any defects in them are readily visible, and masonry culverts can be built to replace them with very little trouble. For small openings piping does admirably, but should be well bedded; as a temporary substitute for pipes, small plank culverts may be inserted, which may afterwards serve as a means of inserting the pipes themselves.

104. A thorough system of drainage along each side of the road-bed should be one of the first points to which the attention of the engineer should be given, for it is often possible to greatly decrease the cost of construction by constructing ditches some little time before the commencement of the work.

As regards the form and size of such ditches, it is usually sufficient to make them with slopes of 1 to 1, but with plenty of width in the base: as a rule, for each foot of water likely to be in the ditch there should not be less than three feet of base, and the rate of fall should be made as uniform as is compatible with the cost of construction. For small ditches, the rate of fall should not be less than 0.2 p. c. if possible; but a large ditch which is likely to have a depth of water of not less than

one foot will draw tolerably well with a fall of only 0.1 p. c. Neither should the fall be so great as to permit scouring to any large extent.

Small extra ditches are usually staked out with centre-stakes only, and the amount of excavation calculated from the centre-heights. But for larger ones slope-stakes should be set, and if the surface is irregular it must be properly cross-sectioned.

105. It is often the case that the cross-sectioning of the work has been done by a party detached from the main location party: if so, the engineer usually has time to check the benchmarks and insert new ones for himself at points which he may consider suitable. These B.M.'s should not be less than 10 stations apart; their positions should be such as to do away as much as possible with turning-points. They should be marked B.M., and the elevation of each inscribed on it. At each bridge-site there should be a bench-mark close at hand. It is a good plan also, if there is time, to check the alignment from the transit-notes. Any error discovered, either in the levels or the alignment, should be at once reported. For discrepancies arising in the checking of the alignment by using short chords, see Part I.

106. When, however, the subdivision engineer has the cross-sectioning to do himself, if the construction is being started at various points on his work almost simultaneously with his taking charge, he then has his time from the very first fully occupied in taking cross sections.

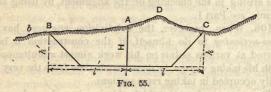
The amount of work which this involves depends a good deal on the manner in which the grading is to be measured. If measured in excavation only, then it is merely the cuts that have usually to be cross-sectioned; but if measured in cut and fill, both must receive equal attention. In the former case, where borrowing has to be done, it is often necessary, however, to have the fills also cross-sectioned, for, owing to the impossibility of measuring the borrow-pits correctly, the work may have to be measured in the fills, and this must be borne in mind at the time of cross-sectioning. Also, to obtain a correct estimate of the over-haul it is necessary to have the fill connected with it cross-sectioned. At all points, too, where the question of the distribution of material is likely to arise, cross-sections of the fills are useful, but these need not be taken with

the same accuracy as those required for the measurement of the work.

To cross-section *properly*, five men are wanted besides the engineer,—namely, a rodman, a man to carry stakes, another to drive them and another to mark them, and a tapeman,—for though the *setting of slope-stakes* is sometimes done separately from the cross-sectioning, it usually saves both time and expense to do both at once.

Before starting to cross-section, the engineer will do well to construct a small table for each different width of road-bed and set of slopes which he is likely to use, giving the "distances out" to the slope-stakes for various amounts of side-heights. For though he rapidly acquire these after a little practice,—and should be checked in his calculations of them by the rodman,—still, by having a table before him, he saves considerable mental work and insures greater accuracy. He should also be provided with a small scratch-block.

The best way to explain the method of cross-sectioning is by means of an example.



Let bBAC, in Fig. 55, represent a surface which we wish to cross-section. We first take the elevation at the centre A, which should correspond within a tenth or so with that given on the location profile. By subtracting the grade at the station from this elevation we thus have H, the centre cut at A. The rodman then goes to the left and holds the rod at some point b near where he judges the slope-stake will come. If on obtaining the side-height for b it is found that the proper distance out from A for this height does not agree with the distance out as actually measured, other points must be tried until a point is obtained, such as B, where these two correspond. An error of only a few tenths in distance can be estimated for by eye without taking a separate reading to correct for it, so that two or three trials are usually all that are required to fix the

position for the slope-stake; and on comparatively level ground the point can be usually hit off by a good rodman at the first trial.

Similarly on the right the point C must be fixed.

If there are any decided irregularities in the surface, such as is represented at D, the elevations of such points must also be taken.

The following rules give all that is required as regards the actual levelling:

1. When H.I. is above grade.—If the rod-reading exceed the difference in elevation of the H.I. and Grade, the excess = the fill; but if it is less, the deficiency = the cut. Consequently, when the rod-reading = the difference of H.I. and Grade that point is a Grade-point.

2. When H.I. is below Grade, the rod-reading + the

difference of H.I. and Grade = the fill.

Cut is always indicated by a positive, and Fill by a negative sign.

The following is a good form for keeping the notes:

Sta.	L.	C.	R.	B.S.	F.S.	н.г.	Elev.	Grade.	Re- marks.
1020	0.0 7.0	+1.0	$\frac{+3.0}{14.5}$ $+3.3 + 1.0$	lassi.	1.3	102 30	101.0	100.00	grade 14' in n cut.
1021	$\frac{-1.0}{8.5}$	0.0	6.0 11.5		1.3		101.0	101.00	dbed 20' i es 1
1022	$\frac{-3.0}{11.5}$	- 2.0	$\frac{0.0}{7.0}$	eiche Code	2.3	tualia	100.0	102.00	Roa fill,

There is no need to work out the elevations in the field, but so doing in the office afterwards forms a useful check on the work, since H.I. — F.S. (which of course is the elevation) should agree within a tenth or so with the sum of grade \pm centre-height, F.S. representing the rod-reading at the centre. We see from the above that it is the Difference of H.I. and Grade which is the foundation of the calculation at each station, and this, when worked out for the next station after a turning-point, can be modified for the succeeding stations by merely adding or subtracting the difference in grade. Thus the calculation is simpler than it at first appears from the above rules.

The slope-stakes should be marked S.S. on the outer sides

and the numbers of the stations on the inner. The centrestakes should have the cut or fill marked on them.

As to the points at which cross-sections should be taken, the rodman in selecting them should bear in mind that it is not necessarily the highest or lowest points that are required, but those points which, when joined by straight lines, will give the contents as nearly as possible equal to the true volume. It is impossible as well as unnecessary to take account of many of the small irregularities which occur, but by a judicious selection of points these may to a considerable extent be made to counteract each other. Where the contents are calculated by "average areas"—as is usually the case—we can easily find from Sec. 130 what limit should be adopted as regards the difference in centre-heights and widths between the slope-stakes of two cross-sections, in order that the error in the volume as calculated shall not exceed a certain amount. For exact work a difference of two feet between the centreheights of two adjoining cross-sections is about the limit which should be allowed; but in ordinary practice we may say that a cross-section should be taken every 50 feet when the difference in centre-height amounts to about 5 feet. This is, of course, mainly to reduce the errors which arise from using an approximate method of calculating the quantities, and not to take into consideration the irregularities of surface. To counteract as much as possible these latter, judgment in the selection of the cross-sections has a better effect than labor spent in obtaining a large number of cross-sections a few feet apart. They should also be taken whenever "grade" occurs on either the edge of the road-bed or in the centre; and whenever a cross-section is taken where a grade-point falls in the road-bed its position must be obtained. For if a grade-point is the only point obtained at any station, it necessitates assuming centre- and side-heights afterwards in working out the contents, in order to make use of that grade-point, so that it is much more satisfactory-and in the end involves no more work-to obtain these heights by direct measurement.

There is of course no need to take cross-sections any closer together on a curve than on a tangent, as may be easily seen from Sec. 134.

When in doubt as to the material in a certain cut, i.e., as to whether it is earth or rock, etc., it is best to cross-section it

for the usual earth-slopes and have it stripped to that width in one or two places; if then rock is encountered in a solid bed, the rest of the cut may be cross-sectioned for rock, and as soon as the rock is reached the earth trimmed off to its proper slopes before the rock is worked. This of course necessitates a cross-sectioning of the rock-surface as well as of the original ground-surface, and these cross-sections should be taken at the same stations, so as to facilitate the calculation of the respective volumes of earth and rock.

107. The referencing of the P.C.'s and P.T.'s is a part of the engineer's work which must also be attended to before construction begins. Reference-points should be placed, two on each side of the alignment, at angles of about 45° with it, and sufficiently distant to be free from all chance of disturbance during construction; the point referenced thus lies at the intersection of the two lines joining the opposite points. Sometimes, however, especially on side-hill work, it is necessary to place all the reference-points on one side of the track, in which case the apex of the angle formed by the lines passing through each pair of reference-points is the point referenced. Each reference-point should be marked R.P. on a guard-stake set beside it, and the magnetic bearings and distances of the points entered in the notes.

108. The Staking out of Borrow-pits consists in driving stakes at the corners of the proposed pits, and obtaining elevations of the ground-surface so as to form the upper line of a set of parallel cross-sections of the pit, the lower line being obtained by taking levels immediately under those taken on the surface, when the excavation is completed. In order that the bottom levels may be properly connected with those taken on the surface, reference-points must be established. The simplest way of doing this is by driving hubs, say 10 feet back from the edge of the pit, in the line of each cross-section. By taking the cross-sections 27 feet apart, as is often done, there is some little labor saved in calculating the contents, since the mean of any two cross-sections in square feet equals the volume between them in cubic yards.

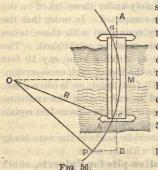
A sketch plan of each pit should be made in the note-book, and properly lettered to accord with the notes.

109. Staking out Foundation-pits for Culverts, either masonry or timber, consists of setting stakes at the corners as

given by the foundation plan and marking on each stake the cut necessary. A sketch of each pit should be made in the note-book, and of course the amount of cut at each stake recorded. When the foundation consists of timber, the pit should be low enough to insure the timber being at all times, if possible, kept under water, or at any rate moist; about 18 inches is the average depth for foundation-pits for wooden culverts on Railroad work. In staking out, it should also be remembered that the culverts should not have a fall of more than, say, 1 in 10, so that when the ground slopes transversely to a greater extent than this the culvert must be put on the skew so that its inclination will not exceed this amount. If the depth of the foundation-pit exceeds 4 or 5 fect, it should be staked out a foot wide all round to allow room for working.

110. Setting out Bridge-foundations.—When a bridge is on a tangent there is no difficulty about staking out the foundation-pits, that needs particular mention. The work is usually best done with a transit and tape from the centre-line,—an optical square comes in very handy for this,—the offsets being obtained by scale or otherwise from the foundation plan. In this way there is less liability to make an error than in any other, since each point is set out independently of the previous ones. When the material is not likely to stand vertically, it should be given a slope sufficient to warrant its stability. If there is not room to admit of this, then of course the sides must be shored-up in some way,

When, however, the bridge is on a curve, if the span is



short, it is from the tangent at the centre of the bridge that the offsets must be set off. In dealing, however, with bridges of comparatively long spans, the centre of the curve on the bridge will by no means coincide with the centre of the structure, as is shown by Fig.

Now AB will be the centreline of the bridge, where $cb = \frac{1}{2}$ ordinate at M to ab

(see Equation 23, Sec. 80); so that the true centres of the piers

lie considerably outside the centre-line at those points. If any pier, as c, is inaccessible, c (its centre) may be located as follows:

In the centre-line of the track take some accessible point P, and set off PB perpendicular to AB, making

$$PB = R \text{ (vers } POM - \frac{1}{2} \text{ vers } bOM);$$

then will

$$Bc = R\left(\sin POM - \frac{ab}{2}\right)$$

C may then be located either by direct measurement from B, or by intersection.

In setting out bridge-foundations great care should be given to a thorough system of referencing all important points, and the reference-points must be so selected as not to be obstructed by staging or scaffolding during the progress of the work.

111. Setting out Trestlework.—In locating the position for the piles in low pile-bents, it is sufficient to locate the centre of each bent and then set off the positions for the piles by measuring out from the tangent at the centre, finding the angle by eye; if possible, the position of each pile should be marked with a stake.

When piles are being driven on a curve by a floating piledriver, in water too deep to drive stakes, the centre of each bent must be given by the intersection of the lines given by two transits, as in Sec. 76.

If, however, the trestle is on a tangent, by placing pickets on either bank in line with each row of piles the centre for any pile can be given without the aid of an instrument; or pickets can be so set that the pile-driver can line itself in without the assistance of any one on the bank; the distances between the bents may be taken by measurement from one bent to the next. In the case of framed bents resting on sills, it is advisable to have the sills brought to a solid foundation at about an indicated elevation before the framing-bill is made out; in this way a firmer foundation is often obtained at a cost of less labor than if the exact elevation for the sills was prescribed. The sills for each bent should then be accurately levelled and centred.

In dealing with high trestles, the transverse centre-line of

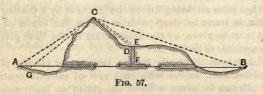
each bent should be referenced, the reference-points being at a considerable distance from the bent itself, so as the better to permit the line being carried to a high elevation in the structure if required. The length of the chords should be corrected according to Sec. 76.

Where pony-bents are used they should be so skewed around as to conform with the contour of the ground; they must be accurately levelled before the sills are laid on.

In giving points for "cut-offs" in piling out of reach, the pile should be blazed and a tack driven into it, the distance above the tack—which should be in full feet—being inscribed. The position of the tack is best found as follows: For example, let the difference of H.I. and grade = 6.11 fect; then if the point of cut-off is 2 feet below grade, and it is wished to put in the tack so as to read "5 feet below cut-off," we must read on the rod 0.89 foot. The position of the tack is then at the foot of the rod.

112. Setting out Tunnels.—This is work which often needs considerable time and care, in order that the results obtained may be satisfactory.

Let Fig. 57 represent the section of a tunnel in course of construction.



The first thing to do is to establish some point C in the alignment from which a good view—if possible—may be had of the mouths of any shafts which it may be required to sink, and also of two distant points A and B, also in the same straight line. If the instrument is then set up at C and the telescope clamped on to A, on reversing it the point B should be intersected. By repeated trials the three points A, B, and C are then established in the same straight line, and these points should be permanently marked.

In order to obtain the centre-line of the tunnel, say at the left end, another point G in the same line as AB must be

given, and the centre-line is then obtained by the production of AG.

But suppose the work is to be carried on also from one or more shafts as EF, then the alignment has to be "dropped" from ED to the elevation of the tunnel at F, and in this operation the greatest care is necessary. There are three or four ways in which this can be done, but the following is that usually adopted for tunnel-work, as it admits of greater accuracy than the others, which are more suitable for simpler mining operations:

Two instruments such as that shown in Fig. 58 should be firmly bolted on either side of the shaft as *D* and *E*, and near to its edge, both being lined in vertically over the centre-line of the tunnel.

Each instrument consists of a plate p—with a narrow vertical slit in it and scale s attached—which can be moved sideways by means of the screws a and b, so that it can be set to

any desired reading on the scale—
the scale being read by a vernier
v attached to the main body of the
instrument. Having set these two
instruments approximately in line,
then, by a series of observations
taken at different times,—so as to
counteract as much as possible the
varying conditions which affect
each separate sight,—ascertain for
each instrument the mean of the

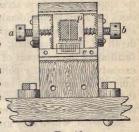


Fig. 58.

readings. Having then set the plates to give that reading, the centres of the vertical slits coincide with the mean alignment.

Two fine steel wires must then be carried from one slit to the other, each being placed against the vertical edge, so that they form two parallel lines, close together, across the shaft, one on each side of the alignment. Midway between these two wires, and as near to the edge of the shaft as possible, but on opposite sides of it, two fine copper wires should be passed, long enough to reach down to the tunnel at F, and to the ends of these two heavy plumb-bobs should be attached. The wires should be enclosed in wooden tubes to protect them from currents of air, falling water, etc. The plumb-bobs themselves should be immersed in buckets of water to lessen their oscilla-

tions. Scales should then be placed so as to read these oscillations slightly above the plumb-bobs. The mean of these sets of readings then gives a point on the alignment, and from the two points so obtained the centre-line of the tunnel may be extended in either direction by first establishing a point in one direction, and then in the other; and these points can then be checked by observing whether all four are in the same straight line: if found to be correct, they should be permanently established. The levels may be dropped by means of a steel tape, with which the levelling-rod used has been previously compared.

The length of the tunnel may be found either by direct measurement (breaking-chain) or by triangulating.

In locating a tunnel, it should be remembered that it is usually cheaper to open a cut at depths under 60 feet than to bore. In many clays, however, a cut of this depth would be barely practicable owing to the increase in the inclination of the slopes necessary on account of the depth itself, and in such cases the limit is considerably less than this. As regards the advisability of sinking shafts, it is mainly a question of the depth of shaft required, the need of ventilation, and the facilitating the transport of material. Where the depth is not excessive it is usually policy to sink several shafts in a long tunnel, and work from each independently, for the work is thereby considerably hastened, and after its completion the shafts themselves form admirable means of ventilation.

Side-drifts, where they are possible, accomplish the same results as shafts, and are usually to be preferred to them on account of less risk to life and property during construction, and their convenience afterwards.

Where the alignment has not to be carried to any great distance from the points dropped to the bottom of a shaft as above described, it is better to sink the shaft a few feet on one side of the centre-line, and to reach the tunnel from it by means of a cross-heading.

The centre line in the tunnel is best given by points on the roof from which plumb-lines can be hung when required.

113. Giving Grade and Centres forms a very large portion of the work to be done by the engineer during construction. The giving of "grade" may be greatly facilitated by having stakes driven to grade, from which at any future time

the levels may be given with a hand-level—an instrument highly useful during railroad construction. To have to carry a heavy level for several miles just to give grade at two or three stations, as is frequently done, is absurd. By having a bubble-tube attached to the telescope of the transit a considerable amount of trouble may also be saved, and with it the elevations can be given quite as correctly as are ever required on a railroad dump.

In setting grade-stakes, allowance must be made in dealing with material which is likely to shrink in order to allow for it. The amount of the Shrinkage depends considerably on the pressure to which the material is subjected, consequently on the height of the fill: as an average, however, in earthy soils the linear contraction is about 10 p. c., so that a 10-foot fill should be "put up" I foot above grade. In dealing with wet or frozen soils greater allowance should be made, but with dry sandy material, less.

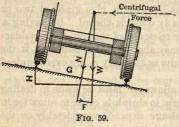
The allowance also depends very largely on the manner in which the dump is constructed. A dump well trodden by horses usually shrinks very little, and in many such cases there is no need to allow for shrinkage at all; but where the work is put up by tipping or shovelling, double the allowance may in some cases be none too much.

The increase in bulk in rook, as well as the shrinkage of earth, necessitates an allowance being made when arranging for the distribution of material. A good general rule for this is, that 10 yards of earth in excavation make 9 yards in embankment, and 10 yards of rock in excavation make 17 yards in embankment.

As regards "giving centres" during construction, it should be seen that the slope-stakes are intact, and then by their means the centres for a cut or fill may be usually obtained from the cross-section notes, without the trouble of setting up the transit, with accuracy quite sufficient to enable the contractor to proceed with his work.

114. Difference of Elevation on Curves.—The centrifugal force brought into play by the inertia of the train when going round a curve must be counterbalanced by a more or less equal and opposite force in order to prevent the flanges of the outer wheels being pressed too severely against the rails. The simplest way of bringing a counteracting force into play

is to make use of a component of the weight itself, which



the track as in Fig. 59.

Thus, if the force W, representing the weight of a car, be resolved into its rectangular components N (normal to the track) and F (parallel to the track), we see from Sec. 7 that F is propor-

tional to $\frac{H}{G}$, H being the difference in elevation of the rails, and G the gauge—or more strictly, the distance from centre to centre of rails. Now the value of the centrifugal force in pounds equals $\frac{v^2}{32R}$, where v= velocity in feet per second, and R the radius of the curve; so that when there is no tendency to tip over on either side—if we assume, as we may well do in practice, that F is the component parallel to the centrifugal force—we have

$$\frac{H}{G} = \frac{v^2}{32R}$$
; therefore $H = \frac{Gv^2}{32R}$.

So that, substituting for R the value given in Sec. 71, and substituting V, velocity in miles per hour, for v, we have

$$H = .00067 \ GV^2 \sin D$$
;

or, as an approximate formula, easy to remember, we have

$$H = \frac{GV^2}{15R}$$
 (nearly).

If we take $G = 4' 8\frac{1}{4}$, we then have

$$H = .0032 \ V^2 \sin D$$
.

The following table, abbreviated from that given by Mr. Searles, calculated for the value of F parallel to the centrifu-

gal force, and for a distance from centre to centre of rail $=4'\,10^{\alpha''}_4$ (suitable to the $4'\,8^{\alpha''}_4$ gauge), gives the difference in elevation of the two rails in feet, at various speeds for different degrees of curvature.

Vel. in				I	EGREE (of Curv	E.			
m. p. h.	1°	20	3°	4°	5°	6°	70	90	12°	16°
10	.006	.011	.017	.023	.029	.034	.040	.051	.069	.091
20			.069		.114	.137	.160	.206	.274	.365
30	.051	.103	.154	.206	.257	.308	.359	.460	.611	.809
40	.091	.183	274	.365	.455	.545	.634	.811	1.069	_
50	.143	.285	.427	.568	.707	.844	.979	071	\$ mind	2
60	.206	.410	.612	.811	1.006	1.196	-	-	1-	_

A convenient rule, much used in practice for a gauge of 4' $8\frac{1}{2}''$, is, that the difference in elevation equals one half-inch for every degree of curvature.

In order to allow for the difference in elevation on the dump, the road-bed should have its outer edge higher, and its inner edge lower, than grade. To allow for it on trestles, whether in pile-bents or framed bents, the posts must be cut so as to give the required inclination to the cap on which the stringers rest: the batter of the batter-posts and the verticality of the upright posts remain unchanged.

It is usual to adopt a difference in elevation in the rails suitable to the mean speed of the trains which pass over them: the consequence of which is, that the rails on both sides get worn, but in different ways-the outer ones by the fast trains and the inner ones by the slow trains. The coning of wheels, which was at one time largely resorted to, is rarely used now on account of the increased oscillation and concussion (see Sec. 4) to which it gave rise, so that the flanges of the wheels, by means of their pressure against the inner sides of the rails, have themselves to keep the balance between the centrifugal force and the component of gravity which is set to counteract it, more or less. In curves uneased by transition curves, the difference in elevation at the P.C. and P.T. must be at least equal to what it is at any other part of the curve, so that it must begin some little distance back on the tangent and increase gradually until it reaches its maximum at the P.C. or

P.T., as the case may be. For a 3° curve it is usually sufficient to begin the difference in elevation about 100 feet back, and for a 10° curve about 200 feet back on the tangent. When transition curves are used, they must be treated with a difference in elevation at all points more or less suitable to their curvature; but where the transition curve is merely a simple curve inserted to ease the approach to a sharper one, the difference in elevation for the terminal curve must begin back on the tangent as above, and for the main curve some little distance back on the terminal curve, so as to admit of its reaching its maximum at the P.C.C.

It is usual to slightly increase the gauge on curves, generally

by about 1' for every degree of curvature up to 5°.

115. Inspecting the Grading.—The engineer should, if possible, pass over every portion of his subdivision at least twice a week, and the oftener the better. In open country there is comparatively little chance of having the dump badly put up owing to lack of supervision, except perhaps through the use of a superabundance of "sods;" but in timber country where there is plenty of grubbing to be done, and the work is largely let as "station-work," the engineer must be constantly on the lookout for the presence of roots and stumps in the dump. In winter too, snow, frozen moss, etc., at the bottom of a fill serve admirably as a temporary means of bringing it up to grade. He should see that there is a fair line of stumps at the side of the track after the completion of the work in places where grubbing has occurred, or that they have really been burnt; and when there is snow on the ground he must have it swept well to the side before the filling is begun. He must see that the ditches on either side of the embankments. etc., as well as those in the cuts themselves, are taken out properly, and thoroughly cleared of all obstructions, that the slopes are neatly dressed off and well out to the slope-stakes. For the final inspection of the road-bed, grades and centres must be carefully run, and the width tested wherever it appears lacking. All litter along the side of the track must be cleared away or burnt, and anything in danger of falling on to the road-bed removed. About this latter injunction the engineer cannot be too careful, and when in doubt as to the stability of a piece of rock or an overhanging tree, he should have it removed at any cost. He must also remember that a rock or tree which at the time of inspection looks tolerably firm, may be a considerable source of danger after the disintegrating effects of a hard winter, or a season of heavy rains, and that it costs very much less to have it removed during construction than at a later period.

116. Running Track-centres and setting Ballast-stakes.—Where the ballasting is done before the track is laid, ballast-stakes must be driven every 50 feet, so that their tops indicate the elevation of the top of the ballast. They should be placed on either side of the centre-line at the foot of the ballast-slopes. Centre-stakes should also be set every 100 feet apart on tangents and every 50 feet apart on curves, to guide the track-layers; tacks should be inserted in them.

When the track is laid without first ballasting, a line of centres must be given before the track is laid, and usually afterwards as well, to guide the surfacing gang, for the centres previously put in are almost sure to have been knocked out in laying the track.

It sometimes happens in hasty work that the engineer who has the track-centres to run cannot get his centres to coincide with the centre of the dump or with the centres of the bridges. As regards the centres on the dump, he must use his own judgment as to what is best to do: if it is clear that the dump is out of line, he must stand by his own centres; but if otherwise, it is usually better for him to increase or ease his curvature a little, so as to make it conform with the centre of the road-bed. On bridges or open culverts he must make his own centres fit the centres of the structures, and if this cannot be done without seriously affecting the adjacent track, the case must be reported at once.

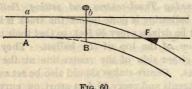
117. Permanent Reference-points.—After the track is laid, large hardwood stakes—or better still, stone monuments—should be set to mark the P.C.'s, P.C.C.'s, and P.T.'s. They should be placed on the outer side of the curves, at right angles to the track, usually about 5 or 6 feet from the centre.

TURNOUTS AND CROSSINGS.

118. In dealing with the subject of turnouts and crossings, we will assume that the Common Stub Switch is used, since it

is the simplest, and the formulæ for it are readily applied to any other form of switch.

Let Fig. 60 represent a turnout from a straight track, A and a forming the "heel" and B and b the "toe" of the switch.



Then if

G = gauge,

N = number of the frog.

F = "Frog angle,"

= Angle of Intersection at F.

R = radius of turnout curve,

AF = frog distance,

AB = length of switch-rail,D =degree of curve.

we have

$$N=rac{\cotrac{F}{2}}{2}$$
, $anrac{F}{2}=rac{G}{AF}$, $AF=2GN$, $AF=\left(R+rac{G}{2}
ight)\sin F$, $R=2GN^2$, $R=\left(AF\csc F
ight)-rac{G}{2}$, $AB=\sqrt{4GN^2 imes \mathrm{Throw}}$.

The throw according to Sec. $78 = \frac{AB^2}{2B}$.

The number of a frog may of course always be found by measuring the tongue: thus if at a certain point we find its width to be 5 inches, this divided into the distance of that point from the theoretic point of the tongue gives the number of the frog; thus if that distance were 4' 2", it would be a No. 10 frog.

The following table gives these values for a gauge of 4' 8½" and a throw of 5".

N	F	AF in feet.	R in feet.	D	AB in ft.
4	14° 15′	37.66	150.66	38° 46′	11.2
5	11° 25′	47.08	235,40	24° 32′	14.0
6	9° 32′	56.50	338.98	16° 58′	16.8
7	8° 10′	65.91	461.38	120 27'	19.6
8	7° 09′	75.33	602.62	9° 31′	22.4
9	6° 22′	84.74	762.70	7° 31′	25.2
10	5° 43′	94.16	941.60	6° 05′	28.0
11	5° 12′	103.58	1139.34	5° 02′	30.8
12	4° 46′	112.99	1355.90	40 14'	33.6

This table may be applied to other gauges; F of course remaining unchanged, AF and R will vary directly as the gauge; D will, of course, vary inversely as R. Thus for a 3-foot gauge and a No. 9 Frog we must multiply the above values of AF and R by $\frac{3.000}{4.708} = .637$; and the above value of

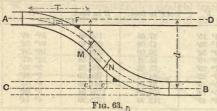
D must be multiplied by $\frac{4.708}{3} = 1.57$. AB is of course dependent on the value of the throw adopted.

119. Suppose, however, that the turnout instead of starting from a straight track, as in Fig. 60, starts from a curve as in Figs. 61 and 62; then we may assume that when the main curve and the turnout curve are both in the same direction, that the case, as regards the position of the frog, etc., is equivalent to a turnout from a straight track, the curvature of the turnout curve being equal to the difference of the curvature of the main and of the turnout curve; and if in opposite directions, then the curvature of the turnout curve may be taken as being equal to the sum of the curvatures.



Suppose we have two parallel tracks AD and CB, as in Fig. 63, which we wish to join by a crossing; or, having the track AD only, we wish to insert a turnout AB which shall connect the side track B with the main track AD. Since the former case differs only from the latter in the fact that the dotted

portion C, with the accompanying frog, is omitted, the two cases may be treated together as follows:



Starting from the centre-line AR with a given frog number, we select a certain length n, expressing the length of the branch AM in terms of 100-foot stations. The length of the offset t at M is then given, according to Sec. 78, by the formula

$$t = R \text{ vers } nD$$
,

and the distance along the track AD to this offset equals

$$T = R \sin nD$$
.

Thus by setting off the offset t at a distance T along the tangent from A, we locate the point M. The position of the frog at F is found by taking from the above table the value of AF, and measuring it off along AD, offsetting F by an amount equal to half the gauge.

Another offset $y = \frac{1}{4}$ gauge may also be set off at a tangential distance $= \frac{1}{2}AF$. These points, together with the toe of the switch, are usually all that are wanted in the curve AM. The length of any other offset, if required, may be found from Sec. 78.

The offset t is then produced across to the centre of the other track (or the other track produced) and—assuming both branches to have the same radius—the offset Ne = t is set off from the point e, which point is found from the formula

$$ce = (d - 2t) \cot nD$$
.

We thus have the point N. The curve NB is then located by using the same value of T, and the same offsets as before, only of course in reverse order.

By obtaining n from the formula

vers
$$nD = \frac{d}{2R}$$
,

which gives its limiting value, we have a simple reverse curve

without the intervening tangent MN: but this is bad practice when it can be avoided.

Should the radius of NB be required different from that of AM, the tangential distance for NB must then be calculated afresh.

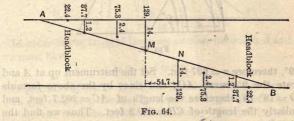
The advantages of this method are, that any length of intervening tangent can be used,—provided that the curves are carried up to the frogs,—so that the engineer can select any value of n for himself; and with simply a tape, he can locate the crossing in a manner a good deal simpler than the ways ordinarily in use.

120. As an example, let d=40 feet and let No. 8 frogs be used; and suppose we select 1.3 as a value for n. Then from the table, AF=75.33, R=602.62, and $D=9^{\circ}$ 31',—the gauge being 4' $8\frac{1}{2}$ ".

Then from the above formulæ we have

$$nD=1.3 \times 9^{\circ} \ 31'=12^{\circ} \ 22',$$
 $t=602.6 \times \text{vers } 12^{\circ} \ 22'=14 \ \text{feet},$
 $T=602.6 \times \sin 12^{\circ} \ 22'=129 \ \text{feet},$
 $ce=12 \times \cot 12^{\circ} \ 22'=54.7 \ \text{feet},$
and $v=1.2 \ \text{feet}.$

The notes for the setting out of the crossing may then be arranged as follows:



When the distance between the two tracks is great, the crossing should be run in with a transit.

- 121. If the turnout or crossing falls on a curve, it is best to locate it with a transit according to one of the two following methods:
- 1. If the curvature of the main track is tolerably sharp and the distance d between the centres of the two parallel tracks comparatively small, we can avoid the insertion of a reverse curve without materially lengthening the crossing as follows:

In Fig. 65 let D = the degree of the turnout curve AC, R = radius of the outer track A, and r = radius of the turnout curve AC

The length of AC may then be found in terms of nD, thus:

$$\text{vers } nD = \frac{d}{R - r};$$

and the length of the tangent equals

$$CB = (R - r) \sin nD$$
.

For example, let the outer track A be on a 4° curve; then R = 1433, and let d = 40 feet, and the given frog number for the main curve = 11.

Then, according to Sec. 119, D for the turnout curve must be that value which is required to make the difference in curvature of the track A and the curve AC equal about 5°, both curves being in the same direction; and since this value

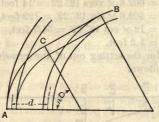


Fig. 65.

is 9°, therefore r=637 feet. Set the instrument up at A and locate the 9° curve AC; and since by the above formula $nD=18^\circ$ 15′, therefore the length of AC=202.7 feet, and similarly the length of CB=249.2 feet. Thus we find the point B.

To run from B to A would be simply a reversal of the above. The frog for the track B will of course be that suitable to a turnout radius equal to the radius of the track B.

But suppose this method would in any particular case cover too much ground, or be unsuitable in some other respect, we can then use the following one, which, though involving the use of a reverse curve, is well enough for station-yards, etc., where no high speeds are attained. In Fig. 66 let R = radius of the inner track B,
 r = radius of branch CB,
 r₁ = radius of branch AC.

Then

vers
$$BHC = \frac{d\left(R - r_1 + \frac{d}{2}\right)}{(R + r)(r + r_1)}$$
,

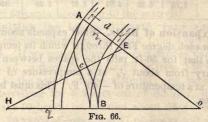
from which we can find the length of the branch BC; and

vers
$$BOA = \frac{d\left(r-r_1-\frac{d}{2}\right)}{(R+r)(R+d-r_1)};$$

and since the angle

$$AEC = BOA + BHC$$
,

we can thus find the length of the arc AC, and locate the crossing with the transit, starting from either end A or B.



In order to use frogs of the same number for tracks A and B, we must have

$$r = r_1 + d$$
 (nearly).

The positions of the frogs may be found according to Sec. 119. In the case of a *Double Turnout* the engineer can, by applying the formulæ given above, always locate it with accuracy sufficient for ordinary purposes, without the aid of special formulæ. The length of switch-rails given in Table in Sec. 118 are the *proper* lengths for a 5" throw, but in practice a difference of 5 feet or so in the length of the rail will be of very little importance. In the same way there is no necessity for the frog to have exactly the number which it should have according to the table. The laxity which is allowable in these matters depends on the speeds at which the trains are likely to pass over the switch.

122. Curving Rails.—The following table gives the midordinates in inches for curves of various lengths. Rails should also be tested for *Uniformity of Curvature* by testing one half of their length for ½ of the mid-ordinate. (See Sec. 80.)

	LENGTH OF RAILS IN FEET.											
Deg. of Curve.	30	28	26	20	18	14	10					
CORVE	In.	In.	In.	In.	In.	In.	In.					
1°	.240	.192	.156	.096	.072	.048	.024					
20	.456	.408	.348	.204	.168	.096	.048					
30	.696	.612	.528	.312	.264	.144	.072					
40	.948	.828	.720	.420	.348	.216	.108					
50	1.19	1.03	.888	.528	.420	.264	.132					
60	1.40	1.22	1.06	.624	.504	.312	.156					
70	1.64	1.44	1.25	.732	.588	.360	.180					
80	1.90	1.64	1.43	.840	.672	.408	.204					
100	2.35	2.05	1.78	1.04	.852	.540	.264					
120	2.83	2.47	2.15	1.26	1.02	.636	.312					
140	3.30	2.87	2.48	1.46	1.19	.732	.360					
160	3.76	3.28	2.83	1.67	1.36	.840	.420					

123. Expansion of Rails.—Steel expands about 1 part in 150,000 for each degree Fah. through which its temperature is raised; so that for 30-ft rails the spaces between their ends should vary from about $\frac{1}{16}$ " at a temperature of 120° F. to about $\frac{5}{16}$ " at a temperature of -40° F. This must be carefully attended to.

B. THE ESTIMATING OF LABOR AND MATERIAL.

124. The Expense of Grading is of course almost entirely dependent on the cost of the labor expended on it, the value of the material not entering into the question; so that estimating the cost of it is simply a matter of ascertaining the time and wages which are absorbed in its execution.

The following notes on the subject of handling earth and rock, which are taken from Trautwine on Excavations and Embankments,—than whom possibly no better authority could be quoted,—serve to show the relative cost of the different processes through which the material has to pass before being finally disposed of in the embankment; and, consequently, from them the aggregate cost may be obtained with a greater or less amount of precision. These processes we will consider in the order in which they occur, taking as the standard of

wages \$1.00 per working day of 10 hours, and the expense of a horse as \$0.75 (including Sundays).

A. THE COST OF EARTHWORK REMOVED BY CARTS.

1. Loosening the Earth ready for the Shovellers.— A two-horse plough, with two men to manage it, will loosen about 250 yards per day of strong heavy soil, about 500 yards of common loam, or about 1000 yards of light sandy soil; thus the cost of loosening these materials per cubic yard will respectively be about 1.5 cents, 0.8 cent, and 0.4 cent—i.e., assuming the total cost of the plough and men and horses connected with it to be about \$3.87 per day. When a four-horse plough is needed, as in dealing with stiff clays or cemented gravel, the cost runs up to about 2.5 cents per cubic yard.

Loosening by picks costs about three times as much as by ploughs, where the latter can work to advantage. The amount which a man can loosen with a pick in a day varies from

about 14 to 60 yards, according to the material.

2. Shovelling the loosened earth into carts.—The shovellers are usually actually at work from 5 to 7 hours out of the day. If we assume that each cart carries, as a working load, ½ cu. yd., a shoveller can load it in from 5 to 7 minutes, according to the nature of the material; and suppose he is actually shovelling for 6 hours out of the day, then in the course of the 10 hours he handles about 24 yards of light sandy soil, 20 yards of loam, and 17 of heavy soil at the cost of 4.2 cents, 5 cents, and 5.8 cents, respectively.

3. Hauling away the earth, dumping and returning.

—The average speed of horses when hauling is about 200 feet per minute, so that every 100 feet of *lead* occupies about one minute; dumping and turning occupies about another 4 minutes; so that the number of trips per cart per day equals

$$N = \frac{M}{4 + L},$$

where M= number of minutes in the working day (here 600) and L= length of the lead in terms of 100 feet. Then $\frac{1}{2}N$ equals the number of cubic yards moved by each cart per day; and $\frac{1}{8}N$, divided into the total expense of the cart per day, gives the cost of hauling per cubic yard. Assuming that one driver attends to four carts (doing nothing else), the total cost per cart may be set at \$1.25 per day.

4. Spreading on the embankment.—The cost of this varies considerably, but may be said to average about 1½ cents per cu. yd. When the earth is dumped over the end of the embankment, or is "wasted," ½ cent per cu. yd. should be allowed for keeping the dumping-places clear.

Keeping the hauling road in good order.—This is an item highly expensive if neglected, but if well looked after, $_{10}^{1}$ cent per cu. yd. per 100 feet of lead is usually sufficient to

cover it.

Wear and tear of tools.—"Experience shows that 1 of a cent per cubic yard will cover this item." This also includes the interest on the cost of the tools.

Besides the above, 1½ cents per cubic yard should be added to cover the cost of *superintendence and water-carriers*, and about ½ cent for extra trouble in ditching and trimming up.

As regards the profit to the contractor, it may be set down as from about 6 to 15 per cent, according to the magnitude of the work and the risks incurred; out of this he usually has to pay the clerks, store-keepers, cost of shanties, etc., but these as a rule cover their own expenses.

The following table gives the cost, exclusive of profit to the

Lead in feet, per 50 100 200	7 day per cart. 44.4 40.0 33.3	Light sandy soil. 10.4 10.8 11.5	Common loam. 12.2 12.5	Strong heavy soil.	Stiff clay or cemented gravel.
100 200	40.0 33.3	10.8			
200	33.3		12.5	140	4 - 0
		11 5		14.0	15.0
200	00 0	11.0	13.2	14.8	15.8
300	28.6	12.2	14.0	15.5	16.5
400	25.0	12.5	14.7	16.2	17.2
600	20.0	14.4	16.1	17.7	18.7
800	16.7	15.8	17.6	19.1	20.1
1000	14.3	17.3	19.0	20.6	21.6
1200	12.5	18.8	20.5	22.0	23.0
1400	11.1	20.2	21.9	23.4	24.4
1600	10.0	21.7	23.4	24.9	25.9
1800	9.1	23.1	24.8	26.3	27.3
2000	8.3	24 6	26.3	27.8	28.8
2500	6.9	28.2	29.9	31.4	32.4
3000	5.9	31.8	33.5	35.0	36.0
4000	4.5	39.0	40.8	42.3	43.3
5000	3.7	46.4	48.1	49.6	50.6

contractor, of earth when ploughed and spread in the embank. ment. When loosened with picks, from 1.3 to 4.5 cents per cu. yd. should be added to the values given, according as to whether the material is of a light sandy nature or a stiff clay. If merely dumped over the embankment, then the values given may be reduced by about 1 cent per cubic yard.

B. THE COST OF ROCK REMOVED BY CARTS.

The total cost of loosening hard rock—with wages at \$1.00 per day—is usually covered by 45 cents per yard in place; in dealing with soft shales which can be loosened by pick, being sometimes as low as 20 cents, while in shallow cuttings of tough rock, in which the stratalie unfavorably, \$1.00 may be insufficient.

A good churn-driller will drill from 8 to 12 feet of 2-inch holes, about $2\frac{1}{2}$ feet deep, per day, at a cost of about 12 to 18 cents per foot.

A cart suitable for $\frac{1}{6}$ cu. yd. of earth as a working load will take about $\frac{1}{6}$ cu. yd. of rock. Rock takes longer to shovel into the carts than earth, so that we may say the equation given above for earth becomes in the case of rock

$$N = \frac{M}{6 + L},$$

and the number of yards hauled per day is given by $\frac{1}{6}N$. Loading costs about 8 cents per cu. yd., and the repair of the hauling-road about $\frac{1}{6}$ cent per cu. yd. per 100 feet of lead. Thus we have, exclusive of the profit to the contractor—

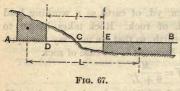
Length of Lead in feet.	No. of cu. yds. per cart per day.	Cost per cu. yd. for hauling and emptying.	Total cost per cu. yd.
50	18.5	6.8	60.0
100	17.1	7.3	60.5
200	15.0	8.3	61.7
300	13.3	9.4	63.0
500	10.9	11.5	65.5
700	9.2	13.6	68.0
1000	7.5	16.7	71.7
1500	5.7	21.9	77.9
2000	4.6	27.1	84.1
2500	3.9	32.3	90.3
3000	3.3	37.5	96.5
4000	2.6	47.9	108.9

"Loose Rock" usually costs about 30 cents per yard less than the above cost for hard rock.

125. Both rock and earth can generally be moved at about the same cost by wheelbarrows as by carts when the lead is equal to about 200 feet; for shorter hauls the wheelbarrows have the advantage, but for longer, the carts.

As regards the cost of removal by scrapers or any other form of vehicle, it may be approximated to in the same manner as the removal by carts in Sec. 124. A scraper generally moves from 30 to 60 cubic yards per day with a short haul. A medium-size steam-shovel, if kept tolerably busy, should, under ordinary conditions, load the cars at a cost of from 2 to 3 cents per cu. yd. Grading-machines, 8 or 12 horse, in light soil and with low fills, can generally turn over from 500 to 1000 cu. yds. per day.

126. Estimating Overhaul.—It is common to allow an extra price, usually from 1



to 2 cents for every cubic yard of material, either earth or rock, for each 100 feet that it is hauled beyond what is termed the limit of free haul.

represented by l in Fig. 67.

Let us suppose that the material in the cut AC is just sufficient to make the fill CB, then the material on which overhaul must be charged is that lying between A and D (or B and E), and the distance which that material is hauled is represented by L, the distance between the centres of gravity of the two solids AD and EB; consequently the length of overhaul =L-l, and if S represents the contents of AD (or EB), then the amount of overhaul = S(L-l).

Thus, for example, if L = 1000 ft., l = 600 ft., and S = 4000cu. yds., the cost of overhaul at 1 cent per cu. yd. per 100 ft. will be \$160.

But though the distance l is always given, in order to locate it on the profile we must find the points D and E, such that the material in DC = the material in EC. This may usually be done by inspection of the profile; and in the same way the points A and B may be fixed. In cases where the centreheights are not fair indications of volume, these points may

be quickly found to within a few feet, by means of the crosssection note book. The positions of the centres of gravity of the two solids AD and EB may also usually be fixed by inspection. On this subject the Engineering News says: "As quick a way as any is to plot the volumes of each solid as ordinates, as one would plot a profile, on stiff card-board, cut out the area thus drawn, and balance it on a knife-edge; but a way which we can recommend as much the best and fairest of any, in competent hands, is to guess at it, throwing the benefit of a doubt for or against the contractor according to the character of the haul, and to some extent of the material excavated. The actual haul cannot fairly be taken at times as the crow flies, nor is it exactly fair that haul over good solid gravel should have the same allowance as haul from a shallow cut through muck. As a contract is a contract, and must be general, no considerable deviations on account of such contingencies as these are admissible, but no considerable ones are necessary, the limits of error in guessing at the 'centre of mass' being very small, and having reference to a small item of price, whereas the limits of error in one unavoidable kind of guessing which is usually going on at the same time, that of classification, are very large, and have reference to a very large item. This consideration alone ought to show the folly of any great hair-splitting in mathematical computations of the precise overhaul; but there is a certain class of minds who are never happy unless they can find some hair to split, and who will split it with just as much care although there may be a log of wood alongside which they can't split, to which the right half of the hair is to be added."

THE CALCULATION OF EARTHWORK.

127. The three solids with which engineers have mainly to deal in the calculation of earthwork are the pyramid, the wedge, and the "prismoid;" for though, owing to the irregularities of surface, these figures, mathematically speaking, are never actually met with in practice where the surface of the ground forms one or more sides of the figure, yet the contents as given by them are sufficiently accurate under ordinary circumstances, when the work has been properly cross-sectioned. But before dealing with the calculation of the contents of

these solids, it will be well to consider the methods of obtaining the areas of the cross-sections themselves, on which the computations are based.

- 1. When the cross-section is of triangular form, as in Fig. 69, its area of course—taking for instance the triangle ABC—equals $AB \times \frac{1}{2}$ the perpendicular distance from C to AB, or AB produced.
- 2. When the cross-section is an ordinary 3-level one, as in Figs. 71 and 72, then if B =width of road-bed and H, h, h', l, and l' are as shown in Fig. 55,

Area =
$$\frac{H}{2}(l+l') + \frac{B}{4}(h+h')$$
,

which is the formula most generally in use.

3. If the surface is horizontal, then this becomes

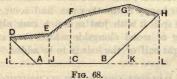
$$Area = H\left(\frac{B}{2} + l\right).$$

4. Or, if regularly inclined,

Area =
$$\frac{B \cdot h}{2} + lh'$$
,

where h is the greater side-height, and l its corresponding distance out from the centre, h' being the smaller side-height.

5. But it frequently happens that we have such a section as that shown in Fig. 68. Such an area may be best calculated



by first finding the contents of the figure *IDHL*, and then deducting from it the areas *DIA* and *HLB*; thus the area of this cross-section equals

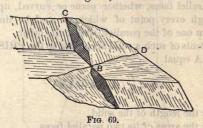
$$\frac{ID+EJ}{2}(IJ)+\frac{EJ+FC}{2}(JC)+\frac{FC+GK}{2}(CK)+\\ \frac{GK+HL}{2}(KL)-\frac{ID\cdot IA}{2}-\frac{BL\cdot HL}{2}.$$

The above forms of cross sections are really all that are required in practice, 1, 2, and 5 being those most generally in

use. Neither of these forms requires plotting, but it is usually advisable to plot cross-sections of large area which are very irregular even though calculated as above, for by so doing mistakes are much more readily apparent. Where the work consists largely of irregular cross-sections, a good and rapid method of obtaining the areas is to plot the cross-sections and use a planimeter. The error in ordinary cross-sections, plotted on cross-section paper to a scale of 10 feet to an inch, should never—where the planimeter is carefully adjusted so as to allow for the shrinkage of the paper, etc.—exceed 1 p. c.; and considering that these errors to a large extent cancel each other and are free from errors of calculation, which are usually much more probable than errors in reading the planimeter scale, the result in the long run is at least equally likely to be as near the truth as that obtained by the more laborious process of calculation.

128. The areas of the cross-sections having been obtained, the calculation of the contents of the solids which they bound is the next point to deal with, and we will consider them in the order given above.

A. The Pyramid.—The usual cases in which pyramids occur are those shown in Fig. 69, which need no explanation.



The contents of such a pyramid as ABCD are found by the formula

$$S = ABC \times \frac{AD}{3}$$
,

and this rule applies to any form of base.

B. The Wedge.—The various forms of wedge which present themselves in calculating the contents of earthwork, of which that represented in Fig. 70 is the usual type, can only be estimated *correctly* by the application of the Prismoidal

Formula. But since at the points where the wedge form of solid occurs the cut or fill is always small, the error involved

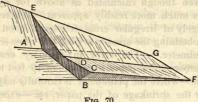


Fig. 70.

by using the formula for the rectangular wedge is immaterial; thus we may say that the contents

$$S={
m area}\;ABCDE imesrac{AG}{2}.$$

C. The Prismoid.—Though the term "prismoid" strictly applies only to such solids as are contained by 6 plane surfaces, the two end-faces being parallel, and two of the other faces being not parallel, the extended application of the "prismoidal formula" has corrupted its true meaning, so that it is now applied very generally in Railroad work to all solids having two parallel faces, whether plane or curved, upon which, and through every point of which, a straight line may be drawn from one of the parallel faces to the other.

The contents of such a solid according to the PRISMOIDAL FORMULA equal

$$S = \frac{L}{6}(A + a + 4M),$$

where L = the length of the solid,

A and a = the areas of its two parallel faces,

and M = the cross-section parallel to A and α , and half-way between them.

This formula at first looks simple enough, but the calculation of M is the difficulty.

129. To explain the application of this formula, suppose we have two end-areas A and a as in Fig. 71.

Now in order to obtain the mid-section, we must know the points in A and a from which the straight lines joining them start, and at which they end; thus in Fig. 71, if the crosssection notes simply give the elevations for the 3-level sections A and a, we assume that the upper surface between them is

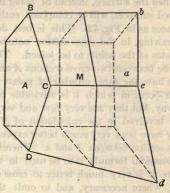
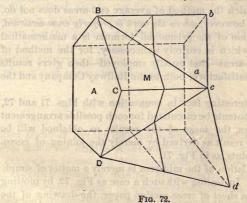


Fig. 71.

composed of two warped surfaces, BCcb and CDdc, which is what follows from supposing that the centre and side heights of M are the averages of the corresponding heights of A and a. So that if the surface were actually as shown in Fig. 72,



we should obtain entirely erroneous results by taking the value of M given by Fig. 71. Thus when the surface is such that points in A and a, other than those directly corresponding, are to be considered as being joined by straight

lines, it becomes necessary to indicate in the notes between what points in A and a the straight lines are assumed to be drawn; and then the surface, instead of being made up of two or more warped surfaces, will be composed entirely of a series of plane surfaces as in Fig. 72. This is best done, where required, by drawing, in the cross-section note-book, lines connecting the notes of the points to be joined. This would also have to be done between two cross-sections A and a which did not happen to have the same number of points taken in each. At times cases occur in which it is advisable to fill in slopelines in this way, but they are very few and very far between; for the labor involved in the calculation of M in such cases would usually have been very much better expended in actually taking a cross-section between A and a. Therefore, as a rule, where the prismoidal formula is to be used in the calculation of the contents, it is very much better to cross-section a little more closely, where necessary, and to omit the filling-in of the slope-lines, than to take cross-sections a little farther apart and fill in the slope-lines by inspection.

The value of the prismoidal formula, as applied in the case of Fig. 71, is not so much to rectify irregularities in surface as to make suitable allowance for the difference in the heights of A and a, which the method of average end-areas does not do. In practice, however, where the work is properly cross-sectioned, the application of the prismoidal formula is a mathematical refinement which is entirely unnecessary, for the method of average end-areas—that usually employed—then gives results sufficiently satisfactory, both to the Railway Company and the Contractor.

It is an interesting fact in connection with Figs. 71 and 72, that if the contents be calculated for each possible arrangement of slope-lines, the mean of the results so obtained will be equal to the result as derived by merely the joining of corresponding points, as in Fig. 71.

The calculation of the mid-area is merely a matter of simple proportion. In dealing with such a case as Fig. 72, by plotting A and a on a sheet of cross-section paper, the drawing of the mid-sections may be done by simply drawing parallel lines; so that this should be done as a check to the calculations and also as a means of facilitating them.

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130. The method used nowadays almost entirely for the calculation of grading, is that of Average End-areas, which assumes that

$$S = \frac{A+a}{2}L.$$

Now this method, which is the simplest of any to work, unfortunately has a considerable tendency to excess; the results obtained by it are, however, the same as those given by the prismeidal formula—applied as in Fig. 71,—therefore presumably correct, under the following circumstances:

1. Whenever the centre-heights of A and a are the same,

whatever the difference in side heights may be.

2. Whenever the entire widths between the slope stakes at A and a are the same, whatever the difference in centre-heights may be.

When, however, the smaller centre-height is at the same end of the solid as the greater width between the slope-stakes, the volume as given by average end-areas will be actually deficient.

But since these cases are the exceptions, the results as given by this method are in the long run considerably too high, unless care is taken in cross-sectioning to limit the excess. To correct for this tendency a **Prismoidal Correction** may be used, found by deducting the prismoidal formula from the formula for average end-areas; and this correction, when the surface of each end-section is horizontal, equals in cubic yards

$$C = (H - H')^2 \frac{sL}{27 \times 6}$$

where H and H' are the end centre-heights in feet, sthe sloperates, and L the lengths of the solid in feet.

Taking $s=1\frac{1}{2}$ and L=100, we obtain the following values for C, which serve in making up preliminary estimates to show the errors involved by a rough system of cross-sectioning when the contents are calculated by average end-areas.

TABLE OF PRISMOIDAL CORRECTION FOR 100 FEET IN CU. YDS. FOR HORIZONTAL SURFACES WHERE $s=1\frac{1}{7}$.

H-H'	0	1	2	3	4	5	6	7	8	9
0	0	1	4	8	15	23	33	45	59	75
10	93	112	133	156	181	208	237	268	300	334
20	370	408	448	490	533	578	626	675	726	779

This value of C is altogether independent of the width of the road-bed; so that, for example, suppose on ground sloping in the direction of the length of the solid we have, between two sections 100 feet apart, a difference in centre-heights of 23 feet, if $s=1\frac{1}{2}$ and there is no slope transversely, the contents as given by average end-areas will be 490 cubic yards too much, even with a 14-foot road-bed; or, if the fill at one end is 2 feet and at the other end 25 feet, the prismoidal formula gives 1957 cubic yards as the volume, while the method of average end-areas gives 2447 cubic yards, or 25 p. c. too much.

But the above values of the prismoidal correction only apply when the surfaces of the sections are horizontal. If, however, in dealing with 3-level sections we call W and W' the entire width between the slope-stakes at each end, then the prismoidal correction equals, in cubic yards,

$$C = (H - H') (W - W') \frac{L}{27 \times 12}$$

which is independent of the side-slopes and width of the roadbed. So that, having calculated the contents according to the formula for average end-areas, we have simply to find for each cross-section the value of (H-H') and (W-W'), and take out from the following table, which gives the values of C, the amount in cubic yards which is to be added to the contents already obtained in order to obtain the result which would be given by the prismoidal formula. Should, however, the smaller centre-height be at the same end of the solid as the greater width between the slope-stakes, then C must be subtracted.

TABLE OF THE VALUES OF C, WHEN L = 100 FEET.

V-W'	CHARLE	$H\!-\!H'$ in feet.											
n feet.	1	2	3	4	5	6	7	8	9	10			
1	.3	.6	.9	1.2	1.5	1.8	2.1	2.4	2.7	3.1			
2 3	.6	1.8	1.8	2.4 3.6	3.0	3.6	4.3	4.9	5.5	6.2			
4	1.2	2.4	3.6	4.9	4.6	5.5	6.5 8.6	7.4 9.8	8.3	9.3 12.3			
5	1.5	3.1	4.6	6.2	7.7	9.2	10.8	12.3	13.8	15.4			
6	1.8	3.6	5.5	7.4	9.2	11.1	12.9	14.8	16.6	18.5			
7	2.1	4.3	6.5	8.6	10.8	12.9	15.1	17.3	19.4	21.5			
8 9	2.4	4.9	7.4	9.8	12.3	14.8	17.3	19.7	22.2	24.6			
9	2.7	5.5	8.3	11.1	13.8	16.6	19.4	22.2	25.0	27.7			
10	3.1	6.2	9.3	12.3	15 4	18.5	21.5	24.6	27.8	30.8			
11	3.4	6.8	10.2	13.6	17.0	20.3	23.7	27.1	30.6	33.9			
12 13	3.7	7.4 8.0	11.1 12.0	14.8 16.0	18.5 20.0	22.2 24.0	25 8 28.0	29.5 32.0	33.3 36.0	37.0 40.1			
14	4.3	8.6	12.9	17.3	21.5	25.8	30.1	34.5	38.8	43.2			
15	4.6	9.2	13.8	18.5	23.1	27.7	32.3	37.0	41.6	46.3			
16	4.9	9.8	14.8	19.7	24.6	29.5	34.5	39.4	44.3	49.3			
17	5.2	10.4	15.7	20.9	26.2	31.4	36 6	41.9	47.1	52.4			
18	5.5	11.1	16.7	22.2	27.8	33.3	38.8	44.4	49.9	55.5			
19	5.8	11.7	17.6	23.4	29.3	35.1	41.0	46.9	52.7	58.6			
20	6.2	12.3	18.5	24.6	30.8	37.0	43.2	49.4	55.6	61.8			
21	6.5	12.9	19.4	25.8	32.3	38.8	45.3	51.8	58.3	64.8			
22 23	6.8	13.5	20.3	27.1	33.9	40.6	47.4	54.3	61.1	67.9			
24	7.4	14.2 14.8	21.3 22.2	28.4 29.6	35.4	42.5	49 6 51.8	56.8 59.2	63.9	71.0			
25	7.7	15.4	23.1	30.8	38.5	46.2	54.0	61.7	69.4	74.1			
26	8.0	16.0	24.0	32.0	40 0	48.1	56.1	64.1	72.1	80.2			
27	8.3	16.6	24.9		41.5	49.9	58.3	66.6	74.9	83.3			
28	8.6	17.2	25.8	34.5	43.1	51.8	60.5	69.1	77.7	86.4			
29	8.9	17.8	26.8	35.7	44.7	53.7	62.7	71.6	80.5	89.5			
30	9.3	18.5	27.7	37.0	46.3	55.6	64.9	74.1	83.3	92.6			

There is no need to apply these corrections at the time when the quantities are worked out by average end-areas, as generally the engineer is then too much occupied in obtaining rough estimates of the work; but they can subsequently be applied, with very little trouble, to such solids as in his opinion need correcting.

The application of this method undoubtedly reduces the final estimate of the grading very considerably, rarely by less than 1 p. c., and in some cases, where the cross-sectioning has been carelessly done, by as much as 4 or 5 p. c. But it must be remembered that in this way the true volume is obtained more nearly than by any other of the approximate processes, and that the results are slightly higher than those obtained by the use of such tables as "Trautwine," "Rice," etc., founded on the principle of Equivalent Level Sections. Without the

application of the prismoidal correction the contractor is entirely at the mercy of the engineer who does the cross-sectioning (if the method of average end-areas is used), who has it, often unconsciously, in his power to make a difference in the final estimate of 3 or 4 per cent, by not paying attention to the differences in centre-heights and widths of the cross-sections he is taking. And though the errors in any given piece of work are in favor of the contractor, still the uncertainty to which they give rise, in the long run do him considerably more harm than good. If a correction is not used, some limiting value for $(H-H')\times (W-W')$ should be established.

Some standard system of measuring grading is much wanted. As it is now, a contractor on one piece of work gets the benefit, possibly of 3 p. c. due to the use of average end-areas, uncorrected; while on the next contract he takes very likely he has the quantities actually cut down, owing to the use of tables of equivalent level sections. It is true that if the work is properly cross-sectioned the excess as given by the method of average end-areas should not exceed 1 or 2 p. c., but in the ordinary way in which cross sectioning is done, a considerable amount of trouble is taken in order to correct for small surface irregularities, while the great errors which are involved by the difference in centre-heights are barely considered so long as the slopes between the sections are tolerably uniform.

When the cross-sections are irregular, the prismoidal correction can usually be applied with sufficient accuracy by treating them as 3-level sections, and thus applying the value of C as given above.

131. The Method of Equivalent Level Sections is an incorrect means of applying the prismoidal formula by reducing the end-sections to sections equivalent in area but with their surfaces horizontal, and then taking as the area of the mid-section that which is given by the mean of the corrected centre-heights. But unfortunately the results so obtained are only correct—

1. When the two end-areas are "similar"—i.e., the corresponding surface-slopes from the centre to the slope-stakes are the same at both ends, provided the road-bed is not intersected between them;

2. When the surface is regularly warped from one end to

the other, provided that no two of the straight lines connecting corresponding points, such as A, α , etc., in Fig. 71 are inclined to grade in opposite direction (as they are in Fig. 71).

In cases where these conditions do not hold, then, assuming that the true result is given by the prismoidal formula if merely the corresponding points A, a, etc., are joined by straight lines, the method of equivalent level sections gives results too small. But if the surface is intersected by undulations, running obliquely, necessitating the use of "slope-lines" as in Fig. 72, then the results may either be too small or too great, according to circumstances. But since this latter method of applying the prismoidal formula is the exception, and the results as obtained by applying it in the manner shown in Fig. 71 more generally correct, the general tendency of the method of equivalent level sections is to deficiency, but not by an amount usually sufficient to warrant the use of a correction. The real objection to this method is the labor involved in applying it when dealing with cross-sections in the slightest degree "irregular," and even in dealing with 3-level sections the work involved is greater than that by the method of average end-areas, corrected; while the result in the former case is an approximation, in the latter it is presumably correct.

132. The method of centre-heights, which is very useful in making preliminary estimates, simply assumes that the contents between any two cross-sections are given according to the method of average end-areas, the area at each end being taken as the area of a horizontal section with a height equal to the actual centre-height. The results so obtained naturally err, sometimes in excess and sometimes in deficiency—the tendency in the former direction being, however, the more common. But since there is no decided tendency to cumulative error, the result obtained as a whole for several stations where the direction of the surface slope is varied, agrees tolerably well with the true volume, though for any one station the error may be very considerable. In the long run more accurate results are usually given by this method than by that of average end-areas. (See Secs. 69 and 70.)

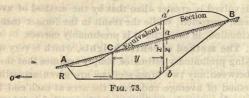
133. By the use of Table XIV the labor of applying the method of Centre-heights is greatly reduced.

Table XV saves considerable labor in reducing areas to cubic yards, by avoiding the necessity of multiplying by 100

and dividing by 27. There is no need to take the quantities out closer than to the nearest yard. In using the table for lengths other than 100 feet a good deal of trouble may be saved in the way of multiplication and division by reducing each time the simpler of the two values with which the table is entered; thus if we have an average area of 634 square feet for 50 feet, the amount opposite 317 gives the quantity required, instead of dividing 2348.2 by 2.

134. Correction for Curvature.—We have hitherto assumed that the cross-sections are parallel to each other—i.e., that the track is straight. Suppose, however, that in Fig. 73, exaggerated for the sake of clearness, o represents the centre of a certain curve whose radius = R, the cross-section ACaB representing any cross-section on the curve.

Now it is clear that if we have two cross-sections whose centres are 100 feet apart (along the curve) and take in each a point b, situated outside the centre by a distance y, the distance between these two selected points, measured along a line parallel to the centre-line, is to 100 feet as R + y is to R, arcs



subtended by equal angles at the centre being proportional to their radii. But instead of calculating the contents for the varying distance, it is simpler to assume that the track is straight, and to correct the sections themselves so as to allow for it: so that, instead of using the above proportion, we may consider that the area of a section at any distance y from the centre must be increased or decreased in the proportion

$$x' = \frac{x(R \pm y)}{R}$$

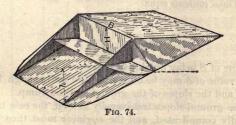
where x' represents the corrected area and x the original area; y being positive if falling, as in Fig. 73, on the outside of the curve, and negative if falling inside. So that if at any point as a we measure the ordinate x and its distance from the

centre y, the above equation gives us x', the corrected length of x, which, being measured upwards from the point b, gives us a', the new position of a. Similarly by finding other positions of a', the curved line ACa'B being drawn through them, gives the equivalent section on a straight track.

In curves of 8° and upwards, where the slope is comparatively steep in one direction, this correction should be applied. It is best to assume an average section for two or three stations together, and to divide the radius by 10, so as to make R a distance easily scaled, and then to divide the correction so obtained by 10. Thus, if the section is taken as an average one for 300 feet on a 10° curve, we plot R = 57 feet, and the correction so obtained—which is of course equal to the difference between the contents given by the actual section and the equivalent section-must itself be divided by 10; or, what is the same thing, be considered to apply only to a length of 30 feet. Two or three ordinates are usually sufficient to locate with sufficient accuracy the surface of the equivalent section. Where the surface is level there will of course be no correction necessary, for then the excess on one side of the centre-line balances the deficiency on the other.

This method is equally easy to apply to any form of cross-section, however irregular it may be.

135. The contents of the toe of a dump are commonly calculated according to the formula given in Sec. 128 for a wedge, but the result so obtained is always considerably too small; neither can the prismoidal formula be directly applied.



First, let us assume the surface of the ground to be level; then the simplest way to obtain correctly the contents of the toe is to consider each corner as a quarter of a cone; then if H equals the height of the fill in feet, and s the slope ratio, the contents of the two corners together equal

$523H^3s^2$;

so that the entire contents of the toe are given by the formula

$$S = .523H^3s^2 + .5BH^2s;$$

B being the width of the road-bed in feet. This formula is easily worked out by means of Table VIII. S must then be divided by 27 to reduce it to cubic yards.

If $s = 1\frac{1}{2}$, then the above equation becomes

$$S = .75BH^2 + 1.178H^3$$
.

But when the ground slopes downward in the direction of the toe, as is the more common case, then we may consider the toe to be divided into two portions, as shown in Fig. 74; the upper one, which we have just dealt with, having a vertical height equal H, and the lower one with a vertical height = h. Then, omitting for a moment the consideration of the circular corners, the contents of the upper portion are to the contents of the lower portion as H is to h. Now, though this does not quite hold good when taking the corners into account, the error involved by assuming it to do so is immaterial; so that we may say, that when the ground slopes forward as in Fig. 74, the total contents equal

$$S' = S\left(1 + \frac{H}{h}\right),\,$$

the value of S being obtained as above.

The value of h may be obtained quite well enough by plotting H and the slopes of the ground and the dump.

If the ground slopes transversely as well, the case becomes decidedly complicated, and the engineer must then assume such values, as will when inserted in the above formulæ, give what he considers fair results.

In dealing with the toe of a dump less than 10 feet in height the wedge formula is sufficiently accurate, but where the fill

TABLE OF BOARD MEASURE.

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amounts to about 20 feet the difference in the results by the two methods is very considerable.

136. The original notes of the cross-sections should be copied on the left-hand pages of another note-book, and opposite them, on the right-hand pages, the sectional areas, contents, etc., should be entered as soon as worked out. A "Record" should also be kept, into which each separate item should be entered as soon as completed,—not in detail, but simply the total amounts; these notes then form the groundwork of the final estimate. The details are entered separately in note-books apportioned to each class of work.

As regards taking notes for the monthly estimates, the simplest way is to walk over the work and sketch on the progress profile the state of construction at the time. Another way, possibly more convenient in light work, is to note the percentage of the total amount which is done up to date.

The classification is often a matter of considerable difference of opinion, especially in the allowance for "loose rock." All boulders, etc., exceeding the limit for loose rock must be carefully measured. When there is much of this to do, a good plan is to have a man especially to look after it on two or three subdivisions, who can also take the Force Account and give to the contractors any simple information they may require concerning the work. The subdivision engineers and their men are thus saved a very considerable amount of time and work.

TIMBER-WORK.

137. Timber is usually measured in railroad structures in B.M. (Board Measure), the contract for culverts, etc., being let by the 1000 feet B.M. One foot B.M. = 144 cubic inches, so that the B.M. of any given stick is found by multiplying together the width and thickness in inches and the length in feet, and dividing the result by 12.

The first portion of this calculation and the division by 12 is accomplished by means of the table on page 151.

In altering the length of trestle-posts, etc., to make allowance for the difference in elevation of the two rails, the following table will be found useful, as well as in many similar operations:

FRACTIONS OF AN INCH IN DECIMALS OF A FOOT.

In.	0	1	2	3	4	5	6	7	8	9	10 -	11
0	Foot	.0833	.1667	.2500	.3333	.4167	.5000	.5833	.6667	.7500	.8333	.9167
1,00	.0026	.0859	.1693				.5026				.8359	.9193
32 16	.0052	.0885	.1719	.2552	.3385		.5052		.6719		.8385	
32	1.0078	.0911	.1745	.2578	.3411	.4245	.5078	.5911	.6745		.8411	
1		.0938					.5104				.8438	
1 8 5 32	.0130	.0964	.1797				.5130				.8464	
16	.0156	.0990	.1823	.2656			.5156		.6823		.8490	
32	.0182	.1016	.1849	.2682	.3516	.4349	.5182	.6016	6849	.7682	.8516	.9349
1	.0208	.1042	.1875	.2708	.3542	.4375	,5208	,6042	.6875	.7708	.8542	9375
1 9 32	.0234	.1068	.1901				.5234			7734	.8568	.9401
5	0260	.1094	.1927	.2760			.5260			.7760		.9427
16 11 32		.1120		.2786			.5286					
3		.1146		2813			.5313		.6979	.7813		.9479
38 132 7 165 232	.0339	.1172	.2005				.5339				.8672	.9505
18		.1198										
35	.0391	.1224	.2057	.2891	.3724	.4557	.5391	. 6224	.7057	.7891	.8724	.9557
1	.0417	.1250	.2083	2917	.3750	.4583	.5417	.6250	.7083	.7917	.8750	.9583
$\frac{\frac{1}{2}}{\frac{17}{32}}$.1276			.3776		.5443	6276	.7109			.9609
18	.0469	,1302	.2135	.2969		4635		6302	.7135			.9635
16 19 32	.0495		.2161				.5495					
5	.0521		.2188				.5521					
0 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	.0547			.3047			.5547		7214		.8880	
16	.0573		.2240			4740			.7240			.9740
32	.0599	.1432	.2266	.3099	.3932	.4766	.5599	.6432	.7266	.8099	.8932	.9766
3	.0625	.1458	.2292	.3125	.3958	.4792	.5625	. 6458	.7292	.8125	.8958	.9792
25	.0651	.1484	.2318	.3151			.5651				.8984	:9818
34-6230075	.0677		.2344		.4010		.5677			.8177		
27	.0703		.2370				.5703		.7370		.9036	
7 8	.0729	.1563		.3229		.4896		6563	.7396		.9063	
29 32 15	.0755		.2422		.4089			.6589	.7422		.9089	
16	.0781			.3281			.5781		.7448		.9115	
31 32	.0807	.1641	.2474	.3307	.4141	4974	.5807	.6641	.7474	.8307	.9141	.9974
2 0	0	1	2	3	4	5	6	7	8	9	10	11

For notes on the strength, etc., of timber, see Part IV.

IRON-WORK.

138. In estimating the weight of Bolts and Nuts the weight of the heads and nuts themselves may be taken from the following table, assuming them to be of ordinary proportion:

WEIGHT OF BOLT-HEAD AND NUT.												
Diameter of Bolt.	1	300	1/2	80100	34	7 8	1	11	11	13	2	21
Hex. Head and	lbs.	lbs	lbs.	lbs	lbs.	lbs						
Nut	.017	.057	.128	.27	.43	.73	1.1	2.2	3.8	5.6	8.8	17
Sq. Head and Nut	.021	.069	.164	.32	.55	.88	1.3	2.6	4.4	7.0	10.5	21

The weight of the shanks of the bolts may be found from the following table of the weight and strength of iron rods. If, however, the screw end is *upset*, with a consequent enlargement of the nut and head, the usual allowance for the weight due to upsetting, and square head and nut, will be equal to about 13 diameters of additional length of the shank of the bolt. If the nut and head are hexagonal, 11 diameters are then sufficient. This allowance is suitable when the length of the upsetting equals about 6 diameters of the shank. Thus if we have a 1-inch bolt upset for 6", if 36" long and the head and nut square, its weight will be given by the weight of a 1-inch bar 49" long.

WEIGHT AND STRENGTH OF ROUND WROUGHT-IRON BARS.

Diam. in inches.	Weight in lbs. per foot run.	Breaking Strain in lbs.	Diam. in inches.	Weight in lbs. per foot run.	Breaking Strain in lbs.
1	.0414 093	550 1240	1½ 14	3.35 4.13	42340 52200
16 4 5	.165 .258	2200 3430	14 13 18	5.00 5.95	63170 75260
7 16	.372	4950 6720	11/25 15/8 11/4 11/8 2	6.99 8.10	88260 102370
100-100 10	.661 .837 1.03	8800 11130 18750	$ \begin{array}{c c} 1\frac{7}{8} \\ 2 \\ 2\frac{1}{8} \end{array} $	9.30 10.6 12.0	117600 133700 142900
7	1.25	16620 19780	23	13.4	160400 178500
156	1.75 2.03	23300 26880	214355 22 22 22 22 22 22 22 23 23 24 23 23 24 23 23 24 23 24 23 24 23 24 24 24 24 24 24 24 24 24 24 24 24 24	16.5 18.2	198000 218200
1 1 1 1	2.33 2.65	3 0910 3 5170	3	20.0	239400 285000

As a safe working strain one fifth of the above breaking strains may usually be taken.

The two washers generally used to each bolt weigh together about the same as a length of shank = 14 diameters; but if the bolt is upset, they then weigh about the same as a length = 22 diameters.

Railroad Spikes.—The following table gives the weight, etc., of the spikes commonly used for fastening the rails to the ties:

Length in inches.	ness in	No. per keg of 150 lbs.	No. per	Length in inches.	Thick- ness in inches.	No. per keg of 150 lbs.	No. per
4½ 5 5 5 5	123/85 7 16 14 9 16 15/8	400 705 488 390 295 257	2.66 4.70 3.25 2.60 1.97 1.71	5½ 5½ 5½ 6 6	100 9 0 100 100 100 10	350 289 218 310 262 196	2.33 1.93 1.46 2.07 1.75 1.30

The following table gives the angle-bars and bolts necessary for 1 mile of track:

Length of Rails in feet.	No. of Angle- bars.	No. of Bolts.	Length of Rails in feet.	No. of Angle- bars.	No. of Bolts.
24	880	1760	27	782	1564
25 26	844 812	1688 1624	28	754 704	1508 1408

The following table gives the weight of Rails required for 1 mile of track:

Weight of Rail per yard.	Weight per mile.		nor mile		Weight of Rail per yard. Weight per mile.		Weight of Rail per yard.	Weight per mile.	
lbs.	tons.	lbs.	lbs.	tons.	lbs.	lbs.	tons.	lbs.	
40	62	1920	56	88	0	65	102	320	
45	70	1600	57	89	1280	68	106	1920	
48 50	75	960	60	94	640	70	110	0	
50	78	1280	62	97	960	72	113	820	
52	81	1600	64	100	1280	76	119	960	

The weight of iron required per mile is very nearly given by the rule: Multiply the weight in lbs. per yard by $1\frac{\pi}{4}$; the product is the weight required in tons of 2000 lbs. (the tons in the table = 2240 lbs.)

The weight of iron in lbs. per yard is given by multiplying its sectional area in inches by 10, assuming the iron to weigh 480 lbs. per cubic foot. Steel rails usually weigh about 490 lbs. per cubic foot.

139. BALLAST AND TIES.—The following table gives the amount of ballast required per mile of road:

Depth	Top Wi	dth, Single	Track.	Top Width, Double Track.			
inches.	10 Ft.	11 Ft.	12 Ft.	21 Ft.	22 Ft.	23 Ft.	
	cu. yds.	cu. yds.	cu. yds.	cu. yds.	cu. yds.	cu. yds.	
12	2152	2347	2543	4303	4499	4695	
18	3374	3667	3960	6600	6894	7188	
24	4694	5085	5474	8996	9388	9780	
30	6111	6600	7087	11490	11980	12470	

This table assumes that the side-slopes of the ballast are at the rate of 1 to 1, and that there is a space of 6 feet clear between the tracks.

The following table gives the number of Ties required per mile of track:

Centre to Centre in inches.	No. of Ties.	Centre to Centre in inches.	No. of Ties.
18	3520	27	2347
18 20 22 24	3168	30	2112
22	2899	33	1920
24	2640	36	1760

For useful information in connection with Construction, see Part IV.

PART III.

EXPLORATORY SURVEYING.

140. In Part I we have already considered the subject of "Preliminary Surveys," made principally with the object of obtaining topography by means of which the final location for a railroad may be selected. We will here deal with the subject of rough Reconnoissance and Exploratory Surveys, in which accuracy—such as it is generally understood—is not essential, and in which the general bearings of rivers and streams, and the elevations of mountain passes, etc., plotted to a scale of a mile or so to an inch, are the main points to be established.

But before dealing with the problems which arise in exploratory surveying it will be well to consider the Instruments usually employed in this class of work.

INSTRUMENTS.

141. The Instruments generally used in Reconnoissance and Exploratory Surveys are the following: The Sextant, Chronometer, Artificial Horizon, and the Cistern and Aneroid Barometers. To these may be added with advantage, a light portable Transit.

We will treat each separately in the order here given.

The Sextant.

There are in common use two forms of sextant—the Nautical and the Box sextant; but since the latter is nothing more than the former reduced into a small portable shape, we can consider them both under one head. For astronomical work the

box-sextant may be considered almost worthless, but for taking ordinary topography it is an extremely handy instrument, and in more extensive work it is a very useful support to a nautical sextant in many ways. The ADJUSTMENTS of the sextant are as follows:

A. To place the index-glass perpendicular to the plane of the instrument.—Set the index to about 60°, and then, looking at the image of the limb of the instrument as reflected in the index-glass, the real limb and the image should appear to form one continuous arc. If they do not do so, the index-glass must be moved by means of the screws at its back (see Fig. 75) until it does.

B. To place the horizon-glass perpendicular to the plane of the instrument.—Clamp the index near to zero, and then, looking at some well-defined object, turn the tangent-serew of the index until the object, as seen directly, and its reflected image are brought, if possible, to coincide. If they cannot be made to coincide the horizon-glass is out of adjustment and must be corrected by means of the adjusting screws with which it is fitted.

C. To obtain the index-error.—For the purpose of measuring the index-error when it is negative, i.e., when the correction for it is to be added, the graduations of the limb are carried a short distance back from zero through what is termed the ARC OF EXCESS. The index-error is obtained by noticing the reading when the coincidence mentioned in Adjust. B is obtained. But in this case the object must be a far distant one, so that the reading may not be affected by instrumental parallax. Had the index been set exactly at zero when the abovementioned coincidence was made, there would of course be no index-error, but it is usually better to apply an index-error than to attempt to obtain an exact coincidence at zero.

A very accurate method of obtaining the index-error is to measure the diameter of the sun several times "on and off the arc"—i.e., on the positive and negative side of zero: the mean of the readings will then be the correction, positive if on the main arc, and negative if on the arc of excess. Thus, for example, if the diameter of the sun measured on the main are = 32′20″, and on the arc of excess 30′40″, the mean being 0′50″ on the main arc, shows that 50″ has to be subtracted from all angles as read from zero on the main arc, i.e., that the coinci-

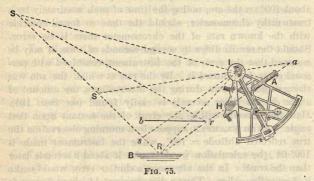
dence mentioned in Adjust. B occurs when the reading is 50" on the main arc.

D. To correct for eccentricity.—A common error to which all sextants are liable is eccentricity of the centre of motion of the index-arm and the centre of the graduated arc. It unfortunately admits of no adjustment, but corrections for it may be obtained as follows: "As it has no appreciable effect on small angles, it is advisable—using the artificial horizon to take a set of altitudes, say 10, which will form a mean of about 100° on the arc, noting the time of each accurately by a trustworthy chronometer; should the time so found coincide with the known rate of the chronometer there is no error. Should the results differ by several seconds of time, it may be assumed that the error of the instrument, combined with personal error, has caused it. By the rate at which the sun was rising or going down during the observations, the amount of angle due to those seconds is easily found (see Sec. 195). Half that amount will be the error of the sextant upon that angle. As an EXAMPLE, suppose by a morning observation the true reflected altitude = 100°, while the instrument made it 100° 01', the calculation would make it about 3 seconds later than the truth. In the afternoon a similar error would make it 3 seconds earlier. Thus a disagreement of about 6 seconds arises for about 1' of altitude. By 4 or 5 such sets of altitudes at different parts of the arc sufficient data will be procured from which to form a table of corrections for all altitudes."

142. The sextant, unlike the transit, has the apex of the angle which it measures not coincident with any particular part of the instrument, but varying its position according to the magnitude of the angle observed. This is due to what is usually called Instrumental Parallax, and arises from the fact that the index-glass is not situated in the direct line of sight. This may be best shown by means of Fig. 75.

Suppose S and R are two objects, the angle between which we wish to measure. When the index-arm has been so placed that the image of S is reflected from the index-glass I, so as to coincide with R as seen directly through the horizon-glass H, the angle which is given by the sextant is the angle SAR, where A is a point in the line of sight, found by producing SI to its intersection. But suppose S' and R were the two objects between which the angle is to be observed, then a will be the

apex of the angle measured. Finally, if S is situated at s, so that sI is parallel to RA, then the angle given by the sextant between s and $R=0^{\circ}$ (i.e., if there were no index-error the reading should be zero), and if the reflection of R were brought to coincide with R as directly seen, then the angle observed would be negative, and would thus be read on the "arc of excess," and be equivalent to IRA. If R is at a distance from the instrument so great that RI and RA are sensibly parallel,—as was assumed in Adjustment C,—the question of instrumental



parallax may be ignored; but in measuring angles between two objects when the object directly looked at is near at_ihand, the instrument must be either so placed that the apex will coincide with the position at which the angle is to be observed, or else a correction applied, the angle as given by the sextant—taking, say, the index-glass as the constant apex of the angle—being always too small.

In using an artificial horizon there is another form of parallax which sometimes needs consideration due to the apex A of the angle observed not coinciding with the artificial horizon. Let R be the image of a star S reflected in the artificial horizon. Then if SA is parallel to SR, as is sensibly the case when dealing with objects at a considerable distance from the instrument, the angle SAR may be considered equal to twice the angle SRB; i.e., the altitude read on the sextant is the "double-altitude" of the star, which needs dividing by two in order to obtain the altitude; but where S is comparatively close at hand, then we cannot consider SAR = 2SRB, and consequently by dividing

the reading on the arc by two, it is not the altitude as reflected from the horizon which is observed, but from a point r so situated that the angle ASr is equal to the angle RSr. Suppose we select this point r in the line of sight, as in Fig. 75, then it may be easily proved that if rb is parallel to RB (the surface of the artificial horizon) $Srb = \frac{1}{2}SAR$. And since the sines of small angles may be assumed to be proportional to the angles themselves, we may consider the point r to be situated halfway between A and R. Thus in observing an altitude with the artificial horizon, where the distance RA is appreciable compared with the distance SA, it becomes necessary either to apply a correction, or to arrange the positions of the horizon and the instrument so that the point r may coincide with the apex of the angle which it is wished to observe.

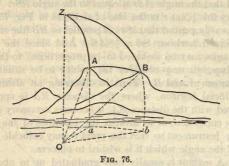
143. A sextant is usually only graduated up to about 140°. For nautical work this is amply sufficient, but where an artificial horizon is used—since the angle read is double the real altitude—the altitude will be limited to about 70°. To obviate this difficulty, sextants are often supplied with a contrivance which consists of a small mirror below the index glass, fixed in such a position that when the index is at the mark numbered 180° upon what is called the Supplementary arc, those two mirrors are at right angles to each other, and the objects whose images appear to coincide in direction really lie in diametrically opposite directions.

144. In observing angles with the sextant, when the two objects and the observer's eye are not in the same horizontal plane, in order that the angle measured may be a horizontal one, it becomes necessary either to arrange matters in such a way that the angle observed between the objects may be the horizontal angle, or to apply a correction to the angle observed.

In the former case two vertical rods may be ranged in line with the objects and the observer's eye, and the angle between them then measured with the plane of the sextant horizontal. But the most accurate method is to observe the angle between the objects themselves, and then to observe the angle of altitude, or depression of each.

Thus, in Fig. 76, let A and B be the two objects, O the position of the observer. Then if Z be the zenith and a and b points where the vertical planes through A and B respectively inter-

sect the horizontal plane abO, then Aa and Bb represent respectively the altitudes of A and B, and the complement of



the altitude of each equals its "zenith distance," AZ or BZ. Then in the spherical triangle ABZ, since we know all three sides, therefore (since ab = Z)

$$\cos\frac{ab}{2} = \sqrt{\frac{\sin S \sin (S - AB)}{\sin AZ \sin BZ}},$$

where
$$S = \frac{AZ + BZ + AB}{2}$$
.

145. Every possible means should be taken in observing angles with a sextant to eliminate instrumental errors. In order to do this all careful observations should be in "doubles:" thus if the observation is for latitude, a star north and a star south should be observed; the errors of the instrument will then affect the result in opposite directions, and taking the mean of the results will eliminate the errors. So also an observation for time should be taken in "doubles:" namely, a star east and a star west. Also in taking Lunar Distances the sets should be taken in "doubles," one set of distances to a star east of the moon and one to a star west.

The Artificial Horizon.

146. The best substance to use for an artificial horizon is mercury, mainly on account of its bright reflecting surface. In a wind, however, syrup is better than mercury, being more

viscous and consequently less liable to be affected by currents of air, but its reflecting surface is decidedly inferior. Oil, too, is frequently made use of. A sheet of water on a still night makes a fairly good horizon.

Black glass horizons, which can be levelled up by means of adjusting screws, are sometimes used, but though at times more convenient than a liquid surface they are considerably less reliable. The best way to carry mercury is in an iron bottle, which can be made by any blacksmith out of a piece of iron pipe, fitted with a screw stopper in the cap. Mercury must be kept carefully away from all greasy substances, and also from lead, gold, or silver, with which it amalgamates. A glass cover in the form of a triangular prism is often of use in shielding the horizon from the wind; but owing to the increased probability of error, due to refraction in the cover itself, it is to be avoided when possible. The mercury can usually be protected from the wind by placing it in a hole slightly below the general surface of the ground, or by building up a sort of protection around it. A wooden trough makes the best form of saucer to hold it in; copper also does well. It should have an outlet at one corner to facilitate the pouring back of the mercury into the bottle. About 5 inches by 3 inches is a good size for the trough. It should also be of about uniform depth, which need not exceed half an inch.

To prepare the horizon, pour the mercury into a small chamois-leather bag, leaving, however, a little behind in the bottle as "scum," and then squeeze it out gently into the trough. The surface so obtained is usually as clear as could be wished for, but if the trough or the leather happens to have been a little dirty, a film of dust will sometimes be found on the surface. This can easily be cleared away by sweeping it lightly with a feather. The horizon is then ready for use.

If a class cover is used over it, the observation should be taken twice, the cover being turned around for the second observation, and the mean of the results taken; in this way the error arising from the refraction of the glass is more or less eliminated.

The mercury should always be carried as steadily as possible, the bottle being kept "end up."

Altitudes less than about 6° cannot be read with the artificial horizon on account of the obliquity of the rays.

An artificial horizon is almost always to be preferred to a natural horizon, such as is given at sea, on account of the refraction of the air, as regards the horizon itself, not entering appreciably into the question.

The Chronometer.

147. Chronometers have been found by experience, when subjected to the shakings and joltings which necessarily more or less accompany their transportation on land, to be very unreliable instruments. A small pocket-chronometer is usually almost as reliable for land work as one of larger and finer make, being less liable to derangement.

As regards the care of chronometers, they should always be kept as much as possible in the same position, and be always wound at the same time of day, and wound to the butt. Also, they must be kept away from all magnetic influence, such as is often caused by their proximity to iron. They should, of course, be rated before starting out, but if they are new chronometers they will probably gain on their "rate." The "shoprate" is almost always different from the field-rate, so that really very little dependence is to be placed on them compared with that placed on chronometers at sea. But though the rate when out on the work may be entirely different from what it was before starting, yet the rate in the field will be more or less constant; and though no great dependence can be placed on the actual position as given by a chronometer after considerable jogging and jolting, yet it serves to connect the various stations observed, relatively to each other, with a fair amount of accuracy when the intervals of time between the observations are not great. These positions can then be finally corrected after the general field-rate of the chronometer has been ascertained.

As regards allowing for temperature, that can only be done by an actual testing at different temperatures. Every chronometer goes fastest in some certain temperature which has to be calculated from the rates that it makes at three fixed temperatures; then as the temperature varies from that at which the chronometer goes fastest, so its rates vary in the ratio of the square of the distance in degrees of temperature from its maximum gaining temperature. A fair test for a pocket-

chronometer is to place it in four extreme positions and let it stay in each for 24 hours; if the rate for any position does not vary by more than five seconds from the rate in any other position, the watch is as good as can generally be found.

BAROMETERS.

148. There are two kinds of barometers used in exploratory surveying—the "CISTERN" form of the mercurial barometer, and the "ANEROID."

The Cistern barometer, owing to its size, is mainly suitable for use in camp as a standard with which the Aneroids may be compared.

The nature of the difficulties involved in observing the difference of elevation between any two points may be best shown as follows:

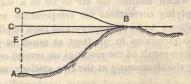


Fig. 77.

In Fig. 77, suppose we have two stations, A and B, whose difference in elevation we wish to determine. If the atmosphere were in a state of rest there would be no difficulty in devising formulæ which should give correct results, supposing the instruments themselves recorded correctly, for then the barometric reading along the horizontal line CB would at all points be the same, and we should simply have to obtain a formula founded on Boyle and Mariotte's law for the pressure of gases, to obtain the difference in the heights of A and C which should correspond with the observed difference in pressure. But since the atmosphere is always more or less subject to disturbing influences, such as temperature, humidity, etc., which cause the barometric gradient at B to assume such forms as BD or BE, no formula founded on statical principles can possibly be expected to give correct results; yet any formula which attempts to take account of the fluctuations in gradient necessitates a knowledge of the temperature,

humidity, and general state of the atmosphere between A and B, which it is impossible to obtain. By taking observations at points immediately between A and B some allowance may be made for these various disturbances, but as a rule very little is gained by so doing compared with the time and labor which it involves.

Since the variations in gradient are generally too rapid to allow of the state of the atmosphere at one hour being of much service in indicating its probable condition a few hours—or even minutes—later, it follows that labor spent in reducing barometric readings between two such stations as A and B, by applying corrections for latitude and various other requirements which are often employed, simply results in a mathematical illusion which is possibly erroneous to the extent of 50 or 100 p. c.

The best way to proceed in ordinary practice is to make use of formulæ which assume the air to be in a state of equilibrium—applying corrections for temperature which experience has shown to be necessary—and then to eliminate the errors due to variations in gradient as much as possible by taking the mean result of the readings on several occasions, or by observing simultaneously at the two stations, as described in Sec. 150.

149. The first information necessary in devising a formula for the reduction of barometric readings is the relative weight of mercury and air. This ratio amounts to about 1050, depending upon which values of the densities are employed. The barometer at the time is supposed to be at sea-level in latitude 45° at a temperature of 32° F. This ratio, if multiplied by 5.74—which is a factor obtained from Boyle and Mariotte's law that the density of a gas varies directly as the pressure to which it is subjected—gives a product known as the barometric coefficient. Various values are given for this coefficient, but probably that given by Regnault is the most accurate, namely, 60,384; from this, taking no account of the effects of temperature or latitude, we find that the difference in elevation in feet equals

$$X = 60384 \log \frac{H}{h},$$

where H is the barometric reading at the lower station and h

is the barometric reading at the upper station. The correction for temperature, as usually applied, assumes that the mean temperature of the air between A and B is the mean temperature of the air at the two stations. If we then take .004 as the coefficient of expansion of air for 1° Centigrade, the above formula needs multiplying by 1+.002(T+t), where T and t are the temperatures on the Centigrade scale at the lower and the upper station, respectively; and if we take T and t as the temperatures on the Fahrenheit scale, then this factor becomes

$$1+\frac{T+t-64}{900}$$

and this is usually called the "temperature term."

Another factor is often employed to correct for the different effects of gravity, due to difference of *latitude*. According to Laplace, this "latitude term" equals

$$1 + .0026 \cos 2L$$
,

where L= the latitude. He also applied a correction for the effect of altitude above sea-level on the force of gravity; but this may be altogether neglected. A correction is also sometimes applied to allow for the effect of temperature on the barometers themselves—which is ascertained by having thermometers attached to them. And since changes of temperature affect both the mercury and the scales in opposite directions, if we take .0001 as the *relative* expansion of mercury for 1° F. to the expansion of the scales, in order to correct the barometers themselves for temperature, the above value of X should be multiplied by

$$\frac{1}{1-.0001(T'-t')}$$
,

where T' and t' are the temperatures as recorded by the "attached" thermometer at the lower and the upper station, respectively.

Thus the complete formula becomes

$$X = 60384 \log \frac{H}{h} \left(1 + \frac{T + t - 64}{900} \right) \times \left(1 + .0026 \cos 2L \right) \left(\frac{1}{1 - .0001 (T' - t')} \right).$$

A correction for humidity is sometimes applied, but it necessitates observations of the state of the air being taken with a hygrometer; and since it is doubtful, even then, whether any material advantage is derived by so doing, we may ignore this correction entirely. We may simplify the above equation considerably by dispensing with the latitude term, which in ordinary practice is never required. In aneroid barometers the last term of course does not enter into the question at all; so that the formula generally applicable to aneroid barometers is

$$X = 60384 \log \frac{H}{h} \left(1 + \frac{T + t - 64}{900} \right).$$

If H and h do not differ by more than about 3000 feet we may do away with the logarithms in the above equation, which thus becomes, approximately,

$$X = 52450 \frac{H - h}{H + h} \left(1 + \frac{T + t - 64}{900} \right).$$

The error involved by this formula is inappreciable within the limits stated.

By assuming (T+t) to equal 108° this formula becomes

$$X = 55000 \, \frac{H - h}{H + h},$$

which is generally known as Belville's Formula and is convenient for rough work.

The table opposite gives the VALUES OF
$$\left(\frac{T+t-64}{900}\right)$$
.

150 The results which are obtained by using only one barometer, carrying it from station to station, are of course subject to all the errors of gradient; and these errors usually increase with the distance between the two stations; but by taking the mean of several results, the probable error becomes greatly reduced. (See Sec. 204.) Errors of gradient may be more or less eliminated by using TWO BAROMETERS, and observing simultaneously at each station, the barometers being

T+t	$\frac{T+t-64}{900}$	T+t	$\frac{T+t-64}{900}$	T+t	$\frac{T+t-64}{900}$	T+t	$\frac{T+t-64}{900}$
200	0489°	660	+.0022°	1120	+.0533°	158°	+.1044°
22	.0467	68	.0044	114	.0556	160	.1067
24	.0444	70	.0067	116	.0578	162	.1089
26	.0422	72	.0089	118	.0600	164	.1111
28	.0400	74	.0111	120	.0622	166	.1133
30	0378	76	+.0133	122	+.0644	168	+.1156
35	.0356	78	.0156	124	.0667	170	.1178
34	.0333	80	.0178	126	.0689	172	.1200 -
36	.0311	82	.0200	128	.0711	174	.1222
38	.0289	84	.0222	130	.0733	176	.1244
40	0267	86	+.0244	132	+.0756	178	+.1267
42	.0244	88	.0267	134	.0778	180	.1289
44	.0222	90	.0289	136	.0800	182	.1311
46	.0200	92	.0311	138	.0822	184	.1333
48	.0178	94	.0333	140	.0844	186	.1356
50 52	0156	96 98	+.0356 .0378	142	+.0867 .0878	188	+.1378
54	.0133	100	.0400	146	.0911	192	.1400 .1422
56	.0089	102	.0400	148	.0933	194	.1444
58	.0069	104	.0422	150	.0956	194	.1444
60	0044	106	+.0467	152	+.0978	198	+.1489
62	.0022	108	.0489	154	1000	200	.1511
64	.0000	110	.0511	156	.1022	202	.1533

compared before and after the observations: and these errors may of course be still further reduced by taking the mean of several simultaneous observations; and in this way the best results can probably be obtained. But between two stations there is usually a permanent gradient dependent on local causes, such as the topography and nature of the ground, which no number of observations would tend to eliminate, and for which allowance can rarely be made. It is largely due to this cause that the heights of mountains, calculated from the mean of a large number of observations which differ but little from each other, are often found, when obtained by more accurate means, to be very largely in error.

151. There are two or three points in connection with the READING OF BAROMETERS that are worth remembering. For instance, readings should never be taken in the immediate vicinity of any body which obstructs the wind. "If the barometer is observed on the windward side of a mountain the reading will be too high; if on the leeward side, too low." Neither should readings ever be taken directly before or after a storm of wind or shower of rain, as the atmosphere is then usually in an unsettled state.

152. "The pressure of the air everywhere undergoes a

daily oscillation. The gradient introduced by this daily change is called the DIURNAL GRADIENT. The pressure has two maxima and two minima which are easily distinguishable. Near the sea-level the barometer attains its maximum about 9 or 10 a.m. In the afternoon there is a minimum about 3 to 5 p.m.; it then rises until 10 to midnight, when it falls again until about 4 a.m., and again rises to attain its forenoon maximum. The day fluctuations are the larger."

"The annual progress of the sun from tropic to tropic throws a preponderance of heat first on one side of the equator and then on the other, which produces an annual cycle of changes in the pressure, and gives rise to what has been called the ANNUAL GRADIENT. The amount of this variation is quite small, but increases rapidly toward the poles; at the equator it rarely exceeds one quarter of an inch per year, while in the polar regions it is often as much as two or three inches in a few days."

We will now consider the barometers themselves.

A, The Cistern Barometer.

153. This is an awkward instrument to carry about, but its usefulness on exploratory work usually fully makes up for the inconvenience which it causes. It is found by experience to be absolutely necessary in carrying forward an extended system of barometric observations to have at hand a standard barometer with which the aneroids may be from time to time compared.

A supply of tubes and mercury should accompany the barometer in case of accident, and it should be provided with a wooden and leather case. When moved from one place to another, even across the room, it should be screwed up so that the tube and cistern will be perfectly full, and gently turned over, end for end, so that the cistern will be uppermost. In wheeled vehicles it should be carried by hand, and on horseback strapped across the rider's shoulder. By carrying it with the cistern uppermost any particles of air which may be contained in the mercury become disengaged by the jolting, and escape at the end where they do no harm.

154. TO FILL A BAROMETER, should it become necessary to do so in the field, proceed as follows: Warm both the

mercury and tube and filter in through a paper funnel-the hole of which does not exceed 1 of an inch-to about 1 of an inch from the top. Close the end and turn the tube on its side: the mercury will then form a bubble which can be made to travel from end to end and gather all the small air-bubbles visible that adhered to the inside of the tube while filling. Let the bubble pass to the open end, fill up with mercury and close the tube. Reverse the tube over a basin, when, by slightly relieving the pressure against the end, some of the mercury will be forced out, forming a vacuum above, which ought not to exceed half an inch. Close up again tightly and let this vacuum-bubble traverse the length of the tube as before, on the several sides, absorbing the minute portions of air still left, now greatly expanded by the reduction in pressure. Perfect freedom from air can be detected by the sharp concussion with which the mercury beats against the sealed end, when, with a large vacuum-bubble, the horizontally held tube is slightly moved. Any air which may still be left-which will probably not affect the reading by more than a few thousandths of an inch-will soon escape if the barometer is carried about cistern uppermost.

Filling by boiling is a slightly more efficient method, but it

is a much more difficult proceeding.

155. IN READING THE BAROMETER, first of all note the temperature on the attached thermometer, then screw up the mercury in the cistern so that its surface just touches the ivory point, being careful that the barometer hangs vertically. Give a gentle tap near the top of the mercurial column to destroy the adhesion of the mercury. Set the vernier by bringing its front and back edges into the same horizontal plane with the top of the mercury; then read.

156. Should the mercury in the cistern become so dirty that neither the ivory point nor its reflection in the mercury can be seen, the instrument must be taken apart and cleaned. To do this "screw up the adjusting screw at the bottom until the mercury entirely fills the tube, carefully invert, place the instrument firmly in an upright position, unscrew and take off the brass casing which encloses the wooden and leather parts of the cistern. Remove the screws and lift off the upper wooden piece to which the bag is attached; the mercury will then be exposed. By then inclining the instrument a little, a

portion of the mercury in the cistern may be poured out into a clean vessel at hand to receive it, when the end of the tube will be exposed. This is to be closed by the gloved hand, when the instrument can be inverted, the cistern emptied, and the tube brought again to the upright position. Great care must be taken not to permit any mercury to pass out of the tube. The long screws which fasten the glass portion of the cistern to the other parts can then be taken off, the various parts wiped with a clean cloth and restored to their former position." Everything used in the operation must be clean and dry, and all breathing on the parts avoided as much as possible.

If the mercury is dusty or dimmed by oxide it may be cleaned by filtering through chamois leather, but if chemically impure it must be rejected and fresh mercury substituted. The cistern should then be filled as nearly as possible and the wooden portion put together and fastened. The screw at the bottom of the instrument should then be screwed up. "The instrument can then be inverted, hung up and readjusted. The tube and its contents having been undisturbed, the instrument should read the same as before."

B. The Aneroid Barometer.

157. The "Aneroid" is a valuable instrument for engineering and exploratory purposes on account of its portability, and though not to be compared in accuracy with the mercurial barometer, the results given by it will often not differ from those given by the latter sufficiently to be of importance. It is in such cases as these that the aneroid is eminently useful. But it is too liable to derangement, and subject to too many defects, to warrant its being used in any other way than to supplement some more accurate form of obtaining elevations. In dealing with the mercurial barometer, after the correction for temperature has been applied, the instrumental errors which need correcting are very small; but with an aneroid the same cannot be said. Most of the better class of aneroids are supposed to compensate automatically for changes in temperature. This compensation should be tested by comparison at different temperatures with a standard barometer, and the errors tabulated and kept for future reference.

While reading, the aneroid should always be held horizontally, for the weight of the parts themselves has a very considerable influence on the readings; a difference corresponding to fifty feet being not uncommon when held in different positions. The aneroid may be adjusted by means of the small screw at its back, so as to agree with the reading of a standard barometer, but when the difference is only slight it is better to regard it as an "index error," and correct in that way, than to alter the reading.

158. Cheap aneroids commonly have the SCALE of inches subdivided so as to read the elevations above sea-level. This would be very convenient if only the corresponding pressure at the sea-level were always the same as given on the index and the atmosphere always in a state of equilibrium. The pressure at the sea-level is generally assumed as being equivalent to 30 inches.

Another method which is convenient, though "unscientific and inaccurate," is that of having a movable scale of elevations which can be set to agree with the barometer reading at any known elevation. But the best way to obtain a reading is to observe the reading in inches, and then to reduce it by one of the formulæ already given.

BAROMETRIC AND ATMOSPHERIC HEIGHTS.

-	Bar.	Alt'de	Bar.	Alt'de.	Bar.	Alt'de.	Bar.		Bar.	Alt'de.
	in.	feet.	in.	feet.	in.	feet.	in.	feet.	in.	feet.
			-						-	
1	21.	9900.1	23.	7375.1	25.	5060.6	27.	2924.4	29.	940.9
1	.1	9768.3	1.1	7254.7	.1	4949.8	.1	2821.8	.1	845.4
	.2	9637.1	.2	7134.7	.2	4839.5	.2	2719.6	.2	750.2
	.3	9506.5	.3	7015.3	.3	4729.6	.3	2617.8	.3	655.3
-	.4	9376.4	.4	6896.5	.4	4620.1	.4	2516.3	.4	560 7
4	.5	9247.0	.5	6778.1	.5	4511.0	.5	2415.2	.5	466.5
	.6	9118.3	.6	6660.2	.6	4402.3	.6	2314.4	.6	372.6
	.7	8990.0	.7	6542.8	.7	4294.0	.7	2214.0	107.7	279.0
	.8	8862.4	.8	6426.0	.8	4186.3	.8	2114.0	.8	185.7
-P	.9		.9	6309.6	.9	4078.9	.9	2014.3	.9	92.7
-	22.	8608.9	24.	6193.8	26.	3971.9	28.	1915.0	30.	0.0000
	.1	8483.0	.1	6078.3	.1	3865.4	.1	1816.0	.1	-92.5
Я	.2	8357.7	.2		.2		.2	1717.4	.2	
	.3	8233.0	.3		.3		.3	1619.2	.3	-276.6
	.4		.4		.4		.4		.4	-368.2
	.5		.5		.5		.5		.5	
	.6		.6		.6		.6		.6	
	.7		.7		.7		.7		.7	- 641.4
	8.	7617.5	.8		.8		.8		.8	
	.9	7495.9	.9	5171.9	.9	3027.4	.9	1036.8	.9	- 822.2
			11	Spirit S	11	Smartin.	li .	minus in	11	Richard Po-

No advantage seems to be gained by the use of large aneroids; in fact experience shows that when the barometer is subjected to much shaking, the best work is usually done by instruments not exceeding 3 inches in diameter. The elevations according to which the elevation-scales on aneroids are usually divided are as given on the preceding page, and are obtained by a formula similar to those already given, assuming the temperature to be 60° Fahr.

Many scales, however, adopt a temperature of 32° F., in which case the corresponding elevations will be reduced in the proportion of 1.058 to 1.

The uncertainty which is connected with barometric observations is greatly dependent on the latitude; the barometric pressure being very much more regular in the tropics than in the polar regions,

EXPLORATORY SURVEYS.

159. There are three distinct ways in which exploratory surveys may be carried on:

A. By a series of triangulations.

B. By direct measurement and compass courses.

C. By astronomical observations.

And though usually an explorer makes use more or less of all three methods, it will be better for the sake of clearness to consider each separately.

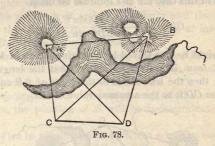
A. By a Series of Triangulations.

The method of triangulating is mainly suitable to mountainous country, or at any rate to country where a view of distant mountain-peaks is to be had.

Before, however, considering the practical working of this system, it will be well to deal with a few of the principal trigonometrical problems which arise in work of this sort.

In Sec. 59 we have already dealt with some of the simpler forms of triangulation, suitable in cases where a straight line has to be continued over an inaccessible surface; but we will here consider the cases of obtaining distances and directions of points relatively to each other.

160. Given two inaccessible points A and B, to find their distance apart and bearing relatively to each other.—In Fig. 78 let CD be a line the length and bearing of



which are known. Observe the angles ACD, BCD, ADC, and BDC. Then in the triangle CDA we have the angles at C and D and the length CD, and can thus find CA. Similarly in the triangle CBD we can find CB. Then in the triangle CAB we have the side CA and CB and the angle at CA, from which we can obtain the distance CAB and its bearing relatively to CD.

The following equations, however, reduce the work which the direct solution given above involves. Find an angle K such that

$$\tan K = \frac{\sin ADC \sin CBD}{\sin CAD \sin BDC};$$

then

$$\tan\left(\frac{CAB - ABC}{2}\right) = \tan\left(45^{\circ} - K\right) \cot\frac{ACB}{2};$$

then

$$CAB = \frac{CAB + ABC}{2} + \frac{CAB - ABC}{2}$$
,

and

$$AB = CD \frac{\sin BDC \sin ACB}{\sin CBD \sin CAB}$$

If C can be ranged in line with A and B we can then find the position of A and B separately, as shown in Sec. 59; the difference of the distances so obtained gives the length of AB, and the bearing is obtained by direct observation.

Suppose, however, that in Fig. 78 the length and direction of AB is known, and it is the distance CD which is required.

Then observe the angles at C and D and obtain CAB as before, but in this case the last formula becomes

$$CD = AB \frac{\sin CBD \sin CAB}{\sin BDC \sin ACB}.$$

This might be also solved by assuming a certain length for CD, and from it finding as above what the length of AB must be; then the true AB is to the value of AB so obtained as the true CD is to the assumed value of CD.



Fig. 79.

If, as in Fig. 79, the lines AB and CD cross each other, the above formulæ apply equally well.

161. The problem known commonly as the "Three-point Problem" is probably the most useful method there is of establishing the position of any given point; it is as follows:

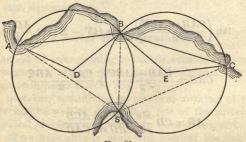


Fig. 80.

Suppose, as in Fig. 80, we know the position of three points A, B, and C and wish to fix the position of the point S; we can do it by simply observing the angle ASB and BSC.

Then, in order to obtain the position of *S geometrically*, proceed as follows:

Find D, the centre of the circle ABS (by setting off at A and B angles equal to $90^{\circ} - ASB$). Then draw the circle through the points A, B, and B. Similarly find the centre E and draw the circle BCS. Then B, the point of intersection opposite B, is the position required.

When one of the angles is obtuse, set off its difference from 90° on the opposite side of the line joining the two objects to

that on which the point of observation lies.

When the angle ABC = the supplement of the sum of the two angles, the position of S will be indeterminate by this method.

S may often be obtained with sufficient accuracy instrumentally by plotting the angles ASB and BSC on a piece of tracing-cloth, and sliding it over the plan until the required position is obtained. The "station-pointer" is an instrument much used for this purpose, especially in hydrographers' offices, where soundings are usually plotted in this way.

If accuracy is required the position of S may be found analytically thus, as given by Prof. Gillespie:

Let
$$AB=c$$
; $BC=a$; $ABC=B$; $ASB=S$; and $BSC=S'$. Also make $T=360^{\circ}-S-S'-B$, and let $BAS=U$, and $BCS=V$. Then

$$\cot U = \cot T \left(\frac{c \sin S'}{a \sin S \cos T} + 1 \right);$$

$$V = T - U;$$

$$SB = \frac{c \sin U}{\sin S}, \text{ or } SB = \frac{a \sin V}{\sin S'};$$

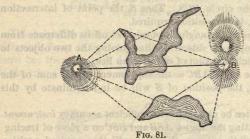
$$SA = \frac{c \sin ABS}{\sin S}, \text{ and } SC = \frac{a \sin CBS}{\sin S'}.$$

Thus if
$$ASB = 33^{\circ} 45'$$
, $BSC = 22^{\circ} 30'$, $AB = 6000$ ft. and $BC = 4000$ ft., we find $ABC = 104^{\circ} 28' 39''$. Then $U = 105^{\circ} 08' 10''$; whence $V = 94^{\circ} 08' 11''$.

SB = 10425.1 ft., SA = 7101.9 ft., and SC = 9342.9 ft.

162. The position of a point may also be fixed by observing the bearings from it of two known points, and may be found on the plan by drawing through those points the bearings so obtained; their intersection gives the point required.

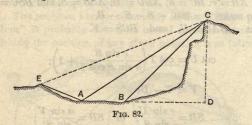
163. Another common method of fixing the positions of



outlying points is by intersection, as in Fig. 81, the position of the two points of observation A and B being known.

164. While on the subject of triangulation, it will be as well to consider the methods of obtaining the heights of mountains trigonometrically.

In the first place, suppose we are able, as in Fig. 82, to ob-



tain two points A and B in the direction of C (a point the elevation of which we wish to obtain) both at the same elevation, and to measure the distance between them; then

$$CD = \frac{AB}{\cot CAD - \cot CBD}$$

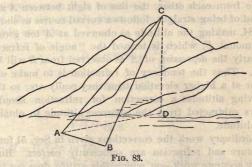
If, however, the two points cannot be taken at the same level, but have to be taken such as E and A, observe the angle CEA, and at A the altitudes of C and E, either with an artificial horizon or with the vertical arc of a transit. Then in the triangle EAC

$AC = EA \sin E \csc C$,

where the angle at C = the sum of the altitudes of E and C (taken at A) — the angle at E.

This would of course hold equally good if EA sloped the other way, but then C= alt. of C from A- alt. of A from E- angle at E. The correction for curvature and refraction given in Sec. 51 must be added to the height as obtained above.

But suppose it is not convenient to obtain a base as above in the same direction as C. Then, as in Fig. 83, measure a



base AB (not necessarily level) and observe the angles CAB and CBA. Then in the triangle ABC

$AC = AB \sin B \csc C$.

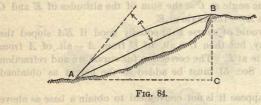
Next observe the altitude of C from A, i.e., the angle CAD; then

$CD = AC \sin CAD$.

To the height so obtained, the correction for curvature and refraction given in Sec. 51 should be added.

Suppose it is required to find the difference in elevation of two inaccessible points, the simplest way is to find the elevation of each separately, as above, and subtract the one from the other,

165. In observing altitudes, the refraction of the air enters so largely into the question and varies so enormously according to the condition of the atmosphere, that every precaution must be taken to eliminate the errors due to it, where accurate work is wanted.



Its nature is such that suppose A and B are two stations visible from each other, the line of sight between A and B. instead of being straight, follows a curved course as shown in Fig. 84, making the altitude as observed at A too great, by the amount F, which is termed the "angle of refraction." Similarly the depression of A as observed from B will be too small. Thus the tendency of refraction is to make objects appear at a higher elevation than they really are; so that in observing altitudes a correction for refraction should be always subtracted from the apparent altitude to obtain the true altitude.

In ordinary work the corrections given in Sec. 51 for both curvature and refraction are sufficiently correct. But for highly accurate work—on which this article does not treat various allowances and corrections must be made.

Refraction diminishes with altitude and is slightly greater over water than land. It is generally at its maximum during the night, and at its minimum about noon; but it is steadier in the night than in the day time, and for this reason night work is usually as reliable as work done during the day. About sunrise and sunset are the worst times to observe altitudes, for not only is refraction then high in quantity, but also extremely variable. A day with the sky overcast is a good day on which to take an observation. Clear days are more subject to rapid changes than dull ones. (For Astronomical Refraction, see Sec. 184.)

166. A method of eliminating to a great extent the effect of refraction in observing the difference of elevation of two stations A and B, is that of observing Reciprocal Angles. Thus in Fig. 84, at A, the altitude of B should be observed, and at B (when practicable) the depression of A. Half the difference of these angles will be the combined correction, and the tangent of half their sum, multiplied by the horizontal distance between them, will give the difference of level, after adding the correction for curvature of the earth given in Sec. 51. This method assumes that the coefficient of refraction is the same at both A and B; therefore the angles should, if possible, be observed simultaneously, lest the refracting power of the air should change in the interval. (For the correction for Refraction, see Sec. 51.)

167. To obtain the height of a mountain by the observed depression of the sea horizon.—The depression of the horizon, or as it is commonly called at sea the "Dip," taking R = the earth's mean radius of curvature in feet, equals in seconds

$$D = 206265 \sqrt{\frac{2\overline{H}}{R}}$$

$$= 63.8 \sqrt{\overline{H}};$$

therefore

$$\sqrt{H} = \frac{D}{63.8},$$

where H = Height in feet.

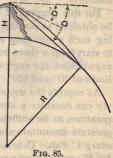
Thus, were it not for refraction, we could find the elevation of A (Fig. 85) by merely observing A the dip D. But D' is the dip actu-

ally observed; so that, taking refraction into account, the above formula becomes

 $\sqrt{H} = \frac{D'}{55}$ (nearly),

which can only be depended on to give approximate results.

168. In observing altitudes with a sextant and artificial horizon, as for instance in Fig. 84, the altitude of Fig. 85. B will be one half the altitude read on the arc, since it is the



"double altitude" that is actually observed. To find a point C on the same level as the instrument the altitude can then be measured down from AB. To observe the depression of A from B with a sextant and artificial horizon, we must establish some point—as far off as possible so as to reduce parallax—the altitude of which exceeds about 6° , and observe its altitude correctly, and then obtain the angle between it and the object whose depression we wish to find. At night a star may often be made use of for this purpose, allowance being made for its motion. This method may also be employed in reading altitudes which would otherwise need the use of a supplementary arc. (See Parallax, Sec. 142.)

To read an altitude or depression with a transit, observe the altitude first in the usual way, then "reverse" and point the telescope to the object and read its co-altitude; the mean altitude so obtained is free from error due to the "horizontal axis" not being truly perpendicular to the "vertical axis" of the instrument. The errors of graduation and observation are also somewhat reduced.

169. It is essential that a survey which consists of a series of triangulations should have an accurate base to start from. Sometimes in exploratory surveys the distance between two mountain peaks, or some prominent objects near the point at which the survey starts, is already known with sufficient accuracy to warrant the line joining them being accepted as a base, but more usually it is necessary to obtain the distance between such points from a base more or less accurately measured.

For this purpose of course as level a piece of ground must be obtained as possible, and as there is often difficulty in finding such a site long enough for a base, it becomes necessary to start from a short base and then extend it by a series of triangulations, the angles of which fall, if possible, between the limits of 30° and 120°.

As regards the MEASUREMENT OF A BASE for ordinary work we can consider a steel tape, properly tested at a given temperature, to be sufficiently accurate. The correction for temperature amounts to about .000007 of the length of the tape for every 1° Fah. Thus a 100-foot tape, tested at a temperature of 50° F., would give a result too long by about 3 feet in 2 miles at a temperature of 90° F.

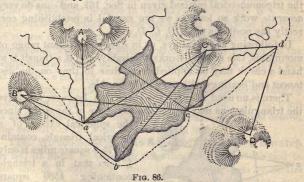
Since all maps are made on the assumption that the linear measurements are *reduced to the sea-level*, in dealing with high altitudes the length of the base may be multiplied by

$$1\frac{h}{r}$$
 (nearly),

where h = elevation above sea-level, r = radius of the earth (see Sec. 206), in order to reduce it to sea-level. But this is a refinement which is usually only needed in work requiring great accuracy.

170. In making a regular triangulation survey, the angles of the main triangles are of course themselves observed; but in such work as exploratory surveys, where mountain peaks are selected as "stations," such a method of procedure would, on account of the time and difficulty involved, be out of the question. A readier method of proceeding may be best shown by an example as in Fig. 86. It depends upon always having in view at any station at least two points whose positions are known.

Suppose we have obtained, by triangulation or otherwise, the distance between and bearing of two conspicuous points *A* and *B*, and suppose our route lies along the dotted line *abcd*.



At a, a point from which A and B are visible, we observe the bearings of A and B, and thus fix the position of a. Suppose that from a a distant mountain peak C is visible, we take the bearing of it also; then if we wish to fix the position of such a point as b, from it we observe the bearings of B and C. When

we get to c we locate its position by bearings from A and B; but suppose we can see A and B no farther, it then becomes necessary to establish two other points which we may use as we have already used A and B. A bearing to C will then locate it. We also observe the bearing of D. When d is reached, we observe the bearings of C, C, and D, which fix its position and also the position of D.

No simpler way of keeping a course can be had than this; and it has the enormous advantage over many of the methods in use, that it fixes the main topographical features bordering along the route at the same time as positions on the route itself. The explorer must be constantly on the lookout for points ahead on his probable route and in the neighborhood. The drawback to the method is its inaccuracy when worked by magnetic bearings alone. But if the points are well selected, an error of a degree or so in the bearings is really immaterial in work of this class, and the errors usually more or less counteract each other. Besides, from time to time the courses and distances can be easily checked by the establishment of another base, and the work already done more or less corrected, and a fresh start made.

If we keep *three* or more points in view we are able to apply the trigonometrical method given in Sec. 161, and thus do very *accurate* work so long as we are careful in establishing correctly the positions of A, B, C, D, etc.

In following along valleys, or in sight of a distant range of mountains, this method works admirably, and if a transit is at hand a check may be applied from time to time on the distances and bearings with very little trouble.

There is no need to apply any correction, however extensive the triangulations may be, for the curvature of the earth, since

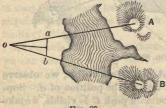


Fig. 87.

the spherical excess of a spherical triangle containing 75,5 square miles is only 1"; so that in a triangle containing 4530 square miles the sum of the three B angles only exceeds 180° by 1'.

171. To measure a

horizontal angle without an instrument between two

such points as A and B from O, as in Fig. 87. Range in a and b with A and B, each distant from O by, say, 50 feet. Measure ab, then

$$\sin\frac{AOB}{2} = \frac{ab}{100}.$$

172. To measure a vertical angle without an instrument, probably the simplest way is to hold a pencil vertically out at arm's length and note the length subtended on it. Then if the distance from the eye to the pencil = l and p is the length subtended on the pencil,

$$an A = rac{p}{l},$$

where A is the angle required. Similarly if L were the distance of some object whose height H we wish to obtain,

$$H = \frac{Lp}{l}$$
.

173. Distance across an open stretch of water can often be taken with sufficient accuracy by observing the time occupied by the passage of the report of a gun from one point to the other. This may be done in the day-time if there is a telescope handy to watch for the smoke, but otherwise the flash of course can be best seen at night. The velocity v, in feet per second, with which sound travels, depends greatly on the temperature; thus at 32° F., v = 1090; at 60° F., v = 1125; and at 100° F., v = 1175.

By taking the mean of 3 or 4 shots, the distance may be obtained with confidence to a quarter of a mile. If the wind is blowing hard in the direction from which the sound comes, the velocity of the wind may be added to v.

174. We can observe an interval of time when a watch is not at hand by counting the vibrations of a stone tied to the end of a string. If from the centre of gravity of the stone (and the string) to the point of suspension is 39.1 inches, each vibration occupies one second. For any other length L, each vibration occupies

$$\sqrt{\frac{L}{39.1}}$$
 seconds.

The vibrations should be kept as small as possible so as to reduce the resistance of the atmosphere. In this way a tolerably long interval may be measured with a fair amount of confidence. The best way, however, is to compare the vibrations with a watch subsequently.

B. BY DIRECT MEASUREMENT AND COMPASS COURSES.

175. By far the most convenient and accurate method of obtaining direct measurement on exploratory surveys is by means of an **odometer**, which answers the same purpose as the patent log at sea, only more efficiently; but unfortunately it necessitates the use of some wheeled vehicle, which is not always a convenient appendage to an exploring outfit.

Pedometers answer well in country where the condition of the ground is comparatively regular and walking easy, but where the surface is much broken they are worse than useless, being misleading as well. The best means of then ascertaining the distance travelled is by estimating the rate of progress and keeping track of the time. The approximate rate may always be found by noting the time occupied in covering, say, 100 yards; then if t= the time occupied in seconds, the velocity in miles per hour equals

$$v = \frac{200}{t}$$
 (nearly);

so that we have the following values of v for various values of t:

t secs.	w. p. h.	t secs.	v m. p. h.	t secs.	v m. p. h.	secs.	w. p. h.
200	1	80	2.5	40	5	25	8
133	1.5	68	3	3.3	6	22	9
100	2	50	4	28	di biruan	20	10

As regards keeping the courses by compass, in open country, it is best to establish the bearing of some point ahead on the probable route and then to correct it by estimation, if, when abreast of that point, it should be found to be considerably to

one side of the route taken. In timber country, the bearing of the sun being taken from time to time, it forms a highly useful guide when no distant landmarks are visible. At night the pole-star forms as good a guide as could be wished for.

C. BY ASTRONOMICAL OBSERVATIONS.

176. Before attempting the solution of astronomical problems in connection with the establishment of positions on the earth's surface, it will be well to give a few explanations as briefly as possible regarding the fundamental principles involved, and definitions of the terms used.

od vab olates anor H .. TIME.

177. Civil or Common Time is really what is termed in astronomical language Mean Solar Time, with this difference, that a civil day being reckoned from midnight to midnight, the corresponding astronomical day is reckoned from the noon of that day to the following noon, and is also counted continuously up to 24 hours. Thus 4 A.M. on Jan. 10 would be stated in mean solar time as 16h 0m Jan. 9. Now the velocity with which the earth travels round the sun varies in different parts of its orbit. Owing to this cause and also to the obliquity of the ecliptic (see Sec. 180) the sun's apparent motion is irregular. Thus we find that the sun is apparently travelling faster in winter than its average rate, and in summer slower. It is simpler to consider the earth as stationary and the celestial bodies as revolving round it. In speaking of the velocity of the sun's motion, then, it is its motion among the stars-or on the star sphere—that is referred to, not its actual motion in the sky; the average rate of this motion is about 59' per day and in a direction opposite to that in which the whole star sphere is apparently revolving, so that the motion of the sun in the sky is really slower than that of any given star, the result of which is that the star apparently revolves round the earth 366 times while the sun only makes 365 revolutions

Now, owing to the irregularity in the sun's motion, it is more convenient to substitute for the real sun a *fictitious* one, termed the "Mean Sun," which is imagined to make the same number of revolutions in the course of the year as the real sun, but always to maintain the same rate of motion. Thus it follows that the mean sun sometimes crosses the meridian—i.e., is due south—before, and sometimes after, the real or, as it is termed in the Nautical Almanac, the apparent sun.

178. The interval of time between the passage of these two suns across the meridian is called the Equation of Time, which when the mean sun is ahead of the apparent sun is considered positive, and when the apparent sun is ahead, negative. Thus, since the mean sun is always south at mean noon, by adding or subtracting (as the case may be) the equation of time to or from 24 hours—subtracting 24 hours if necessary—we obtain the mean solar time at which the apparent sun is on the meridian, i.e., apparent noon. Thus, if for a certain day the equation of time is given as + 12^m 04^s, the apparent sun will be on the meridian 12^m 04^s after mean noon, or at 0^h 12^m 04^s astronomical mean time. Had the equation been negative, apparent noon would have occurred at 23^h 47^m 56^s mean astronomical time.

Expressing the relative positions of the two suns in the form of an equation, we have

Mean Time = Apparent Time ± Equation of Time.

The mean time of that sun is the greater whose R.A. is the less. (See Sec. 180.)

Day of Month.	Jan.	Feb.	March.	April.	May.	June.
1 11 21	+ 4 ^m 0° + 8 21 + 11 41	+14 29	+ 12 ^m 28 ^s + 10 06 + 7 12	+3 ^m 50 ^s +0 58 -1 25	- 3 ¹⁰ 03 ⁸ - 3 48 - 3 37	- 2 ^m 24 ^s - 0 36 +1 31
malvara (July.	August.	Sept.	Oct.	Nov.	Dec.
1 11 21	+ 3m 36s + 5 15 + 6 05	+ 6 ^m 04 ^s + 4 56 + 2 53	- 0 ^m 13 ^s - 3 35 - 7 06	- 10 ^m 27° - 13 19 - 15 22	- 16 ^m 19 ^s - 15 49 - 13 53	- 10 ^m 39 ^a - 6 23 - 1 31

The above values of the Equation of Time show approximately the positions of the two suns relatively to each other throughout the year. These values change but little from year to year; and are sufficiently accurate to enable an engineer to find mean time to a few seconds whenever he may not have a Nautical Almanac at hand; or to correct the reading of a sun-dial, which of course gives apparent solar time, in order to reduce it to mean time.

179. Now the interval of time between the passage of a star across the meridian one day and its passage on the following day is equal to one Sidereal day; and since the sun makes only 365.242 revolutions to 366.242 of the stars, we have

A sidereal day = 23^h 56^m 4^s.09 mean solar time,

or, A mean day = $24^{\circ} 03^{\circ} 56^{\circ}.55$ sidereal time; or, in other words,

To convert a sidereal interval of time into mean solar units, it has to be reduced at the rate of 9.830 seconds per hour;—while

To convert a mean solar interval into sidereal units, it has to be increased at the rate of 9.856 seconds per hour.

Sidereal time is reckoned from the "vernal equinox," or the moment at which the sun crosses from the southern to the northern hemisphere, and is thus, in a way, altogether independent of mean solar time; but if we know the moment at which the vernal equinox occurs in mean time, we thus have a means of connecting sidereal with mean time. But instead of having to start our calculations from the vernal equinox each time, the sidereal time of mean noon is given for every day in the year in the Nautical Almanac; so that

To convert sidereal time into mean time, we have this rule: From the sidereal time given (increased if necessary by 24 hours) subtract the sidereal time at the preceding noon, and then reduce the result at the rate of 9.830 seconds per hour;—and,

To convert mean time into sidereal time: Increase the mean time at the rate of 9.856 seconds per hour; the time thus obtained, added to the sidereal time at the preceding noon (subtracting 24 hours if necessary), gives the corresponding sidereal time.

The Conversion of the Intervals may be greatly facilitated by means of Table XIX.

DECLINATION AND RIGHT ASCENSION.

180. These are terms used to denote the positions of celestial bodies in the star sphere relatively to the equinoctial (which is really its "equator") and a plane perpendicular to it passing

through the vernal equinox; in the same way as terrestrial Latitudes and Longitudes give the positions of places on the earth's surface, relatively to the equator and the meridian of Greenwich.

The plane of the earth's equator produced to the star sphere gives what is called the *Equinoctial*; and the *Ecliptic*, which is really the plane occupied by the earth's orbit, is inclined to the equinoctial at an angle of about 23° 27′ (slightly varying), which is termed the *Obliquity of the Ecliptic*.

Instead, however, of expressing the Right Ascension of bodies as so many degrees E. or W. of the vernal equinox, it is more convenient to adopt the phraseology of sidereal time and denote the positions of bodies according to the interval of time at which they cross the meridian after the zero of sidereal time, i.e., the vernal equinox. Thus it follows that the sidereal time at which a body is on the meridian is given by its Right Ascension (R.A.), so that instead of speaking of the "sidereal time at preceding noon" as in the rules given in Sec. 179, we might have said "the R.A. of the mean sun at preceding noon," for the sidercal time at noon is often so stated in almanacs. And if we know the sidereal time at mean noon, say at Greenwich, we can, by adding or subtracting the equation of time (as the case may be) obtain the R.A. of the apparent sun at mean noon at Greenwich, and by correcting the sidereal time at mean noon at the hourly rate of +9.856 seconds, and also correcting the equation of time, we can find the sun's R.A. at any later hour.

The Declination of a body, which is really its angular measure on the star sphere, north or south of the equinoctial, is considered *positive* when north, and *negative* when south.

181. But so far we have assumed, except in the case just mentioned above, that it has been unnecessary to correct either the equation of time, R.A. or Dec., as given in the almanac; but since these quantities are always varying, and they are only given for a certain hour at a certain place, when required for any other hour the values as given in the tables must be corrected—usually with sufficient accuracy by simple interpolation—to reduce them to the time for which they may be required. And since every 15° of longitude west is equivalent to 1 hour later and 15° east to 1 hour earlier, if in longitude 90° west of Greenwich we want the declination of the sun at

4 P.M., and for noon on that day it was given in the almanac as + 17° 40′, and at noon on the following day as + 18° 00′, the declination at 4 P.M. in longitude 90° west (which is equivalent to 10 hours later) will be 17° 48′.3; and in the same way the R.A. and Equation of time must be corrected.

In dealing with stars, daily and hourly corrections are unnecessary, since their Decs. and R.A.'s change but little in the course of the year (see Sec. 213); but in dealing with the moon, the change is so rapid as to necessitate a more accurate interpolation than would be given by simple proportion as above.

HOUR-ANGLE, ETC.

182. The "hour-angle" is a term which may best be explained by means of Fig. 87.

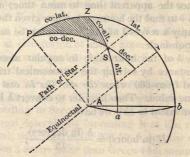


Fig. 87.

Suppose a person stationed at A, on the earth's surface, observes a star S at an altitude Sa above the horizon ab. Then if P is the celestial pole and Z the zenith, since he knows the declination of the star, if he also knows his latitude, he has the three sides of the spherical triangle PZS given by the complements of these values; and this triangle, if PZb is the meridian of A, is generally known as the astronomical triangle, and the angle ZPS is the hour-angle, which, if expressed in time, is really the difference in R A. of the star S and of a point on the meridian at the moment of the observation; or, in other words, it equals the difference between the R. A. of the star and the sidereal time at the moment. Thus if the hour-angle

in sidercal time = H and the local sidercal time = T, we have, to convert the hour-angle into sidercal local time,

$$T = H + R.A.$$
 (-24 hours if necessary);

and conversely,

$$H = T (+24 \text{ hours if necessary}) - \text{R.A.},$$

which is the formula for obtaining the hour-angle when the body observed is either the moon, a planet or star; the R.A. being the R.A. of the body observed at the moment of observation. In the case of the sun, in order to convert the hourangle into mean local time, we have simply to reduce it to apparent time by dividing by 15 (as given below), and then apply the equation of time (corrected for the time of observation) to reduce the apparent time to mean time; and the converse of this—to find the hour-angle when given the mean local time—is simply a reversal of the process, for the sun's apparent time is its hour-angle.

The value h of the hour-angle in angular measure, as obtained for instance by solving the astronomical triangle, must be subtracted from 360° when the star lies in east in order to give it its true value. Then in order to convert h into H, since 1 hour is equivalent to 15° , we have

$$H(\text{in hours}) = \frac{\hbar \text{ (in degrees)}}{15};$$

and this equation of course holds good if for the words "hours" and "degrees" we substitute on both sides either the word "minutes" or "seconds." So that, for instance, if we obtain by an observation of a star in the *east* a value for the hour-angle—as obtained from the astronomical triangle—of 40° , we have $h = 320^{\circ}$; therefore $H = 21^{\ln} 20^{\text{m}}$.

Table XX greatly facilitates the conversion of H into h, or vice versa.

183. The following examples serve to illustrate what has already been said.

1. At what hour will Arcturus culminate (i.e., be on the meridian) on Sept. 18, 1889, at Greenwich? From the Nautical Almanac we find that the sun's mean R.A. at mean noon at Greenwich on Sept. 18 = 11^h 50^m 22^s.8, and also that the R.A.

of Arcturus will then = 14^h 10^m 37^s .8; and since the R.A. of the star is really the sidercal time at which it culminates, we have merely to convert its R.A. into mean time according to Sec. 182. Thus Arcturus will be on the meridian at 2^h 20^m 15^s mean astronomical time, i.e., at 2^h 20^m 15^s P.M.

- 2. What will be the R.A. of the apparent sun on Nov. 15, 1889, in longitude 90° W. at 4 P.M.? Since 4 P.M. in 90° W. occurs 10 hours after mean noon at Greenwich, and from the Nautical Almanac we find the Sun's mean R.A. at mean noon on Nov. $15 = 15^{\rm h} 39^{\rm m} 03^{\rm s}$.0. Since the correction for 10 hours = $+10 \times 9^{\rm s}.856 = 1^{\rm m} 38^{\rm s}.5$, the Sun's mean R.A. corrected to date = $15^{\rm h} 40^{\rm m} 41^{\rm s}.5$. Similarly the equation of time corrected to date = $15^{\rm m} 08^{\rm s}.3$; and since the apparent sun is then ahead of the mean sun, the R.A. of the apparent sun for the date required = $15^{\rm h} 39^{\rm m} 40^{\rm s}.5 0^{\rm h} 15^{\rm m} 08^{\rm s}.3 = 15^{\rm h} 24^{\rm m} 32^{\rm s}.2$.
- 3. Find the Sun's declination at 8 a.m. July 22, 1889, in longitude 30° E. Now 8 a.m. at 30° E. occurs 6 hours before mean noon at Greenwich; and from the Nautical Almanac the declination at Greenwich at mean noon on July $22d = +20^{\circ}$ 12′ 16″, which, corrected to 6 hours earlier, $=+20^{\circ}$ 15′ 15″, which is the declination required.
- 4. Given 10^h 24^m 08^s as the local astronomical mean time on Feb. 1, 1889, in longitude 60° W. to convert it into local sidereal time. According to Sec. 179, we must first convert this time into a sidereal interval by increasing it at the rate of 9.856 secs. per hour, which gives 10^h 25^m 50^s.5, and the sidereal time at mean noon 4 hours later than Greenwich mean noon = 20^h 48^m 11^s.2, thus the local sidereal time (deducting 24 hours) = 7^h 14^m 01^s.7.
- 5. Suppose on June 1, 1889, we observe Castor at 2^h 30^m 04^s A.M. local time, in longitude 105° W. what is the Rour-angle in angular measure?

This in mean astron. time equals, May 31 Increase at rate of 9°.856 per hour		04 ⁸ 22 ⁸ .9
Sidereal interval in sidereal time		
Sidereal local time of obs. $= T$		178.6

6. Given the hour-angle of the apparent sun in the east, as obtained from the astronomical triangle, as 14° 29' 10'' on June 14, 1889, in longitude 90° E., find the mean local time. Since the observation is in the east, $h = 345^{\circ}$ 30' 50'', which corresponds with 23° 02° 03° ; therefore the observation occurred 23° 02° 03° apparent time after apparent noon on June 14; and at that moment the mean sun was ahead of the apparent sun by 0° 10° , therefore the mean local time of observation $= 23^{\circ}$ 02° 13° June 14.

REFRACTION, PARALLAX, SEMI-DIAMETER, AND DIP.

184. In Secs. 51 and 165 we have already considered the effect of Refraction when dealing with objects on the earth's surface. The same uncertainty exists in dealing with celestial objects as to the amount of the correction necessary to counter-

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	0 00	33 00	2 30	16 23	6 30	7 52	12 20	4 16	30	1 38	60	0 33	
	0 05	32 11 31 22	2 35 2 40	16 04 15 45	6 40 6 50	7 41 7 31	12 40 13 00	4 09 4 03	31 32	1 35	61 62	0 32	
	0 15	30 36	2 45	15 27	7 00	7 21	13 20	3 57	33	1 28	63	0 29	
	0 20	29 50	2 50	15 09	7 10	7 12	13 40	3 51	34	1 24	64	0 28	
	0 25	29 06	2 55	14 52	7 20	7 03	14 00	3 46	35	1 21	65	0 27	
	0 30	28 23	3 00	14 35	7 30	6 54	14 20	3 40	36	1 18	66	0 25	
	0 35	27 41	3 05	14 19	7 40	6 46	14 40	3 35	37	1 16	67	0.24	
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	0 45	26 20	3 15	13 48	8 00	6 30	15 30	3 23	39	1 10	69	0 22	
	0 50	25 42	3 20	13 33	8 10	6 22	16 00	3 17	40	1 08	70	0 21	
	0 55	25 05 24 29	3 25 3 30	13 19 13 05	8 20 8 30	6 15	16 30 17 00	3 11 3 05	41 42	1 05	71 72	0 20 0 19	
	1 00	23 54	3.40	12 39	8 40	6 08	17 30	2 59	43	1 01	73	0 17	
	1 10	23 20	3 50	12 14	8 50	5 55	18 00	2 54	44	0 59	74	0 16	
	1 15	22 47	4 00	11 50	9 00	5 49	18 30	2 49	45	0 57	75	0 15	
	1 20	22 15	4 10	11 28	9 10	5 43	19 00	2 44	46	0 55	76	0 14	
	1 25	21 44	4 20	11 07	9 20	5 37	19 30	2 40	47	0 53	77	0 13	
	1 30	21 15	4 30	10 47	9 30	5 31	20 00	2 36	48	0 51	78	0 12	
	1 35	20 46	4 40	10 28	9 40	5 26	20 30	2 32	49	0 50	79	0 11	
	1 40	20 18	4 50	10 10	9 50	5 20	21 00	2 28	50	0 48	80	0 10	
	1 45	19 51	5 00	9 53	10 00	5 15	21 30	2 24	51	0 46	81	0 09	
	1 50	19 25	5 10	9 37	10 15	5 08	22 00	2 20	52	0 45	82	0 08	
	1 55 2 00	18 59 18 35	5 20 5 30	9 21 9 07	10 30	5 00 4 54	23 00 24 00	2 14 2 07	53 54	0 43	83 84	0 07	
	2 05	18 11	5 40	8 53	11 00	4 47	25 00	2 02	55	0 40	85	0 05	
	2 10	17 48	5 50	8 39	11 15	4 41	26 00	1 56	56	0 38	86	0 04	
	2 15	17 26	6 00	8 27	11 30	4 35	27 00	1 51	57	0 37	87	0 03	
-	2 20	17 04	6 10	8 15	11 45	4 29	28 00	1 47	58	0 36	88	0 02	
	2 25	16 44	6 20	8 03	12 00	4 23	29 00	1 43	59	0 34	89	0 01	
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act the refractory power of the air, as we found to exist when the objects observed were near at hand; but in the case of Astronomical Refraction the altitude of the object is a much more important factor than in the previous case; for the lower the altitude not only the more obliquely do the rays pass through the successive layers of air, but the extent of atmosphere which they have to traverse is greater than at a higher altitude. The preceding table of Mean Refractions, calculated for a barometer pressure of 29.6 inches and a temperature of 50° F., may be used at all times under ordinary circumstances, when dealing with celestial objects whose altitudes exceed 30°.

At low altitudes the corrections given in the table should be corrected by multiplying them by the factors B and T, which make allowance respectively for the height of the Barometer and the Temperature of the air: thus

True Refraction = Mean Refraction $\times B \times T$.

VALUES OF B.

Bar. In.	28	28.5	29	29.5	30	30.5	31
В	0.946	0.963	0.980	0.997	1.014	1.031	1.047

VALUES OF T.

Temp.	- 30° F.	– 10° F.	+ 10° F.	+ 30° F.	+ 50° F.	+70° F.	+90° F.
T	1.180	1.130	1.082	1.038	1.000	0.960	0.925

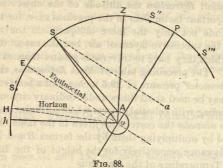
The correction for refraction must of course be *subtracted* from the observed altitude.

185. The positions of all celestial bodies as given in the Nautical Almanac are calculated with reference to the Centre of the Earth; thus if, as in Fig. 88, an observer at A observes the altitude of the sun S to be the angle SAH, in order to reduce this angle to the centre of the earth, i.e., to the angle SOh, he must add to it the angle ASO, which is termed the Parallactic angle.

Now if S were just on the horizon, i.e., at H, then

$$\sin AHO = \frac{AO}{HO} = \frac{\text{Radius of Earth}}{\text{Distance of Sun'}}$$

where AHO is termed the Horizontal Parallax, and is given in the Nautical Almanac. In the case of the sun it varies



from about 8".7 to 9".0. In order to reduce this to Parallax in Altitude, we have from the above figure

$$\sin ASO = \sin AHO \sin SAZ$$
:

therefore

or, assuming the sines of small angles to be proportional to the angles themselves,

Par. in alt. = Hor. Par.
$$\times$$
 cos (alt.).

Thus, at an altitude of 45° , Parallax in altitude = 6", and at $60^{\circ} = 4$ ".

In the case of the *moon*, since its distance from the earth compared with the radius of the latter makes it important what value of the radius is used, the Hor. Par. is given in the Nautical Almanac as *Equatorial horizontal parallax*, meaning that the value of the radius used is that at the Equator; thus for other latitudes the correction taken from the following table should be subtracted from it before applying the correction for altitude, in order to obtain the value of the Horizontal parallax suitable for the latitude in question:

	LATITUDE.										
Eq. Hor. Par.	10°	20°	30°	40°	50°	60°	70°	80°	90°		
53' 61'	0".3	1".2 1".4	2".7 3".1	4".4 5".1	6".2	8".0 9".2	9".4 10".8	10".3 11".9	10".6 12".2		

186. Correcting for Semi-diameter.—In taking an altitude of the sun, the upper or lower "limb" is generally observed, and the altitude so obtained corrected by the subtraction or addition of the semi-diameter—obtained from the Nautical Almanac—to reduce it to the sun's centre. In observing with an artificial horizon, the application of the correction for semi-diameter can be avoided by bringing the reflections to coincide. With either a transit or sextant a good way is to observe one limb and note the time, and immediately after observe the other limb and note the time; the mean altitude may then be considered to give the altitude of the sun's centre at the mean time.

Similarly in observing the transit of the sun across any vertical plane we take the mean time of the passage of its east and west limbs.

In observing the moon, we usually can only observe one limb; and in this case, on account of its proximity to the earth, it is necessary to apply a correction to the semi-diameter as given in the Nautical Almanac, which assumes the observer to be at the centre of the earth, in order to allow for the increase in its semi-diameter on account of his being nearer to it than the centre of the earth. This is termed correcting for the Augmentation of the Semi-diameter. The corrections are given in the following table:

With TO S	APPARENT ALTITÜDE.											
Semi-diam.	10°	20°	30°	40°	50°	60°	70°	80°	900			
14' 30'' 17' 0''	2".4 3".4	4".7 6".5	6".9 9".5	8".8 12".1	10".5 14".4	11".8 16".3	12".9 17".7	13".5 18".6	13".7 18".8			

In finding the time occupied by the semi-diameter of the sun or moon in crossing the meridian, it must be remembered that it is only when the declination = 0° that (if the R.A. is not changing) the semi-diameter will travel across the plane at the rate of 15° to one sidereal hour (or 15° 2' 24" to one mean hour). At any other declination we have, as the rate of travel,

$$15^{\circ} = 1 \text{ sid. hour} \times \cos (\text{dec.}),$$

on just the same principle as the length of a degree of longitude decreases as the cosine of the latitude. In the same way,

it is only when the body is on the horizon that its semi-diameter can be measured, without correction, by the horizontal circle of a transit, for as the altitude of the body increases, so also does the horizontal circle increase its reading in proportion to the secant of the altitude.

The change in R.A. during the passage of the semi-diameter must of course be added to the time which it would have occupied had its R.A. been constant.

187. Dip.—This is a correction only necessary when the sealevel is taken as the horizon, and is practically the same as that given in Sec. 167. It is to be subtracted from the observed altitude. The following are its approximate values, but refraction enters too largely into the question to enable accuracy to be obtained by the use of a sea-horizon:

Height above { Sea-level in feet, {	5	10	20	30	40	50	60	75
Dip,	2' 5"	3' 0''	4′ 10′′	5′ 10′′	6' 0''	6' 40''	7′ 20′′	8′ 10′′

Other values may be found from the values of H, calculated according to Sec. 167.

188. We will now sum up the corrections (which we have already considered) necessary to apply in taking ordinary observations.

1. Observation for Altitude.

A. Using a sea horizon or level.

If a Star. Observed Altitude (- Dip) \pm Index-error - Refraction = True Altitude.

If the Sun, or a Planet. Observed Altitude (— Dip) \pm Index-error — Refraction \pm Semi-diameter + (Hor. Parallax \times cos alt.) = True Altitude.

If the Moon. Observed Altitude (— Dip) ± Index-error — Refraction + (Hor. Eq. Parallax corrected for latitude and converted into Par. in alt.) ± Semi-diameter, reduced for Augmentation = True Altitude.

B. Using an artificial horizon.

In this case the double-altitude as read on the arc + or - the Index-error must be divided by 2 in order to obtain the observed altitude, and then the other corrections—except of

course for Dip, which only comes in when using a sea-horizon-applied as above. If the two reflections are brought to coincide, there will be no correction needed for semi-diameter; but a more perfect observation can usually be obtained by bringing the limb of one reflection in contact with the opposite limb of the other, in which case the semi-diameter must be corrected for as above.

"Index-error" includes errors of any sort in connection with the instrument for which allowance must be made.

2. Observation for Azimuth.

If a Star. Observed Azimuth = True Azimuth,

If the Sun or a Planet. Observed Azimuth ± (Semidiameter × sec alt.) = True Azimuth.

If the Moon. Observed Azimuth ± Semi-diameter (reduced for Augmentation) × Sec. alt. = True Azimuth.

Having now considered all the corrections which need be applied in the case of ordinary field observations when using either a sextant or small portable transit, we will next consider the methods by which the latitude and longitude of a place may be established by astronomical observations.

LATITUDE.

189. A. By a Meridian Altitude.—In Fig. 88, if for the moment we assume the observer to be at the centre of the earth, so as to do away with the idea of parallax, if PSH is the meridian and S the Sun, SE represents the Sun's Dec. N.: and if its declination did not change, since Sa indicates its path, we can easily see that its altitude would be greatest when on the meridian. But since its declination is always changing. the Sun attains its maximum altitude in the northern hemisphere when its declination is changing towards the north, after it has passed the meridian, and when changing towards the south, before it reaches the meridian. The difference between its meridian altitude and its maximum altitude does not exceed at any season 1", so that in ordinary work the maximum altitude is assumed as being equal to the meridian altitude.

In taking an observation of the moon with a sextant it is necessary to allow for this, especially about the time of the equinoxes, the difference between its meridian and maximum altitudes sometimes amounting to as much as 2' 15".

When a transit is used to observe the meridian altitude, it is usually set in the meridian, so that no correction is then required.

For the amount of the correction, see Note G, Appendix.

Now in Fig. 88, if Oh were the observer's horizon, the altitude of the Sun is represented by the angle SOh, Z is the Zenith, and the latitude of the place of observation is given by the angle ZE. Therefore the latitude of the place equals

$$ES + SZ = Dec. N. + Zenith distance.$$

And since the Zenith distance is the complement of the altitude, we are thus able, by means merely of the meridian altitude, to obtain the latitude; and this applies equally well to all celestial bodies, so that in the northern hemisphere, if, as S in Fig. 88, the Dec. is N., then

If declination is south, as S',

Lat. = Zenith distance – Dec. S.
$$(b)$$

If the Star is above the Zenith, as S",

If the Star is below the pole, as S''',

In the Southern Hemisphere the same formulæ apply, bearing in mind that what is South in the southern hemisphere is equivalent to what is North in the northern.

The altitude taken "below the pole" is of course the minimum altitude. The altitudes of S" and S" are observed in the north.

Suppose, for instance, we observe the meridian altitude of Regulus on Mar. 17, 1889, to be 40° 16′ 40″.

Now the declination of Regulus at that date = 12° 30′ 30″; so that we have

Observed altitude of Regulus Correction for refraction	40° 16′ 40′′ - 1′ 07′′
True altitude	40° 15′ 33′′ = 49° 44′ 27′′ 12° 30′ 30′′
Therefore, Latitude by Eq. (a)	ude 105° W., the
Correction for refraction	- 50" + 5" - 16' 15"
True altitude of sun's centre Therefore, zenith distance	48° 10′ 20′′ = 41° 49′ 40′′
Now the sun's declination S. at Greenwich at app. noon on Feb. 8	= 14° 49′ 30″ - 5′ 36″
Sun's declination at date	14° 43′ 54′′

When using a transit, we may proceed in two ways:

- 1. By observing the maximum altitude and correcting according to Sec. 189, and Note G, Appendix.
- 2. By setting the transit in the meridian, and then observing the altitude of the passage.

The meridian may best be obtained by an Elongation of Polaris as described in Sec. 57, or by the other methods described in Secs. 57 and 202.

In taking meridian altitude it is well to observe a star in the north as well as a star in the south; the mean result is then tolerably free from instrumental errors.

Polaris, either at its upper or lower transit, is a good star to use on account of its slow motion admitting of several altitudes being taken.

B. By Transits across the Prime Vertical.

191. This is the most accurate method of obtaining the latitude, but necessitates the use of a transit.

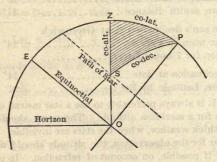


Fig. 89.

In Fig. 89 let PZE represent the meridian, Z the zenith, P the celestial pole, and S the body, the time of whose transit across the prime vertical—i.e., the vertical plane ZO, lying due east and west—we wish to observe, in order by it to obtain the latitude. Now in the spherical triangle ZPS the angle at P = the hour-angle \hbar (see Sec. 182), and ZS = the co-alt. of the body when on the prime vertical, ZP the co-latitude, and PS the co-declination.

Therefore, since $Z = 90^{\circ}$,

$$tan (lat.) = tan (dec.) \times sec h.$$

But in order to obtain h, we must know the exact local time of the observation, which may be obtained according to Secs.

195, etc. The longitude we need only know with sufficient accuracy to admit of correcting the sidereal time at mean noon, i.e., for ordinary work, to about 20 miles.

This method of determining the latitude of a place admits of high precision, since an error of 1 second in the local time only causes an error of about 1\frac{2}{3} seconds in latitude, or about 170 feet.

The passage of the star across the prime vertical should be observed both in the east and the west (or else another star used), and the mean result taken to eliminate errors.

The altitude of a body when on the prime vertical is given by the equation

$$\sin (alt.) = \sin (dec.) \csc (lat.);$$

and the hour at which the observation occurs is given by the equation

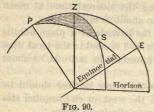
$$\sec h = \tan (lat.) \cot (dec.).$$

If the transit has three vertical hairs, which it should at least have for astronomical work, the star may be observed at, say, its eastern transit on the north side of the prime vertical upon the hair which is to the left of the collimation centre; then after reversing the instrument, the star may be observed again on the same hair. If the telescope is left in the last position until the star comes to its western transit, it is observed again on the same hair to the south of the prime vertical, and then reversing the telescope the star again crosses the same hair on the north side. Thus a latitude determination is arrived at free from instrumental errors and with the errors of observation greatly reduced. It is best to select a star with as small a declination as possible, as its motion in azimuth will then be more rapid.

C. By an Altitude out of the Meridian.

192. It often happens that just about the time when the sun or star is on the meridian suitable for obtaining the latitude according to method A, it becomes obscured by passing

clouds. If, however, the local time is known approximately,



the latitude can still be obtained in the following way:

Suppose in Fig. 90 PZE is the meridian and S a star which has only a short time before crossed the meridian. Then in the "astronomical triangle" PZS, if we know ZS = co-alt., PS = co-dec. and the hour-angle

ZPS, we can at once, by solving the spherical triangle, find the side PZ= co-lat. But instead of using the common formulæ (as given in Sec. 233), the following will be found simpler:

Make

$$\tan A = \cos ZPS \times \tan PS$$

and

$$\cos B = \cos A \times \cos ZS \times \sec PS$$
.

Then, if the six-o'clock circle and the prime vertical lie on the same side of S, as will always be the case when S is near the meridian.

co-latitude =
$$A - B$$
;

but if S lies between them, we have

co-latitude =
$$A + B$$
.

But since this method is really only suitable for use within an hour or two of the meridian circle, it is the former of these two equations which is almost exclusively used.

When the latitude and declination are of contrary signs, we then have simply

Lat. =
$$(A + B) - 90^{\circ}$$
.

To use this method, it is necessary to know the value of the hour-angle with tolerable accuracy. This can be obtained by one of the methods given in Secs. 195, etc.; or in the case of a star it can easily be obtained by observing its altitude before reaching the meridian,—assuming that it is only cloudy about the time of the meridian passage,—noting the time by an or-

dinary watch; then on the other side of the meridian, if the moment is observed at which it again reaches the same altitude, half the interval (converted into a sidereal interval) = hour-angle H (see Sec. 183). With the sun this is only applicable when its declination is changing but little, or when near the zenith.

D. By double Altitudes.

193. The following are very convenient methods of obtaining the latitude when the local time is not known.

A. By two altitudes and the interval of time between them.— In Fig. 91 let Z be the zenith, P the celestial pole, S and S' the two positions of the star at the moments at which the altitudes and times are observed.

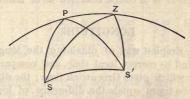


Fig. 91.

Then the interval between the two observations in sidereal time = the hour-angle, which converted into angular measure = SPS'. Then in the triangle PSS', SP = S'P = codeclination; thus we can find SS' and PS'S. Then in the triangle ZS'S, since we have the three sides we can find the angle ZS'S, which, subtracted from PS'S, gives the angle PS'Z. Then in the triangle PS'Z we have S'P, S'Z, and the angle PS'Z, from which we can find PZ = co-latitude.

A good common watch is all that is required to observe the intervals.

But instead of taking two altitudes of the same star, it is better to observe—

B. By simultaneous altitudes of different stars.—The hourangle is given by the difference in R.A. of the two stars, and the rest of the working is the same as above. When, however, there is but one observer, so that the altitudes must be taken in succession, he must proceed thus: The altitude of one star must be taken, and the time noted by the watch; the

altitude of the other star must then be taken, and the time again noted. After a short interval the altitude of the second star must again be taken, and the time noted. He thus finds the motion in altitude of the second star in a given time, from which, by proportion, he can find what its altitude was when the first star was observed.

In both A and B the altitudes as observed must of course be reduced to the true altitudes in order to obtain SZ and S'Z.

194. On the last page of the Nautical Almanac for each year is given a Table for computing the latitude from an observed Altitude of Polaris at any time, the hour-angle being approximately known; and as full instructions accompany the table, these need not be repeated here. The local time being known, the hour-angle H is of course obtained as in Example 5, Sec. 183.

LONGITUDE.

195. The simplest way of obtaining the longitude of a place is to find its correct local time, and compare it with a chronometer which gives Greenwich time; the difference between the two times equals the difference of longitude: so that if we have a chronometer at hand keeping Greenwich time, obtaining the longitude is simply a matter of obtaining the local time.

A. To obtain Local Time by an altitude of a star.

If it were not for the slowness of the motion of a star when near the meridian, a convenient method of obtaining the local time would be to reduce its R.A. to mean time at the moment of its maximum altitude, which would then be the mean local time of its transit. But in order to obtain a well-defined moment of observation, it is necessary for the motion in altitude to be as rapid as possible, and for this reason a star snould be selected as near the prime vertical as possible. Suppose at a certain moment by the chronometer we observe the altitude of a star S (see Fig. 90); then if the latitude is known, in the triangle PZS, since PZ = co-lat. = l, PS = co-dec. = d, and SZ = co-alt. = a, we have, by spherical trigonometry,

$$\cos\frac{h}{2} = \sqrt{\frac{\sin s \sin (s-a)}{\sin d \sin l}},$$

where $s = \frac{a+d+l}{2}$ and h = the hour-angle ZPS; if the dec-

lination and the latitude are of opposite signs, $d = \text{dec.} + 90^{\circ}$.

Now the nearer S is to the prime vertical, the less is an accurate knowledge of the latitude essential, and the less does an error in altitude affect the result. Thus the body should be observed as nearly east or west as possible, and certainly not within an hour or two of its transit.

The following table shows the errors in longitude in minutes of arc involved by an error of 1 minute in latitude, when S is observed at different bearings in different latitudes.

militar in	LATITUDE.											
Bearing.	10°	20°	30°	40°	50°	60°	70°					
10° 20°	5'.67	5'.76 2'.79	6'.55 3'.17	7'.40	8'.82 4'.27	11'.33 5'.49	6'.03 2'.92					
40° 60°	1'.19 0'.58	1'.21 0'.59	1'.38 0'.67	1'.55 0'.75	1'.85 0'.90	2′.38 1′.15	1'.27					
80°	0'.18	0'.18	0'.20	0'.23	0'.27	0'.35	0'.19					

Thus in latitude 30° if the bearing of a star when observed is 80° an error in latitude of 5 miles would only cause an error of about half a mile in longitude.

An error in the altitude is of much more importance, as the following table, giving the errors in longitude in minutes caused by an error of one minute in altitude, shows:

of all ha	LATITUDE.										
Bearing.	10°	20°	30°	40°	50°	60°	700				
10° 30°	5'.91 2'.03	6'.25	6'.65	7'.50 2'.64	8'.96 3'.14	12'.17	16'.87				
50° 90°	1'.32	2'.17 1'.39 1'.06	1'.51 1'.15	1'.71	2'.03 1'.55	3'.98 2'.63 2'.00	5'.84 3'.78 2'.90				

Since the accuracy of the altitude is of great importance, it is well to take several sights, say 3 or 5, within a minute or so of each other, and note the corresponding chronometer readings; the mean altitude may then be considered to correspond with the mean time. If the local time which was used in order to correct the sidereal time at noon for the assumed

longitude is found to have been appreciably in error, allowance must be made for this.

In observing altitude for time, if great accuracy is desirable, it is well to observe both in the east and the west; the mean result of the two sets is thus practically free from instrumental errors. This method of course applies equally well to the sun as to a star; and since the co-declination is always a large arc, whatever error there may be in it, there will only be half that error in the half sum; and since the errors in these altitudes oppose one another, an error in the co-declination such as might arise from an error of two or three degrees in the longitude assumed to correct the sun's declination will not seriously affect the result.

B. To obtain local time by equal altitudes of a star.

196. All that we have to do in this case is to observe the altitude of a star in the east and note the time, then note the time when in the west it again descends to the same altitude. Half the interval between the two observations is the "middle-time," which corresponds with the local sidereal time given by the star's R.A. Thus we have simply to convert the star's R.A. into mean local time and compare it with the middle-time by the watch to obtain the watch-error.

By taking a set in the east and a set in the west, since index or instrumental errors do not enter into the question at all, the mean altitude for the mean time should give a really good result. There is no necessity to apply a correction for refraction, unless the barometric pressure or temperature has changed considerably between the observations.

C. To obtain local time with a transit.

197. The best way to proceed with a transit is to set it in the meridian and observe the time of transit of the sun or one or more stars; the correct local time is then found by merely converting the R.A. of the body at the time of its transit into mean time.

198. But so far in obtaining the longitude we have assumed that we have had at hand a chronometer rated to Greenwich time. But since little reliance can be placed on chronometers

when travelling across country, one of the following methods should be adopted as a check on the chronometer from time to time.

TO OBTAIN THE LONGITUDE BY LUNAR CULMINATIONS.

The principle on which this method of obtaining Greenwich time is based is as follows:

In the Nautical Almanac the moon's R.A. is given for every hour during the year at Greenwich. If then in any other longitude we find the moon's R.A. at a certain moment, that moment will correspond with the time at Greenwich at which the moon would have the same R.A. as that which we observed. Thus, if the moon's R.A. in the Almanac at 6 P.M. were given as 8h, if in a certain longitude we find at exactly 10 P.M. local time the moon's R.A. to be 8h, we know we are in a longitude 4 hours ahead of Greenwich, i.e., 60° E. To obtain the R.A. of any body by observation, we have only to find the mean local time of its transit across the meridian and convert it into sidereal time, which is the R.A. required. Thus we proceed as follows:

Find the correct local time by the watch. Set the transit in the meridian. Observe the moment of transit of the moon's bright limb. Again find the correct local time by the watch, The moon's semi-diameter, which is given for every 12 hours in the Almanac, must then be found and divided by 15 to reduce it to equivalent time, which would then be the sidereal time occupied by its passage if its declination = 0° and its R.A. were unchanging. But since its R.A. is always increasing, the passage of the semi-diameter will occupy a time longer than this by an amount which may be obtained from the Almanac by simple proportion, by seeing what the increase in R.A. is at the assumed Greenwich time of the observation; the total time of the passage so obtained multiplied by the secant of the declination (see Sec. 186) then gives the time actually occupied in the passage; and this added to, or deducted from, the observed time of transit of the limb, gives the time of transit of the moon's centre, which, converted into sidereal time, gives the moon's R.A. at the moment of observation

It is well to take a set of altitudes for time before and after the moon's passage; and the instrument, if possible, should not have less than 3 vertical hairs, the passage across each of which may be observed and reduced to the centre hair.

Every possible precaution should be taken in this observation, for the error of a second of time in observing the moon's limb, compared with the corrected watch time,—i.e., an error of 1 second in R.A.,—may easily cause an error in longitude of 5 miles. Thus by a single observation with a small transit we cannot depend on our longitude to within about 10 miles. But if the observer is stationed for 3 or 4 days at any one place, by taking the mean result of 3 or 4 observations he should be able to obtain the longitude with a probable error, say, not exceeding 4 or 5 miles, corresponding with an error in Greenwich time (in ordinary latitudes) of from 20 to 30 seconds.

Having now obtained the moon's R.A., the next thing to do is to find the hour at Greenwich with which it corresponds.

Since the moon's change in R.A. is usually rapid, and great accuracy is necessary, the ordinary method of simple interpolation will not apply here. The following formula may therefore be used instead:

$$T-t=rac{60\left(A-a
ight)}{D+rac{d}{2}\left(rac{T-t}{3600}
ight)};$$

where T = the hour required;

t = the hour for which R.A. is given in the Almanac, previous to T;

A = R.A. corresponding with T;

a = R.A. corresponding with t;

D =Increase in R.A. in 1 mean minute at time t;

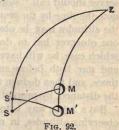
d =Increase in D in 1 mean hour at time t.

If D is decreasing, d is of course negative. In the term involving the unknown value (T-t), the *probable* value must be used, which is correct enough. We thus have the value of the Greenwich time corresponding with the observed local time of the transit of the moon's centre, the difference of which, divided by 15, gives the difference of longitude.

199. TO OBTAIN THE LONGITUDE BY LUNAR DISTANCES.—This method is similar in principle to the preced-

ing one, the difference being that here it is the distance from the moon to some star which is observed instead of its R.A. The present case, since it does not involve the use of a transit and admits of several observations being taken on one night, is more suitable for exploratory work, and is the method altogether used for checking the chronometers at sea. The distances between the moon's centre and certain stars of the first and second magnitude are given in the Nautical Almanac for every three hours at Greenwich, so that it is simply a case of measuring the distance from the moon's limb to a star, and correcting for refraction, semi-diameter, etc., noting the local time of the observation, and then finding from the Almanac what hour at Greenwich corresponds with the corrected distance.

In Fig. 92 let M' and S' be the positions of the moon and star at the moment of observation, and Z the zenith; then M'S'. corrected for semi-diameter, equals the apparent Lunar distance, and M'Z and S'Z the co-altitudes. The true positions will differ from these by the differences in altitude MM' and SS': the moon, on account of the correction for parallax exceeding that for refraction, will be elevated



above its apparent position; whilst the star, on account of refraction only, will be depressed below its observed position.

Now, if the apparent altitudes are observed at the time of observing the lunar distance S'M', we have the three sides of the triangle S'ZM', so that the angle at Z may be found trigonometrically. Then the two sides S'Z and M'Z, being corrected for refraction and parallax, give the sides of the corrected triangle SZM; and since we thus have two sides and the included angle Z, we can calculate the true lunar distance SM. This operation is termed "Clearing the lunar distance."

The following formula, by Borda, is probably the most convenient to use for effecting this:

$$\sin\frac{D}{2} = \cos\frac{H+H'}{2}\cos C,$$

where

$$\sin^2 C = \frac{\cos s \cos (s \sim d) \cos H \cos H'}{\cos h \cos h' \cos^2 \frac{H + H'}{2}},$$

where
$$s = \frac{h + h' + d}{2}$$
,

and h = app. alt. of moon's centre, h' = app. alt. of star; H = true alt. of moon's centre, H' = true alt. of star; d = app. distance S'M', D = true distance SM.

An error of a minute or two in the altitude makes no appreciable difference in the distance.

The vernier should be set to a division easily read off, and at the moment when the distance agrees with this reading the observer should call "stop," at which signal the assistant should note the time by the watch, and at the same instant, if possible, the altitudes may be observed by two assistants. But usually one observer has to do the whole work with the sextant, in which case he will have to observe the altitudes of the moon and star, both before and after the observation, and note the times, and then deduce the altitudes at the time of measuring the distance, by proportion.

But a better way is to spend the time otherwise occupied in observing altitudes, in obtaining a large number of lunar distances and then to *compute the altitudes* as follows:

Since we know the time of each observation, we can obtain the hour-angle at that moment, which, in either the case of the moon or a star, is merely the difference in R.A. of the body and the sidereal time at the moment +24 hours if necessary, the R.A. in the case of the moon being corrected for the time of observation by assuming a probable value for the longitude. Then if L= latitude and d= co-declination,

$$\sin (alt.) = \frac{\sin L \sin (E+d)}{\sin E},$$

where

$$\cot E = \cot L \cos h$$
,

and h = the hour-angle. If h exceeds 90° cos h is negative, which will make cot E also negative; so that to avoid the use

of supplements, it is simpler to say

$$\sin (alt.) = \frac{\sin L \sin (E - d)}{\sin E}.$$

These are of course the true altitudes.

In selecting stars from which to measure the distance, it should be remembered that the mean of two distances, one measured to a star on the right and the other on the left, will be practically free from instrumental errors; so that this plan of observing should always be adopted when possible. It is well, too, to select stars the distances between which and the moon are varying most rapidly,—for there is a considerable difference sometimes between the rates,—and yet at the same time the altitudes should not be less than, say, 10°.

A complete lunar observation should consist of 6 "sets," each set including 3 simple distances; 3 of these sets should be taken to the left of the moon and 3 to the right; also two observations for latitude, one in the north and one in the south, to eliminate instrumental errors; and two sets of observations for time, one to a star in the east and another in the west, one before and the other after the measuring of the distances.

Having thus obtained the mean lunar distance for the mean local time, the corresponding Greenwich time may best be deduced according to the instructions and data given in the Nautical Almanac with sufficient clearness to render any further explanation superfluous, as that work must of necessity be an accompaniment to the observations. Since, however, the Nautical Almanac assumes that the computer has at hand a table of Ternary Proportional Logarithms, such as is given in Chambers' Mathematical Tables or Bowditch's Navigator, it will be well to see how these may be calculated, in the event of such not being the case.

A Proportional Logarithm for any portion of a certain period is merely the difference of the logarithms of the period and of the portion. Thus, taking the period as 3 hours, since lunar distances are given in the Almanac at intervals of every 3 hours, or 10,800 seconds, the logarithm for it = 4.0334; then since the logarithm for 1 hour (= 3600 seconds) = 3.5563, the proportional logarithm for 1 hour = 0.4771. The explorer, however, should provide himself with some portable form of

logarithmic tables if likely to have much of this sort of work to do.

200. Another method of obtaining Greenwich time is by observing with a powerful telescope the local time of the Eclipses of Jupiter's Satellites. But this method, for a variety of reasons, is considerably less reliable than those given above. The Nautical Almanac gives instructions and data as to the manner of obtaining Greenwich time by this method.

TO TEST THE CHRONOMETER RATE.

201. Whenever a halt is made for over 24 hours, it is a very simple matter to check the rate of the chronometer. With a transit this can best be done by setting it in a vertical plane lying fairly north and south, and noting the moments of the passages of 3 or 4 stars. The interval of time before the respective passage of each on the following evening = 23^h 56^m 04^s.9. With a sextant this may best be done by observing the altitudes of 3 or 4 stars lying fairly east or west—their motion being greater in altitude when near the prime vertical—and noting the chronometer times; after the lapse of the above interval, each will again be at the same altitude on the following night.

TO SET THE TRANSIT IN THE MERIDIAN.

202. Three methods of obtaining a north and south line have already been given in Sec. 57; the method by Maximum Elongations of Polaris is the best, for it admits of plenty of time to reverse the instrument and establish a true north and south line. When Polaris is not convenient for this purpose, any other star (which has an elongation) may be used as shown in Note D, Appendix. In the same way, if neither Alioth nor γ Cassiopeia is convenient for observation, other stars may be used as shown in Note E, Appendix. When, however, neither of these methods is exactly suitable, the azimuth of Polaris out of the meridian may be found at any moment by solving the astronomical triangle PZS in Fig. 87, and thus obtaining the angle at Z, which is the azimuth.

To do this we have given the declination, and we must also have two of the following three: latitude, altitude, and hourangle. Since the latitude is most easily obtained, and the

altitude gives the best result if near the elongations, these two should then be used. If, however, the star is near the meridian, the latitude and the hour-angle should be employed.

In the former case we have

$$\cos\frac{Z}{2} = \sqrt{\frac{\sin s \sin (s-d)}{\sin a \sin l}},$$

a, d, and l being the complement of the altitude, declination and latitude respectively, and s the half sum of a, d, and l.

In the latter case we have

$$\cos a = \cos d \cos l + \sin d \sin l \cos h$$
,

from which we obtain

$$\sin Z = \sin h \sin d \csc a$$
.

h = hour-angle. (See Sec. 182.)

When the latitude and declination are of opposite signs, $d = \text{dec.} + 90^{\circ}$.

203. In observing the altitude of the moon for time or latitude, as is often practicable in thick weather when the stars are invisible, and more accurate interpolation of its declination is necessary than is obtained by simple proportion, the method usually adopted for this purpose is that known as INTER-POLATION BY SUCCESSIVE DIFFERENCES. The interpolation formula is

$$F^{\mathbf{n}} = F + \frac{nd_1}{1} + \frac{n(n-1)}{1 \times 2} d_2 + \frac{n(n-1)(n-2)}{1 \times 2 \times 3} d_3 +, \text{ etc.}$$

For example, suppose we wish to find the moon's declination at Greenwich at 2^h 15^m on Nov. 15, 1889.

From the Nautical Almanac we find the declination given for every hour. We select the declination at the hour before the one for which we wish to interpolate (=F), and put it in the first column as below; beneath it we put in order the declinations for, say, 3 or 4 following hours, as given in the Almanac. In the second column we put down the first differences of these (d_1) obtained by subtracting downwards and prefixing the proper algebraic sign. In the third column we place the second difference (d_2) (i.e., the differences of the first differences), and so on.

Now n is the ratio of the fractional period for which we wish to interpolate, to the interval between which the values are given; in this case 15 minutes to 1 hour, therefore $n=\frac{1}{4}$: so that now we have merely to insert the upper values in the columns for d_1 , d_2 , etc., and the above value of n, in order to find the declination at 2^h 15^m .

Dec. at
$$2^{\text{h}} = \frac{F}{18^{\circ} \ 17' \ 4'} \begin{vmatrix} d_1 \\ -7' \ 59'' \\ -8' \ 05'' \\ -8' \ 10'' \end{vmatrix} \begin{vmatrix} d_2 \\ -6'' \\ -8'' \end{vmatrix} \begin{vmatrix} d_3 \\ -6'' \\ -5'' \end{vmatrix}$$

Thus,

$$F^{n} = 18^{\circ} 17' 4'' - 1' 59'' . 8 + .56'' - .07'';$$

therefore,

Dec. at
$$2^h 15^m = 18^\circ 15' 04''.75$$
.

In such a case as the above, as it happens, the simple method of interpolation would have given $F^a = 18^\circ 15' 04''.2$, which of course would have been amply near enough for anything in the way of ordinary work. But where the explorer is desirous of obtaining a really accurate observation this method is often of high value.

204. Adjustment of Observations.—It is a well-recognized fact in practice, when making a series of measurements of any quantity, that after every possible means of eliminating and correcting for instrumental errors have been employed, there still remain certain accidental errors which no experience or skill on the part of the observer can rectify, since the causes to which they are due are themselves unknown. Thus it happens that each measurement in the set may be different, although, judging from the care taken in observing each and the apparent similarity of the conditions under which they were taken, no such differences should exist. The question then arises as to what is to be taken as the most probable result.

Now according to the Theory of Least Squares, the method usually adopted for the solution of these problems, the most probable value of any number of measurements of the same quantity, each measurement being considered to be equally reliable, is that which makes the sum of the squares of the

"errors" a minimum; and the value which does so is the arithmetical mean of all the measurements. The "error" in the case of each measurement being its difference from the mean.

But it often happens that the circumstances under which the several measurements are made are such as to warrant greater "weight" being given to some of them than to others. These weights are often deduced from the observations themselves, or from them in connection with a special series of observations; but in ordinary field practice, weights assigned arbitrarily after a thoughtful perusal of all the attendant circumstances are more likely to be of value than those found by a strict application of the formulas of Least Squares. Weights being thus assigned, the most probable value of the results will be found by multiplying each observed value by its weight, and dividing the sum of the products by the sum of the weights, the result being that value which renders the sum of the products of the squares of the errors and the respective weights a minimum. And this value is termed the Weighted Mean. This may be best illustrated by an example.

Suppose that we have, as several corrected measurements of a base, the following numerators, and that, considering all the attendant circumstances, we have assigned to each the weight shown as its denominator, assuming, for the sake of simplicity, that the weight of the least reliable is expressed by unity:

$$\frac{2056.32 \text{ feet}}{1}$$
, $\frac{2056.20 \text{ feet}}{4}$, $\frac{2056.16 \text{ feet}}{3}$.

Then the most probable value of the result is given by

$$\frac{2056.32 + (2056.20 \times 4) + (2056.16 \times 3)}{1 + 4 + 3} = 2056.20.$$

A fair test of precision in dealing with a set of measurements is afforded by means of the "probable error" of a single determination, which is found by taking the difference between each individual result and the mean, squaring these quantities, and dividing their sum by (n-1) where n represents the number of individual results; then, on extracting the square root of this quotient and multiplying by 0.674, we

obtain the so-called Probable Error. But this term does not mean that that error is more probable than any other, but merely that in a future observation the probability of committing an error greater than the probable error is equal to the probability of committing an error less than the probable error.

The probable error of the arithmetical mean may be similarly found, the value n(n-1) being substituted for (n-1) in the rule given above for a single determination.

Errors in excess are considered positive; those in defect, negative.

205. Having now examined the various methods of obtaining positions on exploratory surveys, we next come to the subject of ascertaining the bearings and distances of these positions relatively to each other or to other points, when taking into consideration the curvature of the earth's surface.

From what has already been said in Sec. 58 on the subject of the Convergence of the Meridians, we can see what form the corrections will have to take in order to allow for the spherical—or more correctly spheroidal—form of the earth; and now, by means of 3 or 4 simple problems, we can obtain all the formulæ necessary for the construction of the groundwork of a map, or the calculation of courses, which are ever likely to be needed in connection with exploratory surveys.

In Engineering Geodesy it is usually sufficiently accurate to assume the earth to be a sphere, the radius of which equals the mean radius of curvature of the spheroid; but it may be as well here to examine the subject roughly, in order that the engineer may have an idea of the extent of the errors which this assumption involves.

206. THE FIGURE OF THE EARTH.—According to Col. Clarke,

the mean Equatorial semi-axis = 20926202 feet, and the Polar Semi-axis = 20854895 feet.

Also the radius of curvature in the direction of the meridian in any latitude L equals in feet

and the radius of curvature in a direction perpendicular to the meridian equals in feet

$$r = 20961932 - 35775 \cos 2L + 46 \cos 4L$$
.

Thus at the Equator

$$R = 20783832$$
 feet, $r = 20926203$ feet;

and at the poles

$$R = 20890564$$
 feet, $r = 20961932$ feet.

So that for engineering purposes we may take 20,890,000 feet as the mean radius of curvature. Again, according to the same authority, the length of a degree of latitude equals in feet

$$D = 364609.1 - 1866.7\cos 2L + 4\cos 4L,$$

and the length of a degree of longitude equals in feet

$$d = 365542.5 \cos L - 311.8 \cos 3L + 0.4 \cos 5L$$
.

The value of the foot taken above is the English standard, which is less than the American standard in the ratio of 1 mile to 1 mile and 3.677 inches.

For rough work we may consider

$$D = 364000$$
 feet and $d = D \cos Lat$.

Table XVIII gives the true values of 1 minute of arc, to the nearest foot.

207. Now from the formula for the length of a circular arc given in Sec. 73, if we take the above value of the mean radius of curvature, we find the length of an arc on the earth's surface in feet equals

$$l = 6076n$$
 (nearly),

where n = the number of minutes in the arc; and the converse of this,

$$n = \frac{l}{6076} \text{ (nearly)},$$

enables us to convert any given distance into its equivalent in angular measure.

If it is desirable to obtain the value of l more accurately than by this means, we can do so by obtaining first the value of l in the direction of the meridian, either from Table XVIII, or more correctly by dividing the value of D, given in Sec. 206, by 60. Also the length of a 1' arc perpendicular to the meridian is needed, which may be obtained by means of the value of r, given in Sec. 206. Then if we call this latter value l', the length of an arc subtending 1' at the earth's centre, which makes an angle A with the meridian, equals

$l\cos^2 A + l'\sin^2 A$.

208. Given the latitude and longitude of two places to obtain their distance apart, and the bearing of the course joining them.—Suppose A and D in Fig. 12 are the two given places, then the arc AF and the arc ED represent their latitudes. Then in the spherical triangle AND, since N = difference of longitude, and AN and ND are equal to the co-latitudes of A and D, we can find AD thus:

$\cos AD = \sin a \sin d + \cos a \cos d \cos AND,$

where a and d are the latitudes of A and D. And the bearing of the arc AD, which at A is represented by the angle NAD, is then given by the equation

$\sin A = \cos d \csc AD \sin AND.$

Or, if A and D are in the same latitude, we have

$\tan A = \cot \frac{1}{2}AND$ cosec lat.

The arc so obtained can be converted into feet as shown in Sec. 207; and this is the distance along the arc of the great circle passing through A and D, i.e., the shortest distance between them on the earth's surface.

Conversely, given the latitude and longitude of A, and the bearing and distance of another place D, to find the latitude and longitude of D.—First convert AD into angular measure according to Sec. 207; then we have the sides

AD, AN, and the included angle A. Then to find d we have

 $\sin d = \cos AD \sin a + \sin AD \cos a \cos A$.

Then AND, the difference of longitude, is given by

 $\sin AND = \sin A \sin AD \sec d$.

The bearing of AD at D may be obtained from the equation

 $\sin D = \sin AND \cos a \csc AD$.

The formulæ given in this section are simply those ordinarily used for the solution of spherical triangles. (See Sec. 233.)

209. To find the radius of a Circle of Latitude.-In

Fig. 93 let C be the centre of the earth, N the pole, and L any given latitude; then, considering the earth to be a sphere, the angle LPC= the latitude of L, so that

PL = LC cot latitude,

where PL = radius of the circle of latitude. LC may be taken as equal to 20,890,000 feet.

point C to a parallel of latitude AC from a straight line AB, tangent to AC at A.—We can do this by treating the parallel of latitude AC in Fig. 94 as a curve Fig. 93. to which the arc of a great circle AB is tangent at A, and thus

obtain the offset *CB* according to Sec. 78; or, we can solve the right-angled spherical triangle *ANB*, and so find the latitude of *B*, if we know the differ-

ence of longitude N, thus:

tan (lat. B) = tan (lat. A) cos N.CB then equals the difference of latitude of A

and B:

211. We are now in a position to consider the influence of the spherical form of the earth, assuming for the moment the earth to be a

Fig. 94. sphere, on a map the linear measurements of which have been computed on the supposition that the surface of the earth is a plane.

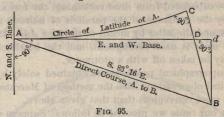
Now a spherical surface cannot be developed on a plane surface, but can only be developed on a sphere of equal radius, Thus no map can, theoretically even, be correct to the same scale in all its parts. In nautical charts, which are generally made on Mercator's Projection, this difficulty is overcome by the use of a scale of meridional parts, the scale at all points being proportional to the secant of the latitude. And this is a very convenient method, where all positions are obtained astronomically and where the error involved by calculating the courses according to "Middle Latitude Sailing" is of no importance. But in constructing a map this method is inconvenient; for if the same scale is used throughout, it assumes that parallels of latitude are right lines, and that there is no convergence of the meridians. In plotting exploratory surveys, simplicity is an important factor; also, the map must be adapted to the same scale throughout, and be so arranged as to be suitable to the plotting of topography as on a plane surface. To approximate as near as possible to correctness in the more important portions, and to throw the excess of error into the less important parts, is the best that can be done under any circumstances.

212. In Sec. 58 we referred to the corrections which it was necessary to make on account of the convergence of the meridians. By extending this method we are able, with the aid of the preceding problems, to construct the groundwork of our map without any other principles than those already explained. The best way is to take an example and work it out as if in actual practice.

Suppose from A in Latitude 60° N. and Longitude 120° W. we intend starting off straight across country for B, a place which, from the maps, we find to be situated in about Lat. 59° N. and Long. 110° W., and wish before starting to lay out the groundwork of a map to be constructed from the knowledge of the topography which we intend to obtain on the way—that we may have some reliable means of plotting our results as soon as obtained, and also of determining positions relatively to each other by means of bearings and distances.

At A we draw, as in Fig. 95, the base-lines AS and AD. Then find the length of AC from Table XVIII, calculating as if it were in the mean latitude of A and B, i.e., 59° 30′ N.; thus AC = about $10 \times 60 \times 3095$ = say 1,857,000 feet. If

great accuracy were required, we could find the value of d in latitude 59° 30′ according to Sec. 206, then AC = 10d.



Next we make AD = AC, and through D draw the meridian CB, the bearing of which on the map, relatively to A, = the convergence between A and $B = 8^{\circ}$ 36'. Therefore the angle $CDA = 81^{\circ}$ 24'.

The length of the offset CD may be found according to Sec. 78, and is equal to about 140,000 feet; and since B lies 1° to the south of C, and on the meridian passing through D, we have DB = about 225,400 feet. Then by solving the plane triangle ADB, we obtain AB = 1,903,800 feet, and the angle $BAD = 6^{\circ}$ 44′. Thus the direct course from A to B is S. 83° 16′ E., and Ad = "Total departure" = $AB \cos 6^{\circ}$ 44′ = 1,890,700 feet, and Bd = "Total latitude" = $DB \cos 8^{\circ}$ 36′ = 222,800 feet.

We have thus the groundwork of our map ready for the plotting of the courses, and if we use sheets of cross-section paper, with 10 divisions to the inch, and plot to a scale of 10,000 feet to an inch, we then have a map of tolerably convenient size, plotted to a scale sufficiently large to show the main features of the country, since any important parts which may have been made the subjects of special survey can be best shown separately.

In order to connect the Astronomical work with that which is plotted by Latitudes and Departures, or by protractor, and which we may call our "dead-reckoning," we must draw meridians and curves of latitude at about every 30'. To fill in these meridians, divide AC equally into 20 parts, and draw the meridians perpendicular to the curve at each of these points, i.e., dividing up the convergence equally among them. The curve of latitude AC, since we know the distance CD, can be drawn by assuming that the offset half-way between A and D = 4CD, and so on, according to Sec. 78.

The advantages of this method of plotting are, that we can readily connect positions taken by astronomical observations with those calculated from dead-reckoning, the former being plotted by the guidance of the parallels of latitude and the meridians, and the latter by means of the base Ad. Also, that the same scale is used throughout, and the bearings of all points may be taken off with a protractor.

If the topographical positions are obtained solely by direct astronomical observations, then the method of Mercator's Projection is more convenient than that given above.

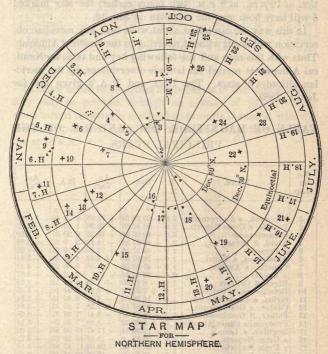
To plot our route we proceed as follows: Suppose we take rough compass courses; these we plot lightly on the map, having worked them out, say, by Latitudes and Departures, correcting the "latitudes" absolutely according to any latitude observations we may take, the "departures" being guided to a reasonable extent by the observations for longitude. Thus our course is constantly being broken, involving a new "total latitude" for each fresh start. This we can best find by scaling from Ad, after having plotted the position astronomically. At the end of our journey, whatever error in longitude we may have, may usually be divided up proportionally along the whole route, if the trip has been made at a tolerably uniform pace. The error in latitude should be inappreciable.

The above example shows what must be considered in plotting an extensive survey; and though a more rough and ready method is usually correct enough, yet where the field-work is run in such a way as to warrant a tolerably accurate plot of it being made, the little extra time involved in making a good map is time well spent.

As regards the mode of procedure in keeping a course astronomically, Col. Frome says: "It is probably inconvenient always to obtain latitude at noon, but we can generally do so, and more correctly, at night by the meridian altitude of one or more of the stars. The local time can immediately before or after be ascertained by a single altitude of any other star out of the meridian—the nearer the prime vertical the better; and if a pocket-chronometer is carried, upon which any dependence can be placed, the explorer has thus the means, by comparison with his local time, of obtaining his approximate longitude, and laying down his position on paper. The longitude should also be obtained occasionally by Lunar Dis-

tances, or some other method. The latitude he should always get correct to half a mile, and the longitude to 8 or 10 miles,"

213. The Star Map given below will be found convenient in selecting suitable stars for observations. The stars are plotted from their R.A.'s and Decs. in the same way that a map of the earth is plotted by longitudes and latitudes, i.e., looking down on it.



The centre is the celestial pole, and the 24 radiating lines divide the 24 hours of R.A. Now the initial point for R.A. being on the meridian at 10 P.M. about Oct. 21, we can divide the circle into 12 divisions, and arrange them so that the radiating line marked 0 *Hours* will cut the 10-o'clock division about two thirds along it. Thus we read off that about Oct. 21 the star marked 1 will be on the meridian, i.e., due south, at

10 P.M. Similarly the star marked 23 will be on the meridian at 10 P.M. about Aug. 17.

But suppose we want to know what star will be near the meridian about 8 P.M. on Jan. 10. Imagine the margin of the map, with the months marked on it, to be stationary, and the interior portion to rotate in the same direction as the hands of a watch, once in $23^{\rm h}$ $56^{\rm m}$; then, since the map shows the position at 10 p.m., at 8 P.M. (two hours earlier) the star marked 5 will have been near the meridian on Jan. 10.

In this way we can tell at about what time any meridian observation will occur without referring to the Nautical Almanac. Thus with this map and the following key and table no Nautical Almanac is needed for latitude observations, by the meridian altitudes of stars. The Decs. and R.A.'s given are for Jan. 1, 1889.

TABLE OF MAGNITUDE, DEC., AND R.A. OF THE PRINCIPAL STARS.

No. in Map.	NAME.		Dec.	An. Var.	R.A.	An. Var.
1 2 3 4 5 6 7 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26	Alpherat, a Andromedæ Polaris, a Ursæ Minoris. y Cassiopeiæ Algol, ß Persei. a Persei Aldebaran, a Tauri. Capella, a Aurigæ. a Arietis Rigel, ß Orionis. Betelgeuze, a Orionis. Sirius, a Canis Majoris. Castor, a Geminorum. Procyon, a Canis Minoris Regulus, a Leonis a Ursæ Majoris. y Ursæ Majoris. y Ursæ Majoris. y Ursæ Majoris. Arcturus, a Bootis. Spica, a Virginis. Antares, a Scorpii. Vega, a Lyræ Altair, a Aquilæ. a Cygni. Fomalhaut, a P. Aust. Markab, a Pegasi.	2.00 2.07 2.00 1.00 1.00 1.00 1.31 1.00 1.32 2.00 2.33 2.00 1.00 1.31 1.00 1.31 1.00 1.31 1.00 1.31 1.00 1.00	** / '/' + 28 28 39 - 88 42 59 - 60 65 55 - 40 31 38 - 49 27 56 14 - 8 19 50 - 16 33 52 - 16 33 52 - 32 07 53 - 28 17 37 - 5 30 32 - 12 30 32 - 12 30 45 - 10 34 52 - 30 12 30 - 10 34 53 -	+ 19.88 + 18.90 + 19.56 + 14.12 + 13.10 + 7.52 + 4.03 + 17.7 + 4.40 + 0.95 - 8.41 - 8.99 - 17.47 - 19.36 - 20.03 - 18.08 - 18.08 - 18.09 - 18.90 - 18.	1 18 08 0 50 50 50 50 50 50 50 50 50 50 50 50 5	8.

IN THE SOUTHERN HEMISPHERE WE ALSO HAVE—

NAME.	Mag.	Dec.	An. Var.	R.A.	An. Var.
β Hydri Achernar, a Eridani Canopus, a Argus β Argus α Crucis β Centauri α Centauri α Trianguli Aust α Ophiuchi α Gruis	3.0 1.0 1.0 1.5 1.0 1.0 2.0 2.0 2.0	0 / // - 77 52 46 - 57 48 03 - 52 38 07 - 69 15 36 - 62 29 02 - 59 50 14 - 60 22 47 - 68 49 21 + 12 38 29 - 47 29 53	" + 20.28 + 18.36 - 1.87 - 14.80 - 20.01 - 17.59 - 15.38 - 7.16 - 2.87 + 17.25	h. m. s. 0 19 54 1 33 34 6 21 29 9 11 59 12 20 26 13 55 59 14 32 05 16 36 55 17 29 47 22 01 14	S. + 3.23 + 2.23 + 1.33 + 0.68 - 3.29 + 4.18 + 4.05 - 6.30 + 2.78 + 3.81

In order better to recognize the positions of the stars at night, they may be pricked through on a sheet of paper, which, when turned backwards and held up towards the south, with the month at the lowest part, will correspond with the face of the sky at 10 P.M.

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to see the court of the second of 100 pag. Then II a start to the

PART IV.

MISCELLANEOUS.

THE following miscellaneous information may at times be found of service in the field to both the engineer and the explorer:

214. To find the Horse-power of Falling Water.

$$H.P. = 0.00189 \ QH$$

where Q = the number of cubic feet of water passing over the fall per minute, and H = height of fall in feet.

Turbines can utilize about 75 p. c. of this H.P. Thus the *Effective* horse-power, i.e., available for useful work, = about

.0014 QH.

215. To gauge a stream, roughly. Take some body, which, when floating, will be almost entirely immersed, and throw it into the middle of the stream, in a part, if possible, unobstructed by reeds, etc., and free from slack-water, eddies, or counter-currents; and where the cross-section of the stream is fairly uniform. Observe the time T in seconds which the body takes to float a distance of 100 feet. Then if A= the cross-section of the stream in square feet, and Q= cubic feet of water that pass per minute,

$$Q = \frac{5000A}{T}.$$

This assumes that the middle surface velocity is to the mean velocity as 6 to 5, which is a fairly average ratio.

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216. The Sustaining power of ordinary wooden piles in lbs. equals

 $\frac{FW}{8S}$

where

F = fall of hammer in inches, W = weight of hammer in lbs.,

S = space driven by last blow in inches.

This formula is generally found to give results about as reliable as any general formula *can* give.

217. Supporting power of various materials.

Firm Rock 10.0 "

These are the pressures to which the above may usually be safely loaded.

218. Transverse strength of rectangular beams.

Let L = length of beam in feet between points of support,

b =breadth of beam in inches,

d =depth of beam in inches,

W =Load at centre of beam in lbs.,

f = coefficient of modulus of rupture.

Then

$$W = \frac{bd^2f}{18L}$$
; $d = \sqrt{\frac{18WL}{bf}}$; and $b = \frac{18WL}{d^2f}$.

For the values of f see following table.

For example, if b=6", d=10", and L=20 feet, if we take f=10,000 lbs., by the above formula W=16,666 lbs.; so that with a Factor of Safety of 6 we may safely load it at its centre, and consequently at any part of it, with a weight of 2778 lbs.

A beam will carry as a centre load only half the weight that it will bear distributed uniformly over it. So that, for instance, if we wish to know what total breadth we must give to a set of stringers, where d=16", in order safely to carry an ordinary train over a span of 15 feet, if we take f=10,000 lbs. and the

load per foot run as equivalent to 4000 lbs., we have as the equivalent value of W, 30,000 lbs. So that by the above formula b = about 3 inches. Therefore, taking a factor of safety of 8, b = about 24 inches; so that four $6'' \times 16''$ stringers may safely be used. The factor of safety usually adopted for wood varies from 5 to 10, according to the condition of the timber, the amount of impact caused by the load, and the possible amount of decay to which it will be subjected.

For spans, in railroad bridges, less than 10 feet, 5000 lbs. per foot run should usually be taken as the uniformly distributed load. In spans exceeding 15 feet 3500 lbs. is usually sufficient. These values take no account of the weight of the beams themselves.

VALUES OF f.

Material.	Lbs. per sq. in.	Material.	Lbs. per sq. in.
AshBirchBlue Gum	11,700 18,000	Red Pine Spruce Brit. Oak Am. Red Oak	7100 to 9500 9900 to 12,300 12,000 10,600

219. Natural Slopes of Earths.

Material.	Slope.	Material.	Slope.	Material.	Slope.	
Gravel Dry Sand Sand	40° 38° 22°	Vegetable Earth Compact Earth Shingle	28° 50° 39°	Ruble	45° 45° 16°	

220. Weight of Earths, Rocks, etc., per cubic yard.

Material.	Weight in lbs. per cu. yd.	Material.	Weight in lbs. per cu. yd.	Material.	Weight in lbs. per cu. yd.
Sand	3360	Clay	3470	Quarts	4590
Gravel	3360		4030	Granite	4700
Mud	2800		4370	Trap'	4700
Marl	2900		4480	Slate	4810

A cubic yard of water weighs about 1680 lbs.

221. Weight of Timber and Metals per cubic foot.

11 12 VB	Material.	Weight in lbs. per cu. ft.	Material.	Weight in lbs. per cu. ft.	Material.	Weight in lbs. per cu. ft.
I	Elm, English . Canadian Elm Maple English Oak American Oak	35 45 42 48 50	Pine, red "white Teak Spruce Larch	50	Iron, cast wrought Steel Copper Lead	450 482 490 550 710

222. Mortar. Cement. etc. (common mixtures).

Mortar. -1 of lime to 2 or 3 of sharp river sand.

Coarse Mortar.—1 of lime to 4 of coarse gravelly sand.

Concrete. -1 of lime to 4 of gravel and 2 of sand.

Hydraulic Mortar.—1 of blue lias lime to $2\frac{1}{2}$ of burnt clay, ground together.

Beton.—1 of hydraulic mortar to 1½ of angular stones.

Cement.—1 of sand to 1 of cement; or if great tenacity is required the sand may be omitted.

Portland Cement is composed of clayey mud and chalk ground together and afterwards calcined at a high temperature, and then ground to a fine powder.

NOTES.—For ordinary engineering work the following proportions make a good mortar:

1 measure of Lime;

3 to 5 measures of sand, according to the "hunger" of the sand, 1 measure of ashes, brick dust, or burnt clay.

For engineering work, if exposed to dampness, $\frac{1}{4}$ of the lime in the above should be replaced by hydraulic cement; whilst for work under water, 1 measure hydraulic cement to 2 measures of sand make a good mixture.

NOTES ON TIMBER.

223. Selection of standing trees.—"Scribner's Log Book."—"The principal circumstances which affect the quality of growing trees are soil, climate, and aspect.

"In a moist soil the wood is less firm, and decays sooner than in a dry, sandy soil; but in the latter the timber is seldom fine: the best is that which grows in a dark soil, mixed with stones and gravel. This remark does not apply to the poplar, willow, cypress, and other light woods which grow best in wet situations.

"Trees growing in the centre of a forest or on a plain are generally straighter and more free from limbs than those growing on the edge of the forest, in open ground, or on the sides of hills; but the former are at the same time less hard. The toughest part of a tree will always be found on the side next the north. The aspect most sheltered from prevalent winds is generally most favorable to the growth of timber. The vicinity of salt water is favorable to the strength and hardness of white oak.

"The selection of timber trees should be made before the fall of the leaf. A healthy tree is indicated by the top branches being vigorous, and well covered with leaves, the bark is clear, smooth, and of a uniform color. If the top has a regular, rounded form; if the bark is dull, scabby, and covered with white and red spots, caused by running water or sap,—the tree is unsound. The decay of the uppermost branches and the separation of the bark from the wood are infallible signs of the decline of the tree."

224. Defects of Timber Trees (especially of oak).—"Sap, the white wood next to the bark, which very soon rots, should never be used, except that of hickory. There are sometimes found rings of light-colored wood surrounded by good hard wood; this may be called the second sap: it should cause the rejection of the tree.

"Brash-wood is a defect generally consequent on the decline of the tree from age; the pores of the wood are open, the wood is reddish-colored, it breaks short without splinters, and the chips crumble to pieces.

"Wood which has died before being felled should in general be rejected; so should knotty trees, and those which are covered with tubercles, etc.

"Twisted wood, the grain of which ascends in a spiral form, is unfit for use in large scantling; but if the defect is not very decided, the wood may be used for naves, and for some light pieces

"Splits, checks, and cracks, extending towards the centre, if deep and strongly marked, make the wood unfit for use, unless it is intended to be split. "Wind-shakes are cracks separating the concentric layers of wood from each other; if the shake extends through the entire circle, it is a ruinous defect."

225. Felling Timber.—"The most suitable season for felling timber is that in which vegetation is at rest, which is the case in midwinter and in midsummer; recent opinions derived from facts incline to give preference to the latter season. The tree should be allowed to attain its full maturity before being felled; this period in oak timber is generally at the age of from 75 to 100 years, or upwards, according to circumstances. The age of hardwood is determined by the number of rings which may be counted in a section of the tree.

"The tree should be cut as near the ground as possible, the lower part being the best timber. The quality of the wood is in some degree indicated by the color, which should be nearly uniform in the heart wood, a little deeper toward the

centre, and without transitions.

"Felled timber should be immediately stripped of its bark, and raised from the ground.

"As soon as practicable after the tree is felled the sap-wood should be taken off and the timber reduced, either by sawing or splitting, nearly to the dimensions required for use.

"The best method of preventing decay is the immediate removal of it to a dry situation, where it should be piled in such a manner as to secure a free circulation of air around it, but without exposure to the sun and wind. When thoroughly seasoned before cutting it up into small pieces, it is less liable to warp and twist in drying. When green, timber is not so strong as when thoroughly dry.

"Lumber containing much sap is not only weaker, but decays much sooner than that free from sap."

226. Seasoning and Preserving Timber.—"For the purpose of seasoning, timber should be piled under shelter, where it may be kept dry, but not exposed to a strong current of air; at the same time there should be a free circulation of air about the timber, with which view slats or blocks of wood should be placed between the pieces that lie over each other, near enough to prevent the timber from bending. The seasoning of timber requires from two to four years, according to its size.

"Gradual drying and seasoning in this manner is considered the most favorable to the durability and strength of timber.

"Timber of large dimensions is improved by immersion in water for some weeks. Oak timber loses about one fifth of its weight in seasoning, and about one third of its weight in becoming dry."

227. Decay of Timber.—There are three principal causes of decay of timber—dry-rot, wet-rot, and the "teredo navalis" and other worms.

Dry-rot does not usually occur where there is a free circulation of air, and if the timber is properly dried an occasional immersion in water should do no harm. Timber kept dry and well ventilated has been known to last for several hundred years without apparent deterioration. Dry-rot is caused by a species of wood fungus—Merulius lachrymans—which destroys the tensile and cohesive strength, gradually converting the timber into a fine powder.

Wet-rot.—This is the destructive agent at work more or less on all timber freely exposed to air and moisture. It is of two kinds:

A. Chemical.—In this case a slow combustion takes place, and by a gradual process of oxidation the wood slowly rots away.

B. Mechanical.—This is the more common form, and generally occurs near the water-line in timber subject to frequent immersion. It is the frequent alternate conditions of moisture and dryness that are most trying to timber, as is the case with metals. When timber is constantly under water, the action of the water dissolves a portion of its substance, which is made apparent by its becoming covered with a coating of slime, and this protects the interior. If, however, it is exposed to alternations of moisture and dryness, as is the case with piles in tidal waters, the dissolved parts being continually removed by evaporation and the action of the water, new surfaces are being frequently exposed for decomposition.

Piles driven in sea-water are frequently destroyed by the "teredo navalis," and also by another species of worm called the "limnoria." They both work from about the high-water mark to the surface of the mud.

228. To test Steel and Iron. — Scientific American.— Nitric acid will produce a black spot on steel; the darker the spot the harder the steel. Iron, on the contrary, remains bright if touched with nitric acid.

Good steel in its soft state has a curved fracture and a uniform gray lustre; in its hard state, a dull, silvery, uniform white. Cracks, threads, or sparkling particles denote bad quality.

Good steel will not bear a white heat without falling to pieces, and will crumble under the hammer at a bright-red heat, while at a middling heat it may be drawn out under the hammer to a fine point. Care should be taken that before attempting to draw it out to a point the fracture is not concave; and should it be so, the end should be filed to an obtuse point before operating. Steel should be drawn out to a fine point and plunged into cold water; the fractured point should scratch glass. To test its toughness, place a fragment on a block of cast-iron; if good, it may be driven by a blow of a hammer into the cast-iron; if poor, it will crush under the blow.

Tests of Iron.—A soft tough iron, if broken gradually, gives long silky fibres of leaden-gray hue, which twist together and cohere before breaking.

A medium even grain with fibres denotes good iron. Badly refined iron gives a short blackish fibre on fracture. A very fine grain denotes hard steely iron, likely to be cold-short and hard.

Coarse grain with bright crystallized fracture or discolored spots denotes cold-short, brittle iron, which works easily when heated and welds well. Cracks on the edge of a bar are indications of hot-short iron. Good iron is readily heated, is soft under the hammer, and throws out few sparks.

229. Strength of Rope.—The table on following page gives some idea of the strength of ordinary Manilla Rope.

It must be remembered that these values are for new ropes and that a few months' exposure to the weather will probably cause a decrease in the strength of 40 or 50 p. c. A factor of safety of 4 or 5 is generally employed to obtain their safe working strength.

Ropes made of good Italian hemp are considerably stronger than these.

TABLE OF MANILLA ROPE-3 STRANDS.

Size of Rope.		Breaking-	Size of	F ROPE.	Breaking-
Diam. in inches.	Circum. in inches.	strength in lbs.	Diam. in inches.	Circum. in inches.	strength in lbs.
1	0.71 1.43	375 1,500	21/2	7.14 8.57	37,500 54,000
1	2.14 2.86	3,380 6,000	31/3 4	10.0	73,600 96,000
1½ 1½ 2	3.57 4.28 5.70	9,380 13,500 24,000	2½ 3 3½ 4 4½ 5	12.1 14.2 17.1	121,000 150,000 216,000

Wire Ropes.—The following table gives the strength of iron and cast-steel wire rope:

TABLE OF IRON AND CAST-STEEL WIRE ROPE.

Size of Rope.			AKING- TH IN LBS.	Size of Rope.		BREAKING- STRENGTH IN LBS.	
Diam. in In.	Circum. in In.	Iron.	C. Steel.	Diam. in In.	Circum. in In.	Iron.	C. Steel.
1 2	1½ 2¼ 3⅓	6,960 17,280	15,000 36,000	1½ 1½ 2	48 51 6	78,000 108,000	154,000 212,000
1 11	31/8 4	32,000 54,000	66,000 104,000	2 2 1 2 1 2 1 1 2 1 1 1 1 1 1 1 1 1 1 1	6	130,000 148,000	250,000 310,000

These ropes have 19 wires to the strand and hemp centres. One fifth of the above breaking-strength may be taken as the safe working strength.

For the strength of Iron Rods see Sec. 138.

230. Properties of the Circle.

Diameter \times 3.14159 = circumference.

Diameter × .886226 = side of an equal square.

Diameter × .7071 = side of an inscribed square.

Diameter² × .7854 = area of circle.

Radius × 6.28318 = circumference.

Circumference × .31831 = diameter.

Circumference = 3.5449 V area of circle.

Diameter = 1.1283 V area of circle.

Length of arc = number of degrees × 0.017453 radius

Are of 1° to rad. 1 = 0.01745329.

Arc of 1' to rad. 1 = 0.000290888. Arc of 1' to rad. 1 = 0.000004848.

Degrees in arc whose length = radius = $57^{\circ}.2957795$.

 $\pi = 3.1415926536$; $\text{Log } \pi = 0.4971499$.

231. PLANE TRIGONOMETRY.-In Fig. 96, if the

angle $GAE = 90^{\circ}$; then in the rightangled triangle ABC, if AB = Radius = unity,

eunity, $BC = \sin A; \qquad AF = \operatorname{cosec} A;$ $AC = \cos A; \qquad CE = \operatorname{versin} A;$ $DE = \tan A; \qquad BH = \operatorname{co-versin} A;$ $AD = \sec A; \qquad BD = \operatorname{exsec} A;$ $GF = \cot A; \qquad BF = \operatorname{co-exsec} A.$ Fig. 96.

Therefore

$$\sin A = \frac{BC}{AB};$$
 $\cos A = \frac{AC}{AB};$ $\tan A = \frac{BC}{AC};$

$$\operatorname{cosec} A = \frac{AB}{BC}; \quad \operatorname{sec} A = \frac{AB}{AC}; \quad \operatorname{cot} A = \frac{AC}{BC},$$

Thus,

$$\sin A = \frac{1}{\csc A};$$
 $\cos A = \frac{1}{\sec A};$ $\tan A = \frac{1}{\cot A}.$

An angle and its Supplement have the same Sine and Cosecant; but the Tangents, Secants, Cosines and Cotangents, though of equal length, are of contrary signs: so that in applying to obtuse angles trigonometrical formulæ which were originally intended for acute angles, the algebraic signs of the tangents, secants, cosines, and cotangents must be reversed.

The sine, secant, and tangent of an angle A are respectively equal to the cosine, cosecant, and cotangent of its complement (i.e., of $90^{\circ} - A$).

$$AB^2 = AC^2 + BC^2;$$
 $B = 90^{\circ} - A.$
Area of triangle $= \frac{AC.BC}{2}.$

Examples of Right-angled Triangles: 1. Given $A = 30^{\circ}$, and AC = 100, find BC.

We see above that $\tan A = \frac{BC}{AC}$; therefore

$$BC = AC \tan A = 57.73$$
.

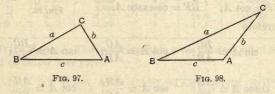
2. Find the sine of 128°.

Since $\sin (180^{\circ} - A) = \sin A$,

$$\sin 128^\circ = \sin (180^\circ - 52^\circ) = \sin 52^\circ$$

which from the tables we find = 0.788.

Solution of Oblique-angled Triangles.



$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}. \qquad (1)$$

$$\tan\frac{A-B}{2} = \frac{a-b}{a+b}\tan\frac{A+B}{2}. \qquad (2)$$

$$A = \frac{A+B}{2} + \frac{A-B}{2} \dots \dots (3)$$

$$B = \frac{A+B}{2} - \frac{A-B}{2}. (4)$$

$$c = (a+b)\frac{\cos\frac{A+B}{2}}{\cos\frac{A-B}{2}}. \qquad (5)$$

Let
$$\frac{a+b+c}{2} = s$$
; then

vers
$$A = \frac{2(s-b)(s-c)}{bc}$$
. (6)

$$\cos\frac{A}{2} = \sqrt{\frac{s(s-a)}{bc}}.$$
 (7)

Area of triangle =
$$\sqrt{s(s-a)(s-b)(s-c)}$$
. (8)

$$=\frac{ab}{2}\sin C. \qquad (9)$$

$$=\frac{a^2\sin B\sin C}{2\sin A}.\qquad (10)$$

$$A = 180^{\circ} - (B + C)$$
. . . . (11)

The above formulæ are all that are required for the ordinary solution of plane triangles.

Remarks.—Though such a formula as No. 2 simply mentions A and B and their opposite sides, it holds equally well whether we substitute C for A, or C for B, provided that the sides are changed to correspond also. In Equations 2, 3, 4, and 5, A is intended to represent the *greater* angle of the two angles A and B.

Examples .-

1. Given A, B, and b, find A.

By Equation 1,

$$a = \frac{b \sin A}{\sin B}.$$

2. Given B, c, and b, find C. By Equation 1,

$$\sin C = \frac{c \sin B}{b}.$$

3. Given A, B, and c, find a. By Equation 11,

$$C = 180^{\circ} - (A + B);$$

and by Eq. 1,

$$a = \frac{c \sin A}{\sin C}.$$

4. Given B, a, and c, find A and b. By Eq. 2,

$$\tan\frac{A-C}{2} = \frac{a-c}{a+c}\tan\frac{A+C}{2};$$

from which we obtain the value of

$$\frac{A-C}{2}$$
;

and by Eq. 11,

$$\frac{A+C}{2} = 90^{\circ} - \frac{B}{2};$$

therefore we can find A from Eq. 3.

Then by Eq. 5,

$$b = (a+c)\frac{\cos\frac{A+C}{2}}{\cos\frac{A-C}{2}}.$$

5. Given a, b, and c, find B.

By Eq. 6,

$$\operatorname{vers} B = \frac{2(s-a)(s-c)}{ac};$$

or, we might equally well have used Eq. 7.

232. The following general equations are worth noting:

$$\sin A = \tan A \cos A = \sqrt{1 - \cos^2 A} = 2 \sin \frac{A}{2} \cos \frac{A}{2};$$

$$\cos A = \cot A \sin A = \sqrt{1 - \sin^2 A} = 2 \cos^2 \frac{A}{2} - 1;$$

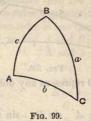
$$\tan A = \sin A \sec A = \frac{\operatorname{vers} 2A}{\sin 2A} = \operatorname{exsec} A \cot \frac{A}{2};$$

$$\cot A = \cos A \csc A = \frac{\sin 2A}{\text{vers } 2A} = \frac{\tan \frac{A}{2}}{\text{exsec } A};$$

vers
$$A = 1 - \cos A = 2 \sin^2 \frac{A}{2} = \cos A$$
 exsec A;

exsec
$$A = \sec A - 1 = \tan A \tan \frac{A}{2} = \frac{\text{vers } A}{\cos A}$$
.

233. Spherical Trigonometry.



RIGHT-ANGLED TRIANGLES.—In Fig. 99 let $A = 90^{\circ}$; then

 $\sin b = \sin a \sin B;$ $\tan c = \tan a \cos B;$

 $\cot C = \cos a \tan B$; $\tan c = \sin b \tan C$;

 $\cos a = \cos b \cos c$; $\cos B = \cos b \sin C$;

$$\tan a = \frac{\tan b}{\cos C};$$
 $\sin c = \frac{\tan b}{\tan B};$ $\sin a = \frac{\sin b}{\sin B};$

$$\sin C = \frac{\cos B}{\cos b};$$
 $\cos c = \frac{\cos a}{\cos b};$ $\sin B = \frac{\sin b}{\sin a};$

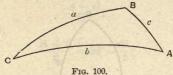
$$\cos C = \frac{\tan b}{\tan a};$$
 $\tan C = \frac{\tan c}{\sin b};$ $\tan B = \frac{\tan b}{\sin c};$

$$\cos c = \frac{\cos C}{\sin B};$$
 $\cos b = \frac{\cos B}{\sin C};$ $\cos a = \frac{\cot C}{\tan B}$

b and c are of the same species respectively as B and C. Any side is greater than 90° if the other sides are of different species, and less than 90° if of the same species.

B or C is less than 90° if the containing sides are of the same species, and less than 90° if of different species.

Oblique-angled triangles.



Let ABC in Fig. 100 represent any oblique-angled spherical triangle; then

$$\frac{\sin A}{\sin a} = \frac{\sin B}{\sin b} = \frac{\sin C}{\sin c}; \qquad (1)$$

$$\begin{cases}
\tan \frac{a+b}{2} = \tan \frac{c}{2} \frac{\cos \frac{A \sim B}{2}}{\cos \frac{A+B}{2}}; \quad . \quad (2a)
\end{cases}$$

$$\tan \frac{a \sim b}{2} = \tan \frac{c}{2} \frac{\sin \frac{A \sim B}{2}}{\sin \frac{A+B}{2}}; \quad (2b)$$

$$\int \tan \frac{A+B}{2} = \cot \frac{C}{2} \frac{\cos \frac{a \sim b}{2}}{\cos \frac{a+b}{2}}; \quad . \quad . \quad (3a)$$

$$\tan \frac{A \sim B}{2} = \cot \frac{C}{2} \cdot \frac{\sin \frac{a \sim b}{2}}{\sin \frac{a + \bar{b}}{2}}; \quad . \quad (3b)$$

$$\cos c = \cos a \cos b + \sin a \sin b \cos C; \qquad (4)$$

$$\sin\frac{A}{2} = \sqrt{\frac{\sin(s-b)\sin(s-c)}{\sin b\sin c}}; \quad . \quad . \quad (5)$$

$$\sin\frac{a}{2} = \sqrt{\frac{\cos S \cos (S - A)}{\sin B \sin C}}; \quad . \quad . \quad . \quad (6)$$

where
$$s = \frac{a+b+c}{2}$$
 and $S = \frac{A+B+C}{2}$.

The greater angle is always opposite the greater side.

No angle or side is greater than 180°.

The sum of any two sides is greater than the third side. The sum of the three sides is less than 360°.

Given a, b, and C, to find A and B; use Eqs. 2a and 2b.

" A, B, and c,	"	a and b ;	"	"	3a and 3b.
" a, b, and C,	"	c;	64	66	2a, 2b, and 3b
given a h and C	66	c.	66	6.	4

or, given a, b, and C, " c; " 4

" A, B, and a, " B or b; " " 1

" A, B, and a, " C; " 1 and 2a.
" A, B, and a, " c; " 1 and 3a.
" a, b, and A. " C: " 1 and 2a.

" a, b, and A, " C; " 1 and 2a.
" a, b, and A, " c; " 1 and 3a.

" A, B, and c, " C; " 3a, 3b, and 2b.

234. Measures of length and surface.

MEASURE OF LENGTH.

Miles.	Furlongs.	Chains.	Rods.	Yards.	Feet.	Inches
1	8	80	320	1760	5280	63360
0.125	1	10	40	220 -	660	7920
0.0125	0.1	1	4	22	66	792
0.003125	0.025	0.25	1	5.5	16.5	198
0.00056818	0.0045454	0.045454	0.181818	1	3	36
0.00018939	0.00151515	0.01515151	0.0606060	0.33333	1	12
0.000015783	0.000126262	0.001262626	0.00505050	0.0277777	0.083333	1

MEASURE OF SURFACE.

Sq. Miles.	Acres.	S. Chains.	Sq. Rods.	Sq. Yards.	Sq. Feet.
1 0.001562 0.0001562 0.00009764 0.000000323 0.0000000358	640 1 0.1 0.00625 0.0002066 0.00002296	6400 10 1 0.0625 0.002066 0.0002296	102400 160 16 1 1 0.0330 0.00367	3097600 4840 484 30.25 1 0.1111111	27878400 43560 4356 272.25 9

235. Measures of weight and capacity.

MEASURES OF WEIGHTS.

AVOIRDUPOIS.

Ton.	Cvt.	Pounds.	Ounces.	Drams.
1	20	2240	35840	573440 28672
0.05 0.00044642	0.0089285	112	1792	256
0.00002790	0.000558	0.0625	1	16
0.00000174	0.0000348	0.0016	0.0625	1

TROY.

Pounds.	Ounces.	Dwt,	Grains.	Pound Avoir
1	12	240	5760	0.822861
0.083333	1	20	480	0.068571
0.004166	0.05000	1	24	0.0034285
0.0001736	0.002083333	0.0416666	1	0.00014285
1.215275	14.58333	291.6666	7000	1

MEASURE OF CAPACITY,

Cub. Yard.	Bushel.	Cub. Feet.	Pecks.	Gallons.	Cub. inch.
1 0.03961 0.037037 0.009259	21.6962 1 0.803564 0.25 0.107421	27 1.24445 1 0.31114 0.133681 0.000547	100.987 4 3.21425 1 0.429684 0.001860	201.974 9.30918 7.4805 2.32729 1 0.004329	46656 2150.42 1728 537.605 231

MEASURE OF SURFACE.

APPENDIX.

NOTE A. (See Sec. 10.)

If we knew the average pressure in the cylinders we could find the propelling force of an engine at any speed, if not limited by adhesion, by the following rule:

Multiply together the square of the diameter of one piston in inches, the length of stroke in inches, and the mean pressure (above atmosphere) in lbs. per sq. in. The product divided by the diameter of a driver in inches gives the propelling force in lbs., ignoring "internal frictional resistances."

Theoretically, the mean effective cylinder-pressure in lbs. per sq. in. equals

$$\frac{P+2.3P\left(\text{Log }S\right)}{S}-15,$$

where P= absolute boiler-pressure in lbs. per sq. in. and S= Stroke \div part of stroke before cut-off.

But owing to the contraction of the steam-ports, the initial cylinder-pressure always falls below the boiler-pressure. Similarly owing to the contraction of the exhaust-port, back-pressure always exists; and these are matters so purely of mechanical detail that no general rule can be given which would take them into consideration.

At 20 miles per hour, however, the effective initial cylinder pressure often equals only about 90 p. c. of the boiler-pressure, and at 50 m. p. h. about 60 p. c.

Thus if P=125 lbs. per sq. in. and the stroke =24 inches; if steam is cut off at 6 inches, the theoretical mean cylinder-pressure =59 lbs. per square inch, which at 50 m. p. h. will probably be reduced to about 36 lbs.: so that if the diameter of the piston =16 inches, and of the driving-wheels 60 inches, the propelling force will equal 3680 lbs.; and if we deduct 10 p. c. from this for internal frictional resistances, the propelling force =3200 lbs.

NOTE B. (See Sec. 19.)

In order to reduce the quantities used in Diagram II into the *same* units, say ton, mile, and hour, the ordinates of the curves must be multiplied by

$$\frac{(3600)^2}{2000 \times 5280} \times 32.2 = 40$$
 (nearly)

to reduce them to tons weight (2000 lbs.), in miles per hour units. Then, with the units selected, the equation of motion is

$$\frac{d}{dt}(OQ) = NQ - MQ.$$

But if x is the space passed over,

$$OQ = \frac{dx}{dt};$$

so that

$$\frac{d}{dt}(OQ) = OQ\frac{d}{dx}(OQ),$$

and therefore

$$\frac{OQ \cdot d (OQ)}{NQ - MQ} = dx,$$

the graphic process giving the integral. But with the scales used in Diagram II, instead of multiplying the ordinates as above, we can simply use as a scale 1 square inch = 1 mile, which practically comes to the same thing. If the horizontal scale were ten miles per hour to one inch, the scale then to be used would be 4 square inches = 1 mile; and this is often a more convenient scale to adopt.

NOTE C. (See Sec. 44.)

Messrs. W. and L. E. Gurley in their Manual give the following methods of adjusting the object-slide:

To Adjust the Object-slide of a Transit.—"Having set up and levelled the instrument, the line of collimation being also adjusted for objects from three hundred to five

hundred feet distant, clamp the plates securely, and fix the vertical cross-wire upon an object as distant as may be distinctly seen; then, without disturbing the instrument, throw out the object-glass, so as to bring the vertical wire upon an object as near as the range of the telescope will allow. Having this clearly in mind, unclamp the limb, turn the instrument half-way around, reverse the eye-end of the telescope, clamp the limb, and with the tangent-screw bring the vertical wire again upon the near object; then draw in the object-glass slide until the distant object first sighted upon is brought into distinct vision. If the vertical wire strikes the same line as at first, the slide is correct for both near and remote objects; and, being itself straight, for all distances.

"But if there be an error, proceed as follows: First, with the thumb and forefinger twist off the thin brass tube that covers the screws. Next, with the screw-driver, turn the two screws on the opposite *sides* of the telescope, loosening one and tightening the other, so as apparently to increase the error, making, by estimation, one-half the correction required.

"Then go over the usual adjustment of the line of collimation, and having it completed, repeat the operation above described; first sighting upon the distant object, then finding a near one in line, and then reversing, making correction, etc., until the adjustment is complete."

To Adjust the Object-slide of a Y-Level.—"The maker selects an object as distant as may be distinctly observed, and upon it adjusts the line of collimation, making the centre of the wires to revolve without passing either above or below the point or line assumed.

"In this position, the slide will be drawn in nearly as far as the telescope-tube will allow.

"He then, with the pinion-head, moves out the slide until an object, distant about ten or fifteen feet, is brought clearly into view; again revolving the telescope in the Y's, he observes whether the wires will reverse upon this second object.

"Should this happen to be the case, he will assume that, as the line of collimation is in adjustment for these two distances, it will be so for all intermediate ones, since the bearings of the slide are supposed to be true, and their planes parallel with each other.

"If, however, as is most probable, either or both wires fail to

reverse upon the second point, he must then, by estimation, remove half the error by the screws at right angles to the hair sought to be corrected, remembering, at the same time, that on account of the inverting property of the eye-piece he must move the slide in the direction which apparently increases the error. When both wires have thus been treated in succession, the line of collimation is adjusted on the near object, and the telescope again brought upon the most distant point; here the tube is again revolved, the reversion of the wires upon the object once more tested, and the correction, if necessary, made in precisely the same manner.

"He proceeds thus, until the wires will reverse upon both objects in succession; the line of collimation will then be in adjustment at these and all intermediate points, and by bringing the screw-heads, in the course of the operation, to a firm bearing upon the washers beneath them, the adjustable ring will be fastened so as for many years to need no further adjustment."

"The centring of the eye-tube is performed after the wires have been adjusted, and is effected by moving the ring, by means of the screws shown on the outside of the tube, until the intersection of the wires is brought into the centre of the field of view."

NOTE D. (See Sec. 57.)

The time at which any elongation will occur may be found by the formula

$$\cos h = \cot (\text{dec.}) \times \tan (\text{lat.}),$$

where $\hbar =$ the hour-angle (see Sec. 182), \hbar really being the supplement of the angle at P in the right-angled spherical triangle WZP (or EZP) in Fig. 10, the right angle being at W or E.

The angle h may be reduced to mean time as shown in Part III.

NOTE E. (See Sec. 57.)

To find the azimuth of two stars when in the same vertical plane (Polaris being one of them) proceed as follows:

Let A = the difference in R.A. of the stars,

d = the declination of Polaris,

and D = the declination of the other star.

Find p and m from the formulæ

$$\tan m = \frac{\cos A}{\tan D}, \quad p = \frac{\sin D}{\cos m};$$

then find a from the formula

$$\cos a = p \sin (d + m)$$
.

Then Z, the azimuth, is given by

$$\sin Z = \frac{\sin A \cos D \cos d}{\cos L \sin a},$$

where L = the latitude of the place.

To find the interval of time which must elapse after the two stars are observed to be in the same vertical plane, before Polaris will be due north, find S from the equation

$$\sin S = \sin A \, rac{\cos \, D}{\sin \, a}.$$
 Then $L+d$

Then
$$\cot \frac{h}{2} = \frac{\cos \frac{L+d}{2}}{\sin \frac{L-d}{2}} \tan \frac{Z \sim S}{2},$$

where h is the hour-angle in sidereal time.

To find the interval in mean time, see Sec. 179.

The above steps may be easily traced by drawing the positions of the star, the pole, and the zenith.

It is not necessary to use Polaris; but if any other star is selected, d refers to the star whose declination is the greater.

The true value of the convergence is given by the equation

$$\sin \frac{\text{convergence}}{2} = \sin \frac{\text{diff. of long.}}{2} \times \sin (\text{lat.}).$$

If the places are in different latitudes, as A and D in Fig. 12, we have the convergence = the difference in azimuth at A and D, which we can find by solving the spherical triangle AND.

NOTE G. (See Sec. 189.)

The difference in altitude in seconds of arc, between the meridian altitude and the maximum altitude of a body, is equal to

 $\frac{d^2}{4\alpha}$

where

$$a = \frac{\cos \text{ lat. } \cos \text{ dec.} \times 1.964}{\sin (\text{lat.} - \text{dec.})},$$

and d = the hourly change of declination in minutes of arc.

When the declination differs in sign from the latitude, it will be negative. If the body has its declination changing towards the north in the northern hemisphere or towards the south in the southern hemisphere, the meridian altitude precedes the maximum altitude, which will be the case between mid-winter and mid-summer; but if changing towards the south in the northern hemisphere, or towards the north in the southern, the maximum altitude occurs to the east of the meridian.

TABLES.

1									
Deg.	Radius.	Deg.	Radius.	Deg.	Radius.	Deg.	Radius.	Deg.	Radius.
0° 0	Infinite 343775. 171887.	1° 0′ 1 2	5729.65 5635.72 5544.83	2° 0′	2864.93 2841.26	3° 0′	1910.08 1899.53	4° 0′	1432.69 1426.74
2 3	114592.	3	5456.82	2 3	2817.97 2795.06	2 3	1889.09 1878.77	2 3	1420.85 1415.01
4	85943.7	4	5371.56	4	2772.53	4	1868.56	4	1409,21
5 6 7	68754.9 57295.8	5	5288.92 5208.79	5 6	2750.35 2728.52	5 6	1858.47 1848.48	5	1403.46
7	49110.7	6	5131.05	7	2707.04	7	1838.59	6 7	1397.76 1392.10
8 9	42971.8 38197.2	8 9	5055.59 4982.33	8 9	2685.89	8	1828.82	8	1386.49
10	34377.5	10	4911.15	10	2665.08 2644.58	10	1819.14 1809.57	10	1380.92 1375.40
11 12	31252.3 28647.8	11 12	4841.98 4774.74	11 12	2624.39 2604.51	11 12	1800.10 1790.73	11 12	1369.92 1364.49
13	26444.2	13	4709.33	13	2584.93	13	1781.45	13	1359.10
14 15	24555.4 22918.3	14	4645.69 4583.75	14	2565.65 2546.64	14	1772.27 1763.18	14	1353.75
16	21485.9	16	4523.44	16	2527.92	16	1754.19	15 16	1348.45 1343.15
17 18	20222.1 19098.6	17 18	4464.70 4407.46	17	2509.47 2491.29	17	1745.26	17	1337.65
19	18093.4	19	4351.67	19	2473,37	19	1736.48 1727.75	18 19	1332.77 1327.63
20	17188.8	20	4297.28	20	2455.70	20	1719.12	20	1322.53
21 22	16370.2 15626.1	21 22	4244.23 4192.47	21 22	2438.29 2421.12	21 22	1710.56 1702.10	21 22	1317.46 1312.43
23 24	14946.7 14323.6	23	4141.96	23 24	2404.19	23	1693.72	23	1307.45
25	13751.0	24 25	4044.51	25	2387.50 2371.04	24 25	1685.42 1677.20	24 25	1302.50 1297.58
26 27	13222.1	26	3997.49	26	2354.80	26	1669.06	26	1292.71
28	12732.4 12277.7	27 28	3951.54 3906.54	27 28	2338.78 2322.98	27 28	1661.00 1653.01	27 28	1287.87 1283.07
29	11854.3	29	3862.74	29	2307.39	29	1645.11	29	1278.30
30	11459.2	30	3819.83	30	2292.01	30	1637.28	30	1273.57
31 32	11089 6 10743 0	31 32	3777.85 3736.79	31 32	2276.84 2261.86	31 32	1629.52 1621.84	31 32	1268.87 1264.21
33	10417.5	33	3696.61	33	2247.08	33	1614.22	33	1259.58
34 35	10111.1 9822.18	34 35	3657.29 3618.80	34 35	2232.49 2218.09	34 35	1606.68 1599.21	34	1254.98
36	9549.34	36	3581.10	36	2203.87	36	1591,81	35 36	1250.42 1245.89
37 38	9291.29	37	3544.19	37	2189.84	37	1584.48	37	1241.40
39	9046.75 8814.78	38 39	3508.02 3472.59	38	2175.98 2162.30	38	1577.21 1570.01	38	1236.94 1232.51
40	8594.42	40	3437.87	40	2148.79	40	1562.88	40	1228.11
41 42	8384.80 8185.16	41 42	3403.83 3370.46	41 42	2135.44 2122.26	41 42	1555.81 1548.80	41 42	1223.74 1219.40
43	7994.81	43	3337.74	43	2109.24	43	1541.86	43	1215.30
44 45	7813.11 7639.49	. 45	3305.65 3274.17	44 45	2096,39 2083.68	44 45	1534.98 1528.16	44 45	1210.82 1206.57
46	7473.42	46	3243.29	46	2071.13	46	1521.40	46	1200.57
47 48	7314.41	47 48	3212.98 3183.23	47	2058.73 2046.48	47 48	1514.70 1508.06	47	1198.17
49	7162.03 7015.87	48	3154.03	48	2034.37	48	1501.48	48	1194.01 1189.88
50	6875.55	50	3125.36	50	2022.41	50	1494.95	50	1185.78
51 52	6740.74 6611.12	51 52	3097.20 3069.55	51 52	2010.59 1998.90	51 52	1488.48 1482.07	51 52	1181.71 1177.66
53	6486.38	53	3042.39	53	1987.35	53	1475.71	53.	1173.65
54 55	6366.26	54 55	3015,71 2989.48	54 55	1975.93 1964.64	54 55	1469.41 1463.16	54	1169.66 1165.70
56	6138.90	56	2963.71	56	1953.48	56	1456.96	56	1161.76
57 58	6031.20 5927.22	57 58	2938.39 2913.49	57 58	1942.44 1931.53	57 58	1450.81 1444.72	57 58	1157.85 1153.97
59	5826.76	59	2889.01	59	1920.75	59	1438.68	59	1150.11
60	1 5729.65	60	2864_93	60	1910.08	60	1432.69	60	1146.28

Deg.	Radius.	Deg.	Radius.	Deg.	Radius.	Deg.	Radius.	Deg.	Radius.
5° 0	1146.28	6° 0	955.366	70 0'	819.020	8° 0′	716,779	9° 0′	637.275
1	1142.47	1		1	817.077	1	715.291	1	636.099
1 2	1138.69	2		2	815.144	2	713.810	2	634.928
3	1134.94	3		3 4	813.238 811.303	3 4	712.335	3 4	633.761
5	1131.21 1127.50	5		5	809.397	5	709 402	5	632.599 631.440
6	1123.82	0		6	807.499	6	709.402 707.945	6	630.286
7	1120.16	7	937.161	7	805.611	7	706.493	7	629.136
8				8	803.731	8	705.048	8	627.991
10				9	801.860	9 10	703.609 702.175	9 10	626.849
11				11	798.144	11	700.748	11	624.579
12 13	1102.23	13		12	796.299	12 13	699.326 697.910	12 13	623.450
14				14	792.634	14	696.499	14	621 203
15		1		15	790.814	15	695.095	15	620 087
16	1088.28	1	914.750	16	789,003	16	693.696	16	618.974
17					787.210	17	692,302	17	617.865
18					785.405 783.618		600.914	18	616.760
20				20	781.840		688.156		614.563
21	1071.3		902.758		780.069		686.785		613.470
2:	2 1068.0 3 1064.7								612.380 611.295
2	1061.4				774.806		682.704	24	610 214
2	1058.1	3 2	5 893.388	25	773.067	25	681.354	25	610.214 609.136
20	$5 \mid 1054.9$	2 2		26		26	680.010	26	608.062
2			7 888.770	27	769.613		678.671	27	606.992
2						28			
3									
3									
3	$\begin{bmatrix} 2 & 1035.8 \\ 3 & 1032.7 \end{bmatrix}$	7 3 6 3	2 877.451 3 875.221	33		38		32	601.698
3	4 1029.6					34	669.446	34	
3	5 1026.6	0 3	5 870.79	35	756.101	3		35	598.567
3			6 868.598				666.856	36	
3			7 866.413 8 864.238	37				37 38	
3		0 3	9 862.07	39		3		30	
4	0 1011.5	1 4	0 859.92						
4	1 1008.5		857.78 2 855.64						
	3 1002.6		853.52					4	
4	4 999.76	2 4	4 851.41	7 4	1 741.456	3 4	4 656.69	1 4	589.364
	5 996.86		5 849.31	7 4		4	5 655.44	6 4	5 588.359
	993.98	8	6 847.22		738.279	9 4		2 4	587.357
	991.13 8 988.28	20	17 845.14 18 843.08			9 4		9 4	586.359 585.364
	19 985.4	51	19 841.02		9 733.56	4 4		9 4	
	982.63		50 838.97		732.00	5	0 649.27	4 5	
	51 979.8 52 977.0		51 836.93 52 834.90						
808.	53 974.2	94	53 832.88	5	3 727.37	0 5			
	54 971.5		54 830.87				4 644.42	0 5	4 579.46
	968.8		55 828.87		5 724.31		5 643.21		
	56 966.0 57 963.3		56 826.88 57 824.90		6 722.79 7 721.28		6 642.02	1 5	6 577.526 7 576.56
	58 960.6		58 822.93		8 719.77	4	8 639.63		8 575.59
1147.	59 958.0	25	59 820.97	3 5	9 718.27	3 1	9 638.45	5 5	9 574.64
1000	60 955.3	66	60 819.0	20 6	60 716.77	9 6	60 637.27	5 6	0 573.68

Deg.	Radius.	Deg.	Radius.	Deg.	Radius.	Deg.	Radius.	Deg.	Radius.
10° 0′ 2 4 6 8 10 12 14 16 18	573.686 571.784 569.896 568.020 566.156 564.305 562.466 560.638 558.823 557.019	12° 0′ 2 4 6 8 10 12 14 16 18	478.339 477.018 475.705 474.400 473.102 471.810 470.526 469.249 467.978 466.715	14° 0′ 2 4 6 8 10 12 14 16 18	410 .275 409 .306 408 .341 407 .380 406 .424 405 .473 404 .526 403 .583 402 .645 401 .712	16° 0′ 2 4 6 8 10 12 14 16 18	359.265 358.523 357.784 357.048 356.315 355.585 354.859 354.135 353.414 352.696	18° 0′ 2 4 6 8 10 12 14 16 18	319.623 319.037 318.453 317.871 317.292 316.715 316.139 315.566 314.998 314.426
20	555,227	20	465.459	20	400.782	20	351.981	20	313.860
22	553,447	22	464.209	22	399.857	22	351.269	22	313.295
24	551,678	24	462.966	24	398.937	24	350.560	24	312.732
26	549,920	26	461.729	26	398.020	26	349.854	26	312.172
28	548,174	28	460.500	28	397.108	28	349.150	28	311.613
30	546,438	30	459.276	30	396.200	30	348.450	30	311.056
32	544,714	32	458.060	32	395.296	32	347.752	32	310.502
34	543,001	34	456.850	34	394.396	34	347.057	34	309.949
36	541,298	36	455.646	36	393.501	36	346.365	36	309.399
38	539,606	38	454.449	38	392.609	38	345.676	38	308.850
40	587.924	40	453.259	40	391.722	40	344.990	40	308.308
42	586.253	42	452.073	42	390.838	42	344.306	42	307.759
44	534.593	44	450.894	44	389.959	44	343.625	44	307.216
46	532.943	46	449.722	46	389.084	46	342.947	46	306.675
48	531.303	48	448.556	48	388.212	48	342.271	48	306.136
50	529.673	50	447.395	50	387.345	50	341.598	50	305.599
52	528.053	52	446.241	52	386.481	52	340.928	52	305.064
54	526.443	54	445.093	54	385.621	54	340.260	54	304.531
56	524.843	56	443.951	56	384.765	56	339.595	56	304.000
58	523.252	58	442.814	58	383.913	58	338.933	58	303.470
11° 0′ 2 4 6 8 10 12 14 16 18	521.671	13° 0′	441.684	15° 0′	383.065	17° 0′	338.273	19° 0′	302.943
	520.100	2	440.559	2	382.220	2	337.616	2	302.417
	518.539	4	439 440	4	381.380	4	336.962	4	301.893
	516.986	6	438.326	6	380.543	6	336.310	6	301.371
	515.443	8	437.219	8	379.709	8	335.660	8	300.851
	513.909	10	436.117	10	378.880	10	335.013	10	300.333
	512.385	12	435.020	12	378.054	12	334.369	12	299.816
	510.869	14	433.929	14	377.231	14	333.727	14	299.302
	509.363	16	432.844	16	376.412	16	333.088	16	298.789
	507.865	18	431.764	18	375.597	18	332.451	18	298.278
20	506.376	20	430 .690	20	374.786	20	331,816	20	297.768
22	504.896	22	429 .620	22	373.977	22	331,184	22	297.260
24	503.425	24	428 .557	24	373.173	24	330,555	24	296.755
26	501.962	26	427 .498	26	372.372	26	329,928	26	296.250
28	500.507	28	426 .445	28	371.574	28	329,303	28	295.748
30	499.061	20	425 .396	30	370.780	30	328,689	30	295.247
32	497.624	32	424 .354	32	369.989	32	328,061	32	294.748
34	496.195	34	423 .316	34	369.202	34	327,443	34	294.251
36	494.774	36	422 .283	36	368.418	36	326,828	36	298.756
38	493.361	38	421 .256	38	367.637	38	326,215	38	293.262
40	491.956	40	420.233	40	366.859	40	325.604	40	292.770
42	490.559	42	419.215	42	366.085	42	324.996	42	292.279
44	489.171	44	418.203	44	365.315	44	324.390	44	291.790
46	487.790	46	417.195	46	364.547	46	323.786	46	291.303
48	486.417	48	416.192	48	363.783	48	823.184	48	290.818
50	485.051	50	415.194	50	363.022	50	322.585	50	290.334
52	483.694	52	414.201	52	362.264	52	321.989	52	289.851
54	482.344	54	413.212	54	361.510	54	321.394	54	289.371
56	481.001	56	412.229	56	360.758	56	320.801	56	288.892
58	479.666	58	411.250	58	360.010	58	320.211	58	288.414
60	478.339	60	410.275	60	359.265	60	319.623	60	287.939

		1						-
Angle.	Tangent.	External.	Angle.	Tangent.	External.	Angle.	Tangent.	External.
1° 10′ 20 30 40 50 2 10 20 30 40 50	50.00 58.34 66.67 75.01 83.34 91.68 100.01 108.35 116.68 125.02 133.36 141.70	.218 .297 .388 .491 .606 .733 .873 1.024 1.188 1.364 1.552 1.752	11 10' 20 30 40 50 12 10 20 30 40 50	551.70 560.11 568.53 576.95 585.36 598.79 602.21 610.64 619.07 627.50 635.93 644.37	26.500 27.313 28.137 28.974 29.824 30.686 31.561 32.447 33.347 34.259 35.183 36.120	21° 10′ 20 30 40 50 22 10 20 30 40 50 50	1061.9 1070.6 1079.2 1087.8 1096.4 1105.1 1113.7 1122.4 1131.0 1139.7 1148.4 1157.0	97.577 99.155 100.75 102.35 103.97 105.60 107.24 108.90 110.57 112.25 113.95 115.66
3 10 20 30 40 50 40 50	150.04 158.38 166.72 175.06 183.40 191.74 200.08 208.43 216.77 225.12 233.47 241.81	1.964 2.188 2.425 2.674 2.934 3.207 3.492 3.790 4.099 4.421 4.755 5.100	13 10 20 30 40 50 14 10 20 30 40 50	652.81 661.25 669.70 678.15 686.6) 695.06 703.51 711.97 720.44 728.90 737.37 745.85	37.070 38.031 39.006 39.993 40.992 42.004 43.029 44.066 45.116 46.178 47.253 48.341	23 10 20 30 40 50 24 10 20 30 40 50 24 10 20 30 40 50 50 20 30 40 50 50 50 50 50 50 60 60 60 60 60 60 60 60 60 6	1165.7 1174.4 1183.1 1191.8 1200.5 1209.2 1217.9 1226.6 1235.3 1244.0 1252.8 1261.5	117.38 119.12 120.87 122.63 124.41 126.20 128.00 129.82 131.65 133.50 135.35 137.23
5 10 20 30 40 50 6 10 20 30 30 40 40 50 50	250.16 258.51 266.86 275.21 283.57 291.92 300.28 308.64 316.99 325.35 333.71 342.08	5.459 5.829 6.211 6.606 7.013 7.432 7.863 8.307 8.762 9.230 9.710 10.202	15 10 20 30 40 50 16 10 20 30 40 50	754.32 762.80 771.99 779.77 788.26 796.75 805.25 813.75 822.25 830.76 839.27 847.78	49.441 50.554 51.679 52.818 53.969 55.132 56.309 57.498 58.699 59.914 61.141 62.381	25 10 20 30 40 50 26 10 20 30 40 40 40 40 40 40 40 40 40 4	1270.2 1279.0 1287.7 1296.5 1305.3 1314.0 1322.8 1331.6 1340.4 1349.2 1358.0 1366.8	139.11 141.01 142.93 144.85 146.79 148.75 150.71 152.69 154.69 156.70 158.72 160.73
7 10 20 30 40 50 8 10 20 30 40 40 50	350.44 358.81 367.17 375.54 383.91 392.28 400.66 409.03 417.41 425.79 434.17 442.55	10.707 11.224 11.758 13.294 12.847 13.413 13.991 14.582 15.184 15.799 16.426 17.065	17 10 20 30 40 50 18 10 20 30 40 50	856.30 864.82 873.35 881.88 890.41 898.95 907.49 916.03 924.58 933.13 941.69 950.25	63.634 64.900 66.178 67.470 68.774 70.091 71.421 72.764 74.119 75.488 76.869 78.264	27 10 20 30 40 50 28 10 20 30 40 40 40 50	1375.6 1384.4 1393.2 1402.0 1410.9 1419.7 1428.6 1437.4 1446.3 1455.1 1464.0 1472.9	162.81 164.86 166.95 169.04 171.15 173.27 175.41 177.55 179.72 181.89 184.08 186.29
10 20 30 40 50 10 10 20 30 40 50	450.93 459.32 467.71 476.10 484.49 492.88 501.28 509.68 518.08 526.48 534.89 543.29	17.717 18.381 19.058 19.746 20.447 21.161 21.887 22.624 23.375 24.138 24.913 25.700	19 10 20 30 40 50 20 20 30 40 40 40 50 20 30 40 50 20 50 20 50 20 50 50 50 50 50 50 50 50 50 5	958.81 967.38 975.96 984.53 993.12 1001.7 1010.3 1018.9 1027.5 1036.1 1044.7 1053.3	79.671 81.092 82.525 83.972 85.431 86.904 88.389 89.888 91.399 92.924 94.462 96.013	29 10 20 30 40 50 30 10 20 30 40 40 50 50	1481.8 1490.7 1499.6 1508.5 1517.4 1526.3 1535.3 1544.2 1553.1 1562.1 1571.0 1580.0	188.51 190.74 192.99 195.25 197.53 199.82 202.12 204.44 206.77 209.12 211.48 213.86

Angle. I.	Tangent.	External.	Angle.	Tangent.	External.	Angle.	Tangent.	External.
31° 10 20 30 40 50 30 40 40 50	1589.0 1598.0 1606.9 1615.9 1624.9 1633.9 1643.0 1652.0 1661.0 1670.0 1679.1 1688.1	216.25 218.66 221.08 223.51 225.96 228.42 230.90 233.39 235.90 238.43 240.96 243.52	41° 10′ 20 30 40 50 42 10 20 30 40 50 50	2142.2 2151.7 2161.2 2170.8 2180.3 2189.9 2199.4 2209.0 2218.6 2228.1 2237.7 2247.3	387.38 390.71 394.06 397.43 400.82 404.22 407.64 411.07 414.52 417.99 421.48 424.98	51° 10′ 20 30 40 50 52 10 20 30 40 50 50 50	2732.9 2743.1 2753.4 2763.7 2773.9 2784.2 2794.5 2804.9 2815.2 2825.6 2835.9 2846.3	618.3 622.8 627.2 631.6 636.1 640.6 645.1 649.7 654.2 658.4 668.0
33 10 20 30 40 50 34 10 20 30 40 50	1697.2 1706.3 1715.3 1724.4 1733.5 1742.6 1751.7 1760.8 1770.0 1779.1 1788.2 1797.4	246.08 248.66 251.26 253.87 256.50 259.14 261.80 264.47 267.16 269.86 272.58 275.31	43 10 20 30 40 50 44 10 20 30 40 40 50 40 50 40 50 40 50 50 40 50 60 60 60 60 60 60 60 60 60 6	2257.0 2266.6 2276.2 2285.9 2295.6 2305.2 2314.9 2324.6 2334.3 2344.1 2353.8 2363.5	428.50 432.04 435.59 439.16 422.75 446.35 449.98 453.62 457.27 460.95 464.64 468.35	53 10 20 30 40 50 54 10 20 20 30 40 50 50	2856.7 2867.1 2877.5 2888.0 2898.4 2908.9 2919.4 2929.9 2940.4 2951.0 2961.5 2972.1	672.6 677.3 681.9 686.6 691.4 693.1 700.8 705.6 710.4 715.2 720.1 724.9
35 10 20 30 40 50 36 10 20 30 40 50 30 40 50	1806.6 1815.7 1824.9 1834.1 1843.3 1852.5 1861.7 1870.9 1880.1 1889.4 1898.6 1907.9	278.05 280.82 283.60 286.39 289.20 292.02 294.86 297.72 300.59 303.47 306.37 309.29	45 10 20 30 40 50 46 10 20 30 40 40 50 40 50 40 50 40 50 50 40 50 60 60 60 60 60 60 60 60 60 6	2373.3 2383.1 2392.8 2402.6 2412.4 2422.3 2432.1 2441.9 2451.8 2461.7 2471.5 2481.4	472.08 475.82 479.59 483.37 487.17 490.98 494.82 498.67 502.54 506.42 510.33 514.25	55 10 20 30 40 50 56 10 20 30 40 50	2982.7 2993.3 3003.9 3014.5 3025.2 3035.8 3046.5 3057.2 3067.9 3078.7 3089.4 3100.2	729.8 734.7 739.6 744.6 749.5 754.5 759.5 764.6 769.6 774.7 779.8 784.9
37 10 20 30 40 50 38 10 20 30 40 50	1917.1 1926.4 1935.7 1945.0 1954.3 1963.6 1972.9 1982.2 1991.5 2000.9 2010.2 2019.6	312.22 315.17 318.13 321.11 324.11 327.12 330.15 333.19 336.25 339.32 342.41 345.52	47 10 20 30 40 50 48 10 20 30 40 50	2491.3 2501.2 2511.2 2521.1 2531.1 2531.1 2541.0 2551.0 2561.0 2571.0 2591.1 2601.1	518.20 522.16 526.13 530.13 534.15 534.15 538.18 542.23 546.30 550.39 554.50 558.63 562.77	57 10 20 30 40 50 58 10 20 30 40 50	3110.9 3121.7 3132.6 3143.4 3154.2 3165.1 3176.0 3186.9 3197.8 3208.8 3219.7 3230.7	790.09 795.2 800.4 805.6 810.8 816.10 821.3 826.6 831.9 837.3 842.6 848.0
10 20 30 40 50 40 10 20 30 40	2029.0 2038.4 2047.8 2057.2 2066.6 2076.0 2085.4 2094.9 2104.3 2113.8 2123.3	348.64 351.78 354.94 358.11 361.29 367.72 367.72 370.95 374.20 877.47 380.76	49 10 20 30 40 50 50 50 10 20 30 40	2611.2 2621.2 2631.3 2641.4 2651.5 2661.6 2671.8 2681.9 2692.1 2702.3 2712.5	566.94 571.12 575.32 579.54 583.78 588.04 592.32 596.62 600.93 605.27 609.62	59 10 20 30 40 50 60 10 20 30 40	3241.7 3252.7 3263.7 3274.8 3285.8 3296.9 3308.0 3319.1 3330.3 3341.4 3352.6	853.46 858.89 864.36 875.33 880.86 886.38 891.95 897.54 903.15

The state of the s				15-1-17			B 14-1	
Angle.	Tangent.	External.	Angle.	Tan- gent.	External.		gent.	External.
I.	T.	E.	1.	T.	E.	I.	T.	E.
61° 10′ 20 30 40 50 62 10	3375.0 3386.3 3397.5 3408.8 3420.1 3431.4 3442.7 3454.1	920.14 925.85 931.58 937.34 943.12 948.92 954.75 960.60	71° 10′ 20 30 40 50 72	4112.1 4124.8 4137.4 4150.1 4162.8 4175.6	1308.2 1515.6 1322.9 1330.3 1337.7 1345.1 1352.6 1360.1	81° 10′ 20 30 40 50 82	4951.5 4966.1 4980.7 4995.4	1805.3 1814.7 1824.1 1833.6 1843.1 1852.6 1862.2 1871.8
20 30 40 50	3476.8 3488.3	972.38 978.31 984.27	20 30 40 50	4188.5 4201.2 4214.0 4226.8	1367.6 1375.2 1382.8 1390.4	20 30 40 50	5010.0 5024.8 5039.5 5054.3	1881.5 1891.2 1900.9 1910.7
63 10 20 30 40 50 64 10 20 30 40 50	3511.1 3522.6 3534.1 3545.6 3557.2 3568.7 3580.3 3591.9 3603.5 3615.1 3626.8 3638.5	990.24 996.24 1002.3 1008.3 1014.4 1020.5 1026.6 1032.8 1039.0 1045.2 1051.4 1057.7	73 10 20 30 40 50 74 10 20 30 40 50 50	4239.7 4252.6 4265.6 4278.5 4291.5 4304.6 4317.6 4330.7 4343.8 4356.9 4370.1 4383.3	1398.0 1405.7 1413.5 1421.2 1429.0 1436.8 1444.6 1452.5 1460.4 1468.4 1476.4 1484.4	83 10 20 30 40 50 84 10 20 30 40 40 50 84 10 20 30 40 50 80 40 50 80 40 50 50 80 40 50 60 60 60 60 60 60 60 60 60 6	5069.2 5084.0 5099.0 5113.9 5128.9 5143.9 5159.0 5174.1 5189.3 5204.4 5219.7 5234.9	1920.5 1930.4 1940.3 1950.3 1960.2 1970.3 1980.4 1990.5 2000.6 2010.8 2021.1 2031.4
65 10 20 30 40 50	3650.2 3661.9 3673.7 3685.4 3697.2 3709.0	1063.9 1070.2 1076.6 1082.9 1089.3 1095.7	75 10 20 30 40 50	4396.5 4409.8 4423.1 4436.4 4449.7 4463.1	1492.4 1500.5 1508.6 1516.7 1524.9 1533.1	85 10 20 30 40 50	5250.3 5265.6 5281.0 5296.4 5311.9 5327.4	2041.7 2052.1 2062.5 2073.0 2083.5 2094.1
10 20 30 40 50	3720.9 3732.7 3744.6 3756.5 3768.5 3780.4	1102.2 1108.6 1115.1 1121.7 1128.2 1134.8	76 10 20 30 40 50	4476.5 4489.9 4503.4 4516.9 4530.4 4544.0	1541.4 1549.7 1558.0 1566.3 1574.7 1583.1	86 10 20 30 40 50	5343.0 5358.6 5374.2 5389.9 5405.6 5421.4	2104.7 2115.3 2126.0 2136.7 2147.5 2158.4
10 20 30 40	3792.4 3804.4 3816.4 3828.4 3840.5	1141.4 1148.0 1154.7 1161.3 1168.1	40	4557.6 4571.2 4584.8 4598.5 4612.2	1591.6 1600.1 1608.6 1617.1 1625.7	10 20 30 40	5437.2 5453.1 5469.0 5484.9 5500.9	2169.2 2180.2 2191.1 2202.2 2213.2
68 10 20 30 40 50	3852.6 3864.7 3875.8 3889.0 3901.2 3913.4 3925.6	1174.8 1181.6 1188.4 1195.2 1202.0 1208.9 1215.8	78 10 20 30 40 50	4626.0 4639.8 4653.6 4667.4 4681.3 4695.2 4709.2	1634.4 1643.0 1651.7 1660.5 1669.2 1678.1 1686.9	88 10 20 30 40 50	5517.0 5533.1 5549.2 5565.4 5581.6 5597.8 5614.2	2224.3 2235.5 2246.7 2258.0 2269.3 2280.6 2292.0
69 10 20 30 40	3937.9 3950.2 3962.5 3974.8 3987.2	1222.7 1229.7 1236.7 1243.7	79 10 20 30 40	4723.2 4737.2 4751.2 4765.3 4779.4	1695.8 1704.7 1713.7 1722.7 1731.7	89 10 20 30 40	5630.5 5646.9 5663.4 5679.9 5696.4	2303.5 2315.0 2326.6 2338.2 2349.8
70 50 10 20 30 40 50	3999.5 4011.9 4024.4 4036.8 4049.3 4061.8 4074.4	1257.9 1265.0 1272.1 1279.3 1286.5 1293.6 1300.9	80 10 20 30 40 50	4793.6 4807.7 4822.0 4836.2 4850.5 4864.8 4879.2	1740.8 1749.9 1759.0 1768.2 1777.4 1786.7 1796.0	90 50 10 20 30 40 50	5713.0 5729.7 5746.3 5763.1 5779.9 5796.7 5813.6	2361.5 2373.3 2385.1 2397.0 2408.9 2420.9 2432.9

TABLE II.—TANGENTS AND EXTERNALS TO A 1° CURVE.

Angle.	Tan-	Ex-	Angle.	Tan-	Ex-	Angle.	Tan-	Ex-
820.	gent.	ternal.	B10.	gent.	ternal.	zaigio.	gent.	ternal
I.	T.	E.	I.	T.	E.	I.	T.	E.
91°	5830.5	2414.9	97	6476.2	2917.3	103	7203.2	3474.4
10'	5847.5	2457.1	10	6495.2	2931.6	10	7224.7	3491.3
20	5864.6	2469.3	20	6514.3	2945.9	20	7246.3	3508.2
30	5881.7	2481.5	30	6533.4	2960.3	30	7268.0	3525.2
40	5898.8	2493.8	40	6552.6	2974.7	40	7289.8	3542.4
50	5916.0	2506.1	50	6571.9	2989.2	50	7311.7	3559.6
92	5983.2	2518.5	98	6591.2	3003.8	104	7333.6	3576.8
10	5950.5	2531.0	10	6610.6	3018.4	10	7355.6	3594.2
20	5967.9	2543.5	20	6630.1	3033.1	20	7377.8	3611.7
30	5985.3	2556.0	30	6649.6	3047.9	30	7399.9	3629.2
40	6002.7	2568.6	40	6669.2	3062.8	40	7422.2	3646.8
50	6020.2	2581.3	50	6688.8	3077.7	50	7444.6	3664.5
93	6037.8	2594.0	99	6708.6	3092.7	105	7467.0	3682.3
10	6055.4	2606.8	10	6728.4	3107.7	10	7489.6	3700.2
20	6073.1	2619.7	20	6748.2	3122.9	20	7512.2	3718.2
30	6090.8	2632.6	30	6768.1	3138.1	30	7534.9	3736.2
40	6108.6	2645.5	40	6788.1	3153.3	40	7557.7	3754.4
50	6126.4	2658.5	50	6808.2	3168.7	50	7580.5	3772.6
94	6144.3	2671.6	100	6828.3	3184.1	106	7603.5	3791.0
10	6162.2	2684.7	10	6848.5	3199.6	10	7626.6	3809.4
20	6180.2	2697.9	20	6868.8	3215.1	20	7649.7	3827.9
30	6198.3	2711.2	30	6889.2	3230.8	30	7672.9	3846.5
40	6216.4	2724.5	40	6909.6	3246.5	40	7696.3	3865.2
50	6234.6	2737.9	50	6930.1	3262.3	50	7719.7	3884.0
95	6252.8	2751.3	101°	6950.6	3278.1	107	7743.2	3902.9
10	6271.1	2764.8	10'	6971.3	3294.1	10	7766.8	3921.9
20	6289.4	2778.3	20	6992.0	3310.1	20	7790.5	3940.9
30	6307.9	2792.0	30	7012.7	3326.1	30	7814.3	3960.1
40	6326.3	2805.6	40	7033.6	3342.3	40	7838.1	3979.4
50	6344.8	2819.4	50	7054.5	3358.5	50	7862.1	3998.7
96	6363.4	2833.2	102	7075.5	3374.9	108	7886.2	4018.2
10	6382.1	2847.0	10	7096.6	3391.2	10	7910.4	4037.8
20	6400.8	2861.0	20	7117.8	3407.7	20	7934.6	4057.4
30	6419.5	2875.0	30	7139.0	3424.3	30	7959.0	4077.2
40	6438.4	2889.0	40	7160.3	3440.9	40	7983.5	4097.1
50	6457.3	2903.1	50	7181.7	3457.6	50	8008.0	4117.0

CORRECTIONS FOR TANGENTS AND EXTERNALS.

		For Tangents, Add						FOR EXTERNALS, ADD					
Ang I.	5° Cur.	10° Cur.	15° Cur.	20° Cur.	25° Cur.	30° Cur.	Ang I.	5° Cur.	10° Cur.	15° Cur.	20° Cur.	25° Cur.	30° Cur.
10°	.03	.06	.09	.13	.16	.19	100	001	.003	.004	.006	.007	.008
20	.06	.13	.19	.26	.32	.39	20	.006	.011	.017	.022	.028	.034
30	.10	.19	.29	.39	.49	.59	30	.013	.025	.038	.051	.065	.078
40	.13	.26	.40	.53	.67	80	40	.023	.046	.070	.093	.117	.141
50	.17	.34	.51	.68	.85	1 02	50	.037	.075	.116	.151	.189	.227
60	.21	.42	.63	.84	1.05	1.27	60	.056	.112	.168	.225	.283	.340
70	.25	.51	.76	1.02	1.28	1.54	70	.080	.159	.240	.321	.403	.485
80	.30	.61	.91	1.22	1.53	1.84	80	.110	.220	.332	.445	.558	.671
90	.36	.72	1.09	1.45	1.83	2.20	90	.149	.299	.450	.603	.756	.910
100	.43	.86	1.30	1.74	2 18	2.62	100	.200	.401	.604	.809	1.015	1.221
110	.51	1.03	1.56	2 08	2.61	3.14	110	,268	.536	.806	1.082	1.355	1.63
120	.62	1.25	1.93	2.52	3 16	3.81	120	,360	.721	1.086	1.456	1.825	2.19

TABLE III.-TANGENTIAL OFFSETS 100 FT. ALONG THE CURVE.

Deg. of Curve.	0'	10′	20′	30′	40′	50′
112	0.000	0.145	0.004	0.400	0 500	0 70
00	0.000	0.145	0.291	0.436	0.582	0.72
10	0.873	1.018	1.164	1.309	1.454	1.600
20	1.745	1.891	2.036	2.181	2.327	2.479
3°	2.618	2.763	2.908	3.054	3.199	3.34
40	3.490	3.635	3.781	3.926	4.071	4.21
50	4.362	4.507	4.653	4.798	4.943	5.088
60	5.234	5.379	5.524	5.669	5.814	5.96
70	6.105	6.250	6.395	6.540	6.685	6.83
80	6.976	7.121	7.266	7.411	7.556	7.70
90	7.846	7.991	8.136	8.281	8.426	8.57
100	8.716	8.860	9.005	9.150	9.295	9.44
11°	9.585	9.729	9.874	10.019	10.164	10.30
120	10.453	10.597	10.742	10.887	11.031	11.170
13°	11.320	11.465	11.609	11.754	11.898	12.04
14°	12.187	12.331	12.476	12.620	12.764	12.90
15°	13.053	13.197	13.341	13.485	13.629	13.77
16°	13.917	14.061	14.205	14.349	14.493	14.63
170	14.781	14.925	15.069	15.212	15.356	15.500
18°	15.643	15.787	15.931	16.074	16.218	16.36
19°	16.505	16.648	16.792	16.935	17.078	17.22
20°	17.365	17.508	17.651	17.794	17.937	18.08
21°	18.224	18.367	18.509	18.652	18.795	18.93
22°	19.081	19.224	19.366	19.509	19.652	19.79
23°	19.937	20.079	20.222	20.364	20.507	20.64
24°	20.791	20.933	21.076	21.218	21.360	21.50

TABLE IV .- MID-ORDINATES TO A 100-FT. CHORD.

Deg. of Curve.	0	1	2	3	4	5	6	7	8	9
0° 10° 20°	2.183	2.402	2.620	2.839	3.058	3.277	3,496	3.716	3.935	1.965 4.155 6.360

200 B.St.

Degree	Actual Arc,		Lo	NG CHORDS.		20 m
of	One			1	1	1
Curve.	Station.	Stations.	Stations 3	4	5	6
- 1K 5V 7	I Little	Stations.	Stations.	Stations.	Stations.	Stations.
1000 100						
00 101	100 000		BELL TO	TYUE TUS	to the state of	000.2
0° 10′ 20	100.000	200.000	299.999	399.998	499.996	599.993
30	.000	199.999	299.997	399.992	499.983	599.970
40	.001	199,998 199,997	299.992	399.981	499.962	599.933
50	.001	199.995	299.986	399.966	499.932	599.882
1	100.001	199.992	299.979	399.947	499.894	599.815
10	.002	199.990	299.970 299.959	399.924 399.896	499.848 499.793	599.733
20	.002	199.986	299.946	399.865	499.729	599.637 599.526
30	.003	199.983	299.932	399.829	499.657	599.401
40	.003	199.979	299.915	399.789	499.577	599.260
50	.004	199.974	299.898	399.744	499.488	599.105
2	100.005	THE REAL PROPERTY.		The second second		1
10	.006	199.970	299.878	399.695	499.391	598.934
20	.007	199.964 199.959	299.857	399.643	499.285	598.750
30	.008	199.959	299.834 299.810	399.586	499.171	598.550
40	.009	199.932		399.524	499.049	598.336
50	.010	199.939	299.783 299.756	399.459 399.389	498.918 498.778	598.106
3	100.011	199.931	299.726	399.315	498.630	597.862 597.604
10	.013	199.924	299.695	399.237	498.474	597.331
20	.014	199.915	299.662	399.154	498.309	597.043
30	.015	199.907	299.627	399.068	498.136	596.740
40	.017	199.898	299.591	398.977	497.955	596.423
50	,019	199.888	299.553	398.882	497.765	596.091
4	100.020					The second second
10	.022	199.878	299.513	398.782	497.566	595.744
20	.024	199,868 199,857	299.471	398.679	497.360 497.145	595.383
30	.026	199.846	299.428 299.383	398.571 398.459	496.921	595.007
40	.028	199.834	299.337	398.343	496.689	594.617 594.212
50	,030	199.822	299.289	398.223	496.449	593.792
5	100.032	199.810	299.239	398.099	496.201	593.358
10	.034	199.797	299.187	397,970	495.944	592.909
20	.036	199.783	299.134	397.837	495.678	592.446
30	.038	199.770	299.079	397.700	495.405	591.968
40	.041	199.756	299.023	397.700 397.559	495.123	591.476
50	.043	199.741	298.964	397.413	494.832	590.970
6	100.046	199.726	298,904	397.264	494.534	590.449
10	.048	199.710	298.843	397.110	494.227	589.913
20	.051	199,695	298.779	396.952	493.912	589.364
30	.054	199.678	298.714	396.790	493.588	588.800
40	.056	199.662	298.648	396.623	493.257	588.221
50	.059	199.644	298.579	396.453	492.917	587.628
7	100.062	199.627	298.509	396.273	492.568	587.021
10	.065	199.609	298.438	396.099	492.212	586.400
20	.068	199.591	298.364	395.916	491.847	585.765
30	.071	199.572	298.289	395.729	491.474	585.115
40	.075	199.553	298.212	395.538	491.093	584.451
50	.078	199.533	298.134	395.342	490.704	583.773
8	100.081	199.513	298,054	395.142	490.306	583.081
10	.085	199.492	297.972	394.938	489.900	582.375
20	.088	199.471	297.888	394.731	489.486	581.654
30	.092	199.450	297.803	394.518	489.064	580.920
40	.095	199.428	297.716	394.302	488.634	580.172
50	.099	199,406	297.628	394.082	488.196	579.409
9	100.103	199.383	297.538	393.857	487.749	578.633
10	.107	199.360	297.446	393.629	487.294	577.843
20	.111	199.337	297.352	393.396	486.832	577.039
30	.115	199.313	297.257	393.159	486.361	576.222
40	.119	199.289	297.257 297.160 297.062	392.918	485.882	575.390
50	.123	199.264	297.062	392.673	485.395	574.545
10	100.127	199.239	296.962	392.424	484.900	573.686

TABLE V.-LONG CHORDS.

Degree of	Actual Arc,	Long Chords.						
			Mr Level	1		Degree		
Curve.	One Station.	Stations.	Stations.	Stations.	Stations.	Stations		
10° 10′	100.131	199.213	296.860	392.171	484.397	572.813		
20 30	.136	199.187 199.161	296.756 296.651	391.914 391.652	483.886 483.367	571.926 571.027		
40	.145	199.134	296.544	391.387	482.840	570.113		
50	.149	199.107	296.436	391.117	482.305	569.186		
11	100.154	199.079	296.325	390.843	482.305 481.762	568.245		
10 20	.158	199.051 199.023	296.214	390.565 390.284	481.211 480.653	567.292 566.324		
30	.168	198.994	296.100 295.985	389.998	480.086	565:343		
40	.173	198.964	295.868	389.708	479.511	564.349		
50	.178	198.935	295.750	389.414	478.929	563.341		
12	100.183	198.904 198.874	295.629 295.508	389.116 388.814	478.338 477.740	562.321 561.287		
20	.193	198.843	295.384	388.508	477.135	560.240		
30	.199	198.811	295.259	388.197	476.521	559.180		
40	.204	198.779	295.132	387.883	475.899	558.107		
13 50	.209	198.747	295.004	387.565 387.243	475.270	557.020		
13	100.215	198.714 198.681	294.874 294.742	387.243 386.916	474.633 473.988	555.921		
20	.226	198.648	294,609	386.586	473.336	553.68		
30	.232	198.614	294.474	386.252	472.675	552.540		
40 50	.237	198.579 198.544	294.337 294.199	385.914 385.572	472.007 471.332	551.395 550.235		
14	100.249	198.509	294.059	385.225	470.649	549.056		
10	.255	198.474	293.918	384.875	469.958	547.867		
20	-261	198.437	293.774	384.521	469.260	546.660		
30	-267	198.401	293.629	384.163	468.554	545.45		
40 50	274	198.364 198.327	293,483 293,335	383.801 383.435	467.840 467.119 466.390	544.226		
15	100.286	198.289	293.185	383.065	466 390	542.987 541.736		
10	.292	198.251	293.034	382.691	465.654	540.47		
20	-299	198.212	292.881	382.313	464.911	539.196		
30 40	-306	198.173	292.726	381.931	464.160	537.908		
50	.312	198.134 198.094	292.570 292.412	381.546 381.156	463.401 462.635	536.606 535.29		
16;	100.326	198.054	292.252	380.763	461.862	533.97		
10	.333	198.013	292.091	380.365	461.081	532.633		
20 30	.339	197.972 197.930	291.928 291.764	379.964 379.559	460.293	531.287 529.927		
40	.353	197.888	291.598	379.150	459.498 458.695	528.55		
50	.361	197.846	291.430	378.737	457.886	527.171		
17	100.368	197.803	291.261	378.320	457.069	527.171 525.776		
10 20	.375	197.760 197.716	291.090	377.900	456.244	524.369		
30	390	197.672	290.918 290.743	377.475 377.047	455.413 454.574	522.950 521.519		
40	.397	197.628	290.568	376.615	453.728	520.078		
50	.405	197.583	290.390	376.179	452.875	518.625		
10	100.412	197.538 197.492	290.211 290.031	375.739 375.295	452.015 451.147	517.160 515.685		
20	.428	197.446	289.849	374.848	450.373	514.198		
30	.436	197.399	289.665	374.397	449.392	512.699		
40 50	.444	197.352 197.305	289.479 289.292	373.942	448.504 447.608	511.190		
19	100.460	197.256	289.293	373.483 373.021	447.008	509.670 508.139		
10	.468	197.209	288.913	372.554	445.797	506.597		
20	.476	197.160	288.722	372.084	444.881	505.043		
30 40	.484	197.111	288.528	371.610	443.957	503.479		
50	.493	197.062 197.012	288.833 288.137	371.133 370.652	443.028 442.091	501.905 500,320		
20	100.510	196.962	287.939	370.167	441.147	498.724		

	1	Factorizes	Way S			
Degree of Curve.	Station.	Stations.	Stations.	Stations.	5 Stations.	6 Stations
0° 10′ 20 30 40 50 1 10 20 30 40 50	.036 .073 .109 .145 .188 .218 .255 .201 .327 .364 .400	.145 .291 .436 .582 .727 .873 1.018 1.164 1.309 1.454 1.600	.327 .654 .982 1.309 1.636 1.963 2.291 2.618 2.945 3.272 3.599	.582 1.164 1.745 2.327 2.909 3.490 4.072 4.654 5.235 5.816 6.398	.909 1.818 2.727 3.636 4.545 5.453 6.362 7.270 8.179 9.087 9.994	1.309 2.618 3.926 5.235 6.544 7.852 9.160 10.468 11.775 13.082 14.389
2 10 20 30 40 50 30 40 50	.436 .473 .509 .545 .582 .618 .654 .691 .727 .703 .800	1.745 1.891 2.036 2.181 2.327 2.472 2.618 2.763 2.908 3.054 3.199 3.345	3.926 4.253 4.580 4.907 5.234 5.561 5.888 6.215 6.542 6.868 7.195 7.522	6.979 7.560 8.141 8.722 9.303 9.883 10.464 11.044 11.624 12.204 13.784 13.363	10.902 11.809 12.716 13.623 14.529 15.435 16.341 17.246 18.151 19.055 19.959 20.863	15.694 17.000 18.304 19.608 20.912 22.214 23.516 24.817 26.117 27.416 28.714 30.012
4 10 20 30 40 50 5 10 20 30 40 50 5 10 20 30 40 50 50 50 50 50 50 50 50 50 5	.872 .909 .945 .982 1.018 1.054 1.091 1.127 1.164 1.200 1.237 1.273	3.490 3.635 3.781 3.926 4.071 4.217 4.362 4.507 4.653 4.798 4.943 5.088	7.848 8.175 8.501 8.828 9.154 9.480 9.807 10.133 10.459 10.785 11.111 11.436	13.943 14.522 15.101 15.680 16.258 16.887 17.415 17.992 18.570 19.147 19.724 20.201	21.766 22.668 23.570 24.471 25.372 26.272 27.171 28.070 28.968 29.866 30.762 31.658	31,308 32,603 33,896 35,189 36,480 37,770 39,059 40,346 41,631 42,916 44,198 45,479
6 20 30 40 50 7 10 20 30 40 50 7	1.309 1.346 1.382 1.418 1.455 1.491 1.528 1.564 1.600 1.637 1.673 1.770	5. 234 5. 379 5. 524 5. 669 5. 814 5. 960 6. 105 6. 250 6. 395 6. 540 6. 685 6. 831	11.762 12.088 12.413 12.739 13.064 13.389 13.715 14.040 14.365 14.689 15.014 15.339	20.877 21.453 22.029 22.604 23.179 23.754 24.328 24.902 25.476 26.049 26.622 27.195	32.553 33.448 34.341 35.234 36.126 37.017 37.907 38.796 39.684 40.571 41.458 42.343	46,759 48,037 49,313 50,587 51,860 53,130 54,399 55,666 56,931 58,193 59,454 60,712
8 10 20 30 40 50 9 10 20 80 40 50 10	1.746 1.782 1.819 1.855 1.892 1.928 1.965 2.001 2.037 2.074 2.110 2.147 2.183	6.976 7.121 7.266 7.411 7.556 7.701 7.846 7.991 8.136 8.281 8.426 8.571 8.716	15.663 15.988 16.312 16.636 16.960 17.284 17.608 17.932 18.255 18.578 18.902 19.225 19.548	27.767 28.338 28.910 29.481 30.051 30.621 31.190 31.759 32.328 32.328 33.464 34.031 34.597	43,227 44,110 44,992 45,873 46,753 47,632 48,510 49,386 50,261 51,135 52,008 52,880 53,750	61.969 63.223 64.475 65.724 66.972 68.216 69.459 70.699 71.936 73.171 74.403 75.632 76.839

Degree of Curve.	Station.	2 Stations.	3 Stations.	4 Stations.	5 Stations.	6 Stations.
10° 10′ 20 30 40 50 11 10 20 30 40 50	2.219 2.256 2.293 2.329 2.365 2.402 2.438 2.475 2.511 2.547	8.860 9.005 9.150 9.295 9.440 9.585 9.729 9.874 10.019 10.164 10.308	19.870 20.193 20.516 20.838 21.160 21.483 21.804 22.126 22.448 22.769 23.090	35.164 35.729 36.294 36.859 37.423 37.986 38.549 39.111 39.673 40.234 40.795	54.619 55.486 56.853 57.218 58.081 58.943 59.804 60.663 61.521 62.377 63.232	78.083 79.305 80.523 81.739 82.951 84.161 85.368 86.571 87.772 88.969 90.164
12 10 20 30 40 50 30 40 50	2.657 2.657 2.698 2.730 2.766 2.803 2.839 2.876 2.912 2.949 2.949 2.985 3.022	10.453 10.597 10.742 10.887 11.081 11.176 11.320 11.465 11.609 11.754 11.898 12.043	23, 412 23, 732 24, 053 24, 374 24, 694 25, 014 25, 334 25, 654 25, 974 26, 298 26, 612 26, 981	41 . 355 41 . 914 42 . 473 43 . 031 43 . 588 44 . 145 44 . 701 45 . 256 45 . 811 46 . 365 46 . 919 47 . 472	64 .085 64 .937 65 .787 66 .636 67 .482 68 .328 69 .171 70 .012 70 .854 71 .692 72 .529 73 .364	91.355 92.542 93.727 94.908 96.086 97.260 98.431 99.598 100.762 101.922 103.079 104.232
14 10 20 30 40 50 15 10 20 30 40 40 50 40 20 30 40 40 50 40 50 40 50 40 50 40 50 40 50 50 60 60 60 60 60 60 60 60 60 6	3.058 3.095 3.131 3.168 3.204 3.241 3.277 3.314 3.350 3.387 3.423 3.460	12. 187 12. 331 12. 476 12. 620 12. 764 12. 908 13. 053 13. 197 13. 341 13. 485 13. 629 13. 773	27. 250 27. 569 27. 887 28. 206 28. 524 28. 841 29. 159 29. 476 29. 794 30. 111 30. 427 30. 744	48.024 48.575 49.126 49.676 50.225 50.773 51.321 51.868 52.414 52.959 53.504 54.048	74.197 75.029 75.859 76.687 77.513 78.337 79.159 79.979 80.798 81.614 82.429 83.241	105.881 106.527 107.669 108.807 109.941 111.071 112.197 113.319 114.438 115.552 116.662 117.768
16 20 30 .40 50 17 10 20 30 40 50	3.496 3.533 3.569 3.606 3.643 3.679 3.716 3.752 3.789 3.862 2.899	13.917 14.061 14.205 14.349 14.493 14.637 14.781 14.925 15.069 15.212 15.356 15.500	31.060 31.376 31.692 32.008 32.323 32.638 32.953 33.267 33.582 33.896 34.210 34.523	54.591 55.133 55.675 56.215 56.755 57.294 57.832 58.369 58.906 59.441 59.976 60.510	84 .052 84 .861 85 .667 86 .471 87 .274 88 .074 88 .872 89 .668 90 .462 91 .254 92 .043 92 .830	118.870 119.967 121.061 122.150 123.235 124.315 125.891 126.463 127.580 128.593 129.651 130.704
18 10 20 30 40 50 19 10 20 30 40 40 50 20	3.935 3.972 4.008 4.045 4.081 4.118 4.155 4.191 4.228 4.265 4.301 4.338 4.374	15.643 15.787 15.981 16.074 16.218 16.361 16.505 16.648 16.792 16.985 17.078 17.222 17.365	34,837 35,150 35,463 35,775 36,088 36,400 36,712 37,023 37,334 37,645 37,956 38,266 38,576	61.042 61.574 62.106 62.636 63.165 63.693 64.221 64.747 65.273 65.797 66.821 66.843 67.365	93.616 94.398 95.179 95.957 96.733 97.506 98.278 99.047 99.813 100.577 101.339 102.098 102.855	131.753 132.797 133.837 134.872 135.902 136.928 137.948 138.964 139.975 140.981 141.982 142.978 143.969

,	0"	10"	15"	20"	30"	40"	45"	50"	1.
1	.00000	00278	.00417	.00556	.00833	01111	01050	04900	
0	.01667	.01944	.02083	.02222	.02500	.01111	.01250	.01389	0
2	.03333	.03611	.03750	.03889	.04167	.04444	.04583	.04722	2
3	.05000	.05278	.05417	.05556	.05833	.06111	.06250	.06389	3
4	.06667	.06944	.07083	.07222	.07500	.07778	.07917	.08056	4
5 6	.08333	.08611	.08750	.08889	.09167	.09444	.09583	.09722	5 6
7	.11667	.11944	.12083	.12222	12500	.12778	,12917	.13056	7
8	.13333	,13611	.13750	.13889	.14167	.14444	.14583	.14722	8
9	.15000	.15278	.15417	.15556	.15833	.16111	.16250	.16389	9
10	.16667	.16944	,17083	.17222	.17500	.17778	.17917	.18056	10
11	.18333	.18611	.18750	.18889	.19167	19111	.19583	.19722	111
12	.20000	.20278	.20417	.20556	,20833	.21111	.21250	.21389	12
13	.21667	.21944	.22083	,22222	,22500	.22778	.22917	.23056	13
14	.23333	.23611	.23750	.23889	.24167	.24444	.24583	.24722	14
16	26667	26944	.27083	27222	27500	27778	.27917	.28056	15 16
17	28333	.28611	.28750	- 28889	29167	29444	29583	.29722	17
18	.30000	.30278	.30417	.30556	.30833	.31111	.31250	.31389	18
19	.31667	.31944	.32083	.32222	.32500	.32778	.32917	.33056	19
20	,33333	.33611	.33750	.33889	.34167	.34444	.34583	.34722	20
21	,35000	.35278	.35417	.35556	.35833	.36111	.36250	.36389	21
22	.36667	.36944	.37083	.37222	.37500	.37778	.37917	.38056	22
23 24	.38333	.38611	.38750 .40417	,38889 ,40556	.39167	.39444	.39583	.39722	23
25	41667	41944	.42083	42222	.42500	.42778	42917	.41389	24 25
26	43333	43611	.43750	43889	.44167	41111	,44583	.44722	26
27	45000	45278	.45417	.45556	.45833	.46111	.46250	.46389	27
28	.46667	.46944	.47083	.47222	.47500	.47778	.47917	.48056	28
29	.48333	.48611	.48750	.48889	.49167	.49444	.49583 .51250	.49722	29
30		The state of the s		100000		10.000	1	.51389	30
31	.51667	.51944	.52083	.52222	.52500	.52778	.52917	.53056	31
32 33	.53333	.53611	.53750	.53889	.54167	.54444	.54583	.54722	32
34	56667	.56944	.57083	.57222	.57500	57778	.57917	.58056	34
35	58333	.58611	.58750	.58889	.59167	,59444	.59583	.59722	35
36	.60000	.60278	.60417	.60556	.60833	.61111	.61250	.61389	36
37	.61667	.61944	.62083	.62222	.62500	.62778	.62917	.63056	37
38	65000	.63611	.63750	.63889	.64167	.64444	.64583	.64722	38
39 40	.66667	.66944	67083	67222	.67500	.67778	.67917	.68056	40
	.68333	,68611	.68750	.68889	.69167	.69444	.69583	.69722	41
41 42	70000	70278	.70417	.70556	.70833	.71111	.71250	.71389	42
43	71667	71944	72083	72222	72500	.72778	72917	.73056	43
44	.73333	.73611	.73750	.73889	.74167	.74444	.74583	.74722	44
45	.75000	.75278	.75417	.75556	.75833	.76111	.76250	.76389	45
46	.76667	.76944	.77083	.77222	.77500	.777778	.77917	.78056	46
47 48	.78333	.78611	.78750	.78889	.79167	.79444	,81250	.79722	47
49	.81667	.81944	82083	.82222	.82500	.82778	82917	.83056	49
50	.83333	.83611	.83750	.83889	.84167	.81111	.84583	.84722	50
51	,85000	.85278	.85417	.85556	,85833	86111	.86250	.86389	51
52	.86667	.86944	.87083	.87222	.87500	.87778	.87917	.88056	52
53 54	.88333	.88611	.88750	.88889	.89167	.89444	.89583	.89722	53
54 55	.90000	.90278	.90417	.90556	.90833	.91111	.91250 .92917	.91389	54 55
56	.93333	.93611	.93750	.93889	.94167	.94444	.94583	.94722	56
57	.95000	.95278	.95417	.95556	.95833	.96111	.96250	.96389	57
58	.96667	.96914	.97083	.97222	.97500	.97778	.97917	.98056	58
59	.98333	.98611	.98750	.98889	.99167	.99414	.99583	.99722	59
1	0"	10"	15"	20"	30"	40"	45"	50"	,

,					
No.	Squares.	Cubes.	Square Roots.	Cube Roots.	Reciprocals.
1 2 3 4 5 6 7 8	1 4 9 16 25 36 49 64 81	1 8 27 64 125 216 343 512 729	1.0000000 1.4142136 1.7320508 2.0000000 2.2360680 2.4494897 2.6457513 2.8284271 3.0000000	1.0000000 1.2599210 1.4422496 1.5874011 1.7090759 1.8171206 1.9129312 2.000000 2.0800837	1.00000000 .50000000 .3333333 .25000000 .20000000 .16666667 .142857143 .125000000 .111111111
10 11 12 13 14 15 16 17 18	100 121 144 169 196 225 256 289 324 361	1000 1831 1728 2197 2744 3875 4006 4913 5882 6859	3.1622777 3.3166248 3.4641016 3.6055513 3.7416574 3.8729833 4.000000 4.1231056 4.2426407 4.3588989	2.1544347 2.2239801 2.2894286 2.3513347 2.4101422 2.4662121 2.5198421 2.5712816 2.6207414 2.6684016	.10000000 .09000091 .08323333 .076923077 .071428571 .066666667 .06250000 .058828529 .05555556 .052631579
20 21 22 23 24 25 26 27 28 29	400 441 484 529 576 625 676 729 784 841	8000 9261 10648 12167 13824 15625 17576 19883 21952 24389	4.4721360 4.5825757 4.6904158 4.7958315 4.8980795 5.0000000 5.0990195 5.1961524 5.2915026 5.3851648	2.7144177 2.7589243 2.8020393 2.8428670 2.8844991 2.9240177 2.9624960 3.0000000 3.0365889 3.0723168	.05000000 .047619048 .045454545 .043478261 .041666667 .04000000 .038461538 .037037037 .035714286 .034482759
30 31 32 33 34 35 36 37 38	900 961 1024 1089 1156 1225 1296 1369 1444 1521	27000 29791 32768 35937 39304 42875 46656 50653 54872 59319	5.4772256 5.5677644 5.6568542 5.7445626 5.8309519 5.9160798 6.000000 6.0827625 6.1644140 6.2449980	3.1072325 3.1418806 3.1748021 3.2075343 3.2396118 3.2710663 3.3019272 3.3322218 3.3619754 8.3912114	.03333333 .032258065 .031250000 .030303030 .029411765 .028571429 .027777778 .027027027 .026315789 .035641026
40 41 42 43 44 45 46 47 48 49	1600 1681 1764 1849 1936 2025 2116 2209 2304 2401	64000 68921 74088 79507 851\$4 91125 97836 103823 110592 117649	6,3245553 6,4031242 6,4807407 6,5574385 6,6332496 6,7082039 6,7823300 6,8556546 6,9282032 7,0000000	3,4199519 3,4482172 3,4760266 3,5033981 3,5303483 3,5568933 3,5830479 3,6088261 2,6342411 3,6599057	.02500000 .024300244 .023809524 .023855814 .022727273 .022222222 .021739130 .021276600 .020833333 .020408163
50 51 52 53 54 55 56 57 58 59	2500 2601 2704 2809 2916 3025 3136 3249 3364 3481	125000 132651 140608 148877 157464 166375 175616 185193 195112 205379	7.0710678 7.1414284 7.2111026 7.2801099 7.3484692 7.4161985 7.4833148 7.5498344 7.6157731 7.6811457	3.6840314 3.7084298 3.7325111 3.7562858 3.7797631 3.8020525 3.8258624 3.8485011 3.8708766 .3.8929965	.02000000 .019607843 .019290769 .018867925 .018518519 .018181818 .017543860 .017241379 .016949153
60 61 62	3600 3721 3844	216000 226981 238328	7.7459667 7.8102497 7.8740079	3.9148676 3.9364972 3.9578915	.016666667 .016393443 .016129032

	A-Product				
No.	Squares.	Cubes.	Square Roots.	Cube Roots.	Reciprocals.
63 64 65 66 67 68 69	3969 4096 4225 4356 4489 4624 4761	250047 262144 274625 287496 300763 314432 328509	7.9372539 8.0000000 8.0622577 8.1240384 8.1853528 8.2462113 8.3066239	8.9790571 4.0000000 4.0207256 4.0412401 4.0615480 4.0816551 4.1015661	.015873016 .015625000 .015384615 .015151515 .014925373 .014705882 .014492754
70 71 72 73 74 75 76 77 78 79	4900 5041 5184 5329 5476 5625 5776 5929 6084 6241	343000 357911 373248 389017 405224 421875 438976 456533 474552 498039	8.3666003 8.4261498 8.4852814 8.5440037 8.6023253 8.6602540 8.7177079 8.7749644 8.8317609 8.8881944	4.1212853 4.1408178 4.1601676 4.1793390 4.1983364 4.2171633 4.2358236 4.2543210 4.2726586 4.2908404	.014985714 .014084507 .013888889 .013698630 .013513514 .013333333 .013157895 .012987013 .012850513 .012658228
80 81 82 83 84 85 86 87 88	6400 6561 6724 6889 7056 7225 7396 7569 7744 7921	512000 531441 551368 571787 592704 614125 636056 658503 681472 704969	8.9442719 9.0000000 9.0553851 9.1104336 9.1651514 9.2195445 9.2736185 9.3273791 9.3808315 9.4339811	4.3088095 4.3267487 4.3444815 4.3620707 4.3795191 4.3968296 4.4140049 4.4310476 4.4479602 4.4647451	.012500000 .012345679 .012195122 .612048193 .011904762 .011764706 .011627907 .011494253 .011263636 .011235955
90 91 92 93 94 95 96 97 98	8100 8281 8464 8649 8836 9025 9216 9409 9604 9801	729000 753571 778688 804357 830584 857375 884736 912673 941192 970299	9.4868330 9.5393930 9.5916630 9.6436508 9.6953597 9.7467943 9.7979590 9.8488578 9.8994949 9.9498744	4.4814047 4.4979414 4.5143574 4.5306549 4.5468359 4.5629026 4.5788570 4.5947009 4.6104363 4.6260650	.01111111 .010989011 .010869565 .010752688 .010638398 .010526316 .010416667 .010309278 .010204082 .010101010
100 101 102 103 104 105 106 107 108	10000 10201 10404 10609 10816 11025 11236 11449 11664 11881	1000000 1030301 1061208 1092727 1124864 1157625 1191016 1225043 1259712 1295029	10.000000 10.0498756 10.0995049 10.1488916 10.1980390 10.2469508 10.2956301 10.3140804 10.3923048 10.4403065	4.6415888 4.6570095 4.6723287 4.6875482 4.7026694 4.7176940 4.7326235 4.7474594 4.7622032 4.77768562	.01000000 .00900990 .009803922 .009708738 .009615385 .009523810 .009433962 .009345794 .000259259 .009174312
110 111 112 113 114 115 116 117 118 119	12100 12321 12544 12769 12996 13225 13456 13689 13924 14161	1331000 1367631 1404928 1442897 1481544 1520875 1560896 1601613 1643032 1685159	10.4890865 10.5356538 10.582052 10.6301458 10.(770783 10.7238053 10.7703296 10.8166538 10.8027805 10.9087121	4.7914199 4.8058955 4.8202845 4.8345881 4.8488076 4.8629442 4.8769990 4.8909732 4.9048681 4.9186847	.009090909 .009009009 .0080285,1 .008849558 .008771930 .008695652 .008620690 .008547009 .00844376 .008403361
120 121 122 123 124	14400 14641 14884 15129 15376	1728000 1771561 1815848 1860867 1906624	10.9544512 11.00.0000 11.0453610 11.0905365 11.1355287	4.9324242 4.9460874 4.9596757 4.9731898 4.9866310	.008333333 .008264463 .008196721 .008130081 .008064516

No.	Squares.	Cubes.	Square Roots.	Cube Roots,	Reciprocals.
405	4200	4050405	44 4000000	F 0000000	000000000
125	15625	1953125	11.1803399	5.0000000	.008000000
126	15876	2000376	11.2249722	5.0132979	.007936508
127	16129	2048383	11.2694277	5.0265257	.007874016
128	16384	2097152	11.3137085	5.0396842	.007812500
129	16641	2146689	11.3578167	5.0527743	.007751938
130	16900	2197000	11.4017543	5.0657970	.007692308
131	17161	2248091	11.4455231	5.0787531	.007633588
132	17424	2299968	11.4891253	5.0916434	.007575758
133	17689	2352637	11.5325626	5.1044687	.007518797
134	17956	2406104	11.5758369	5.1172299	.007462687
135	18225	2460375	11.6189500	5.1299278	.007407407
136	18496	2515456	11.6619038	5.1425632	.007352941
137	18769	2571353	11.7046999	5.1551367	.007299270
138	19044	2628072	11.7473401	5.1676493	.007246377
139	19321	2685619	11.7898261	5.1801015	.007194245
140	19600	2744000	11.8321596	5.1924941	.007142857
141	19881	2803221	11.8743421	5.2048279	.007092199
142	20164	2863288	11.9163753	5.2171034	.007042254
143	20449	2924207	11.9582607	5.2293215	.006993007
144	20736	2985984	12.0000000	5.2414828	.006941141
145	21025	3048625	12.0415946	5.2535879	.006896552
146	21316	3112136	12,0830460	5.2656374	.006849315
147	21609	3176523	12.1243557	5.2776321	.006802721
148	21904	3241792	12.1655251	5.2895725	.006756757
149	22201	3307949	12.2065556	5.3014592	.006711409
150	22500	3375000	12.2474487	5,3132928	
151	22801	3442951	12.2882057		.006666667
152	23104	3511808	12.3288280	5.3250740 5.3368033	.006622517
153	23409	3581577	12.3693169	5.3484812	.006535948
154	23716	3652264	12.4096736	5.3601084	.006493506
155	24025	3723875	12,4498996	5.3716854	.006451613
156	24336	3796416	12.4899960	5.3832126	.006410256
157	24649	3869893	12.5299641	5 3946907	.006369427
158	24964	3944312	12.5698051	5.4061202	.006329114
159	25281	4019679	12.6095202	5.4175015	.006289308
160	25600	4096000	12.6491106	5,4288352	.006250000
161	25921	4173281	12.6885775	5.4401218	.000230000
162	26244	4251528	12.7279221	5.4513618	.006172840
163	26569	4330747	12.7671453	5.4625556	.006134969
164	26896	4410944	12.8062485	5,4737037	.006097561
165	27225	4492125	12.8452326	5.4848066	.006060606
166	27556	4574296	12.8840987	5.4958647	.006024096
167	27889	4657463	12.9228480	5.5068784	.005988024
168	28224	4741632	12.9614814	5.5178484	.005952381
169	28561	4826809	13.0000000	5.5287748	.005917160
170	28900	4913000	13.0394048	5.5396583	.005882353
171	29241	5000211	13.0766968	5.5504991	.005847953
172	29584	5088448	13.1148770	0.5612978	.005813953
173	29929	5177717	13,1529464	5.5720546	.005780347
174	30276	5268024	13.1909060	5.5827702	.005747126
175	30625	5359375	13,2287566	5.5934447	.005714286
176	30976	5451776	13.2664992	5.6040787	.005681818
177	31329	5545233	13.3041347	5.6146724	.005649718
178	31684	5639752	13.3416641	5.6252263	.005617978
179	32041	5735339	13.3790882	5.6357408	.005586592
180	32400	5832000	13.4164079	5.6462162	.005555556
181	32761	5929741	13.4536240	5.6566528	.005524862
182	33124	6028568	13.4907376	5.6670511	.005494505
183	33489	6128487	13.5277493	5 6774114	.005464481
184	33856	6229504	13.5646600	5.6877340	.005434783
185	34225	6331625	13.6014705	5.6980192	.005405405
186	34596	6434856	13.6381817	5.7082675	.005376344

No.	Squares.	Cubes.	Square Roots.	Cube Roots.	Reciprocals.
187	34969	6539203	13.6747943	E 0404004	005045504
188	35344	6644672	13.7113092	5.7184791 5.7286543	.005347594
189	35721	6751269	13.7477271	5.7387936	.005291005
190	36100	6859000	13.7840488	5.7488971	.005263158
191	36481	6967871	13.8202750	5.7589652	.005235602
192	36864	7077888	13.8564065	5.7689982	.005208333
193 194	37249	7189057	13.8924440	5.7789966	.005181347
194	37636 38025	7301384 7414875	13.9283883 13.9642400	5.7889604 5.7988900	.005154639
196	38416	7529536	14.0000000	5.8087857	.005128205
197	38809	7645373	14.0356688	5.8186479	.005076142
198	39204	7762392	14.0712473	5.8284767	.005050505
199	39601	7880599	14.1067360	5.8382725	.005025126
200	40000	8000000	14.1421356	5.8480355	.005000000
201	40401	8120601	14.1774469	5.8577660	.004975124
202 203	40804 41209	8242408 8365427	14.2126704 14.2478068	5.8674643 5.8771307	.004950495
204	41616	8489664	14.2828569	5.8867653	.004926108
205	42025	8615125	14.3178211	5.8963685	.004878049
206	42436	8741816	14.3527001	5.9059406	.004854369
207	42849	8869743	14.3874946	5.9154817	.004830918
208 209	43264 43681	8998912 9129329	14.4222051 14.4568323	5.9249921 5.9344721	.004807692
	THE STREET	THE R. P. LEWIS CO., LANSING, MICH. 49, 100		C. P. Printers of the Control of the	.004784689
210 211	44100	9261000	14.4913767	5.9439220	.004761905
212	44521 44944	9393931 9528128	14.5258390 14.5602198	5.9533418 5.9627320	.004739336
213	45369	9663597	14.5945195	5.9720926	.004694836
214	45796	9800344	14.6287388	5.9814240	.004672897
215	46225	9938375	14.6628783	5.9907264	.004651163
216 217	46656 47089	10077696 10218313	14.6969385 14.7309199	6.0000000	.004629630
218	47524	10360232	14.7648231	6.0092450 6.0184617	.004608295
219	47961	10503459	14.7986486	6.0276502	,004566210
220	48400	10648000	14.8323970	6.0368107	.004545455
221	48841	10793861	14.8660687	6.0459435	.004524887
222	49284	10941048	14.8996644	6.0550489	.004504505
223	49729	11089567	14.9331845	6.0641270	.004484305
224 225	50176 50625	11239424 11390625	14.9666295 15.0000000	6.0731779 6.0822020	.004464286
226	51076	11543176	15.0332964	6.0911994	.004424779
227	51529	11697083	15,0665192	6.1001702	.004405286
228	51984	11852352	15.0996689	6.1091147	.004385965
229	52441	12008989	15.1327460	6.1180332	.004366812
230	52900	12167000	15.1657509	6.1269257	.004347826
231	53361	12326391	15.1986842	6.1357924	.004329004
232 233	53824 54289	12487168 12649337	15.2315462 15.2643375	6.1446337 6.1534495	.004310345
234	54756	12812904	15.2970585	6.1622401	.004273504
235	55225	12977875	15,3297097	6.1710058	.004255319
236	55696	13144256	15.3622915	6.1797466	.004237288
237	56169	13312053	15.3948043	6.1884628	.004219409
238 239	56644 57121	13481272 13651919	15.4272486 15.4596248	6.1971544 6.2058218	.004201681
		A CONTRACTOR OF THE PARTY OF TH	The second secon	and the second second	
240 241	57600 58081	13824000 13997521	15.4919334 15.5241747	6.2144650 6.2230843	.004166667
242	58564	14172488	15.5563492	6.2316797	.004132231
243	59049	14348907	15.5884573	6.2402515	.004115226
244	59536	14526784	15.6204994	6.2487998	.004098361
- 245 - 246	60025 60516	14706125	15.6524758	6.2573248 6.2658266	.004081633
240 247	61009	14886936 15069223	15.6843871 15.7162336	6.2743054	.004048583
248	61504	15252992	15.7480157	6.2827613	.004032258
	200				

No.	Squares.	Cubes.	Square Roots.	Cube Roots.	Reciprocals.
249	62001	15438249	15.7797338	6.2911946	.004016064
90000				Control of the Address	
250	62500	15625000 15813251	15.8113883 15.8429795	6.2996053 6.3079935	.004000000
251	63001 63504	16003008	15.8745079	6.3163596	.003968254
252 253	64009	16194277	15.9059737	6.3247035	.003952569
254	64516	16387064	15.9373775	6.3330256	.003937008
255	65025	16581375	15.9687194	6.3413257	.003921569
256	65536	16777216	16.0000000	6.3496042	,003906250
257	66049	16974593	16.0312195	6.3578611	.003891051
258	66564	17173512	16.0623784	6.3660968	.003875969
259	67081	17373979	16.0934769	6.3743111	.003861004
260	67600	17576000	16.1245155	6.3825043	.003846154
261	68121	17779581	16.1554944	6.3906765	,003831418
262	68644	17984728	16.1864141	6.3988279	.003816794
263	69169	18191447	16.2172747	6.4069585	.003802281
264	69696	18399744	16.2480768	6.4150687	.003787879
265	70225	18609625	16.2788206	6.4231583	.003773585
266	70756	18821096 19034163	16.3095064	6.4312276	.003759398
267 268	71289 71824	19248832	16.3401346 16.3707055	6.4392767 6.4473057	.003745318
269	72361	19465109	16,4012195	6.4553148	.003717472
The second secon			STATE OF THE PARTY	AND THE RESERVE	Edward Company
270	72900	19683000	16.4316767	6.4633041	.003703704
271	73441	19902511 20123648	16.4620776 16.4924225	6.4712736 6.4792236	.003690037
272 273	73984 74529	20346417	16.5227116	6.4871541	.003676471
274	75076	20570824	16.5529454	6.4950653	.003649635
275	75625	20796875	16.5831240	6,5029572	.003636364
276	76176	21024576	16.6132477	6.5108300	.003623188
277	76729	21253933	16.6433170	6.5186839	.003610108
278	77284	21484952	16.6733320	6.5265189	.003597122
279	77841	21717639	16.7032931	6.5343351	.003584229
280	78400	21952000	16.7332005	-6.5421326	.003571429
281	78961	22188041	16.7630546	6.5499116	.003558719
282	79524	22425768	16.7928556	6.5576722	.003546099
283	80089	22665187	16.8226038	6.5654144	.003533569
284 285	80656 81225	22906304 23149125	16.8522995 16.8819430	6.5731385	.003521127
286	81796	23393656	16.9115345	6.5808443	.003508772
287	82369	23639903	16.9410743	6.5962023	.003484321
288	82944	23887872	16.9705627	6.6038545	.003472222
289	83521	24137569	17.0000000	6.6114890	.003460208
290	84100	24389000	17.0293864	6.6191060	.003448276
291	84681	24642171	17.0587221	6.6267054	.003436426
292	85264	24897088	17.0880075	6.6342874	.003424658
293	85849	25153757	17.1172428	6.6418522	.003412969
294	86436	25412184	17.1464282	6.6493998	.003401361
295	87025	25672375	17.1755640	6.6569302	.003389831
296	87616	25934336	17.2046505	6.6644437	.003378378
297 298	88209 88804	26198073 26463592	17.2336879	6.6719403	.003367003
299	89401	26730899	17.2626765 17.2916165	6.6794200	.003355705
				The second second	
300 301	90000	27000000	17.3205081	6.6943295	.003333333
302	90601 91204	27270901 .27543608	17.3493516 17.3781472	6.7017593	.003322259
303	91809	27818127	17,4068952	6.7091729 6.7165700	.003311258
304	92416	28094464	17,4355958	6.7239508	.003289474
305	93025	28372625	17.4642492	6.7313155	.003278689
306	93636	28652616	17.4928557	6,7386641	.003267974
307	94249	28934443	17.5214155	6.7459967	.003257329
308	94864	29218112	17.5499288	6.7533134	.003246753
309	95481	29503629	17.5783958	6.7606143	.003236246
310	96100	29791000	17.6068169	6.7678995	.003225806

<u> </u>					
No.	Squares.	Cubes.	Square Roots.	Cube Roots.	Reciprocals.
	0.000	00000004	48 0054004	0 8000 4000	000017101
311	96721	30080231	17.6351921	6.7751690	.003215434
312	97344	30371328	17.6635217	6.7824229	.003205128
313	97969	30664297	17.6918060	6.7896613	.003194888
314	98596	30959144	17.7200451	6.7968844	.003184713
315	99225	31255875	17 7482393	6.8040921	.003174603
316	99856	31554496	17.7763888	6.8112847	.003164557
317	100489	31855013	17.8044938	6.8184620	.003154574
318	101124	32157432	17.8325545	6.8256242	.003144654
319	101761	32461759	17.8605711	6.8327714	.003134796
320	102400	32768000	17.8885438	6.8399037	.003125000
321	103041	33076161	17.9164729	6.8470213	.003115265
322			17.9443584	6.8541240	.003105590
323	103684	33386248		6.8612120	
	104329	33698267	17.9722008		.003095975
324	104976	34012224	18.0000000	6.8682855	.003086420
325	105625	34328125	18.0277564	6.8753443	.003076923
326	106276	34645976	18.0554701	6.8823888	.003067485
327	106929	34965783	18.0831413	6.8894188	.003058104
328	107584	35287552	18.1107703	6.8964345	.003048780
329	108241	35611289	18.1383571	6.9034359	.003039514
330	108900	35937000	18.1659021	6.9104232	.003030303
331	109561	36264691	18.1934054	6.9173964	.003021148
332	110224	36594368	18.2208672	6.9243556	.003012048
333	110889	36926037	18.2482876	6.9313008	.003003003
334	111556	37259704	18.2756669	6.9382321	.002994012
335	112225	37595375	18.3030052	6.9451496	.002985075
336	112896	37933056	18.3303028	6.9520533	.002976190
337	113569	38272753	18.3575598	6.9589434	.002967359
338	114244	38614472	18,3847763	6.9658198	.002958580
339	114921	38958219	18.4119526	6.9726826	.002949853
340	115600	39304000	18.4390889	6.9795321	.002941176
	116281	39651821	18.4661853	6.9863681	.002932551
341					
342	116964	40001688	18.4932420	6.9931906	.002923977
343	117649	40353607	18.5202592	7.0000000	.002915452
344	118336	40707584	18.5472370	7.0067962	.002906977
345	119025	41063625	18.5741756	7 0135791	.002898551
346	119716	41421736	18.6010752	7.0203490	.002890173
347	120409	41781923	18.6279360	7.0271058	.002881844
348	121104	42144192	18.6547581	7.0338497	.002873563
349	121801	42508549	18.6815417	7.0405806	.002865330
350	122500	42875000	18.7082869	7.0472987	.002857143
351	123201	43243551	18.7349940	7.0540041	.002849003
352	123904	43614208	18.7616630	7.0606967	.002840909
353	124609	43986977	18.7882942	7.0673767	.002832861
354	125316	44361864	18.8148877	7.0740440	.002824859
355	126025	41738875	18.8414437	7.0806988	.002816901
356	126736	45118016	18.8679623	7.0873411	.002808989
357	127449	45499293	18.8944436	7.0939709	.002801120
358	128164	45882712	18.9208879	7.1005885	.002793296
359	128881	46268279	18.9472953	7.1071937	.002785515
- ISSEE MANNEY	The state of the s				
360	129600	46656000	18.9736660	7.1137866	.002777778
361	130321	47045881	19.0000000	7.1203674	.002770083
362	131044	47437928	19.0262976	7.1269360	.002762431
363	131769	47832147	19.0525589	7.1334925	.002754821
364	132496	48228544	19.0787840	7.1400370	.002747253
365	133225	48627125	19.1049732	7.1465695	.002739726
366	133956	49027896	19.1311265	7.1530901	.002732240
367	134689	49430863	19.1572441	7.1595988	.002724796
368	135424	49836032	19.1833261	7.1660957	.002717391
369	136161	50243409	19.2093727	7.1725809	.002710027
370	136900	50653000	19.2353841	7.1790544	.002702703
371	137641	51064811	19.2613603	7.1855162	.002695418
872	138384	51478848	19.2873015	7.1919663	.002688172
012	1 . 100002	01710010	1 40.0010010	1 .1010000	, ,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,

No.	Squares.	Cubes.	Square Roots.	Cube Roots.	Reciprocals.
373	139129	F100=117	19.3132079	7.1984050	.002680965
		51895117 52313624	19.3390796	7.2048322	.002673797
374	139876	52734375	19.3649167	7.2112479	.002675797
375	140625	53157376	19.3907194		.002659574
376	141376 142129	53582633	19.4164878	7.2176522 7.2240450	.002652520
377 378	142884	54010152	19.4422221	7.2304268	.002645503
379	143641	54439939	19.4679223	7.2367972	.002638522
					DESCRIPTION OF THE PARTY OF THE
380	144400	54872000 55306341	19.4935887 19.5192213	7.2431565 7.2495045	.002631579
381 382	145161		19.5448203	7.2558415	.002617801
	145924	55742968 56181887	19.5703858	7.2621675	.002610966
383 384	146689 147456	56623104	19.5959179	7.2684824	.002604167
385	148225	57066625	19.6214169	7.2747864	.002597403
386	148996	57512456	19.6468827	7.2810794	.002590674
387	149769	57960603	19.6723156	7.2873617	.002583979
388	150544	58411072	19.6977156	7.2936330	.002577320
389	151321	58863869	19.7230829	7.2998936	.002570694
390	152100	59319000	19.7484177	7.3061436	.002564103
391	152881	59776471	19.7737199	7.3123828	.002504105
392	153664	60236288	19.7989899	7.3186114	.002551020
393	154449	60698457	19.8242276	7.3248295	.002544529
394	155236	61162984	19.8494332	7.3310369	.002538071
395	156025	61629875	19.8746069	7,3372339	.002531646
396	156816	62099136	19.8997487	7.3434205	.002525253
397	157609	62570773	19.9248588	7.3495966	.002518892
398	158404	63044792	19.9499373	7.3557624	.002512563
399	159201	63521199	19.9749844	7.3619178	.002506266
400	160000	64000000	20,0000000	7.3680630	.002500000
401	160801	64481201	20.0249844	7.3741979	.002493766
402	161604	64964808	20.0499377	7.3803227	.002487562
403	162409	65450827	20.0748599	7.3864373	.002481390
404	163216	65939264	20.0997512	7.3925418	.002475248
405	164025	66430125	20.1246118	7.3986363	.002469136
406	164836	66923416	20,1494417	7.4047206	.002463054
407	165649	67419143	20.1742410	7.4107950	.002457002
408	166464	67917312	20.1990099	7.4168595	.002450980
409	167281	68417929	20.2237484	7.4229142	.002444988
410	168100	68921000	20.2484567	7.4289589	.002439024
411	168921	69426531	20.2731349	7.4349938	.002433090
412	169744	69934528	20.2977831	7.4410189	.002427184
413	170569	70444997	20.3224014	7.4470342	.002421308
414	171396	70957944	20.3469899	7,4530399	.002415459
415	172225	71473375	20.3715488	7.4590359	.002409639
416	173056	71991296	20.3960781	7.4650223	.002403846
417	173889	72511713	20.4205779	7.4709991	.002398082
418	174724	73034632	20.4450483	7.4769664	.002392344
419	175561	73560059	20.4694895	7.4829242	.002386635
420	176400	74088000	20.4939015	7.4888724	.002380952
421	177241	74618461	20.5182845	7.4948113	.002375297
422	178084	75151448	20.5426386	7.5007406	.002369668
423	178929	75686967	20.5669638	7.5066607	.002364066
424	179776	76225024	20 5912603	7.5125715	.002358491
425	180625	76765625	20.6155281	7.5184730	.002352941
426	181476	77308776	20.6397674	7.5243652	.002347418
427 428	182329	77854483	20.6639783	7.5302482	,002341920
428	183184 184041	78402752 78953589	20.6881609 20.7123152	7.5361221 7.5419867	.002336449
THE PERSON NAMED IN			A STATE OF THE PARTY OF THE PAR	100000000000000000000000000000000000000	NAME OF TAXABLE PARTY.
430 431	184900	79507000	20.7364414	7.5478423	.002325581
431	185761 186624	80062991 80621568	20.7605395 20.7846097	7.5536888	.002320186
433	187489	81182737	20.7846097	7.5595263 7.5653548	.002314815
434	188356	81746504	20.8326667	7.5055548	.002309469
70%	1 100000	01110004	20.0020001	1.5111145	1 .002004147

No.	Squares.	Cubes.	Square Roots.	Cube Roots.	Reciprocals.
435	189225	82312875	20.8566536	7.5769849	.002298851
436	190096	82881856	20.8806130	7.5827865	.002293578
437	190969	83453453	20.9045450	7.5885793	.002258330
438	191844	84027672	20.9284495	7.5943633	.002283105
439	192721	84604519	20.9523268	7.6001385	.002277904
440	193600	85184000	20.9761770	7.6059049	.002272727
441	194481	85766121	21.0000000	7.6116626	.002267574
442	195364	86350888	21.0237960	7.6174116	.002262443
443	196249	86938307	21.0475652	7.6231519	.002257336
411	197136	87528384 88121125	21.0713075 21.0950231	7.6288837	.002252252
445 446	198025 198916	88716536	21.1187121	7.6346067 7.6403213	.002247191
447	199809	89314623	21.1423745	7.6460272	.002242152 .002237136
448	200704	89915392	21.1660105	7.6517247	.002232143
419	201601	90518849	21.1896201	7.6574133	.002227171
450	202500	91125000	21.2132034	7.6630943	.002222222
451	202300	91733851	21.2367606	7.6687665	.002217295
452	204304	92345408	21.2602916	7.6744303	.002212389
453	205209	92959677	21.2837967	7.6800857	.002207506
454	206116	93576664	21.3072758	7.6857328	.002202643
455	207025	94196375	21.3307290	7.6913717	.002197802
456	207936	94818816	21.3541565	7.6970023	.002192982
457	208849	95443993	21.3775583	7.7026246	.002188184
458	209764	96071912	21.4009346	7.7082388	.002183406
459	210681	96702579	21.4242853	7.7138448	.002178649
460	211600	97336000	21.4476106	7.7194426	.002173913
461	212521	97972181	21.4709106	7.7250325	.002169197
462	213444	98611128	21.4941853	7.7306141	.002164502
463	214369	99252847	21.5174348	7.7361877	.002159827
464	215296	99897344	21.5406592	7.7417532	.002155172
465	216225	100544625	21.5638587	7.7473109	.002150538
466	217156 218089	101194696 101847563	21.5870331 21.6101828	7.7528606 7.7584023	.002145923
467	219024	102503232	21.6333077	7.7639361	.002136752
469	219961	103161709	21.6564078	7.7694620	.002132196
			STAPSHOE BEGINNING	THE RESERVE OF THE PARTY OF THE	
470	220900	103823000	21.6794834	7.7749801	.002127660
471	221841 222784	104487111 105154048	21.7025344 21.7255610	7.7804904 7.7859928	.002123142 .002118644
473	223729	105823817	21.7485632	7.7914875	.002114165
474	224676	106496424	21.7715411	7.7969745	.002109705
475	225625	107171875	21.7944947	7.8024538	.002105263
476	226576	107850176	21.8174242	7.8079254	.002100840
477	227529	108531333	21.8403297	7.8133892	.002096436
478	228484	109215352	21 8632111	7.8188456	.002092050
479	229441	109902239	21.8860686	7.8242942	.002087683
480	230400	110592000	21.9089023	7.8297353	.002088333
481	231361	111284641	21.9317122	7.8351688	.002079002
482	232324	111980168	21.9544984	7.8405949	.002074689
483	233289	112678587	21.9772610	7.8460134	.002070393
484	234256	113379904	22.0000000	7.8514244	.002066116
485	235225	114084125	22.0227155	7.8568281	.002061856
486 487	236196 237169	114791256 115501303	22.0454077 22.0680765	7.8622242 7.8676130	.002057613
488	238144	116214272	22.0907220	7.8729944	.002049180
489	239121	116930169	22.1133444	7.8783684	.002044990
E PAR		STATE OF THE PARTY		7.8837352	
490 491	240100 241081	117649000 118370771	22.1359436 22.1585198	7.8890946	.002040816
491	241081	119095488	22.1810730	7.8944468	.002032520
493	243049	119823157	22.2036033	7.8997917	.002028398
494	244036	120553784	22.2261108	7.9051294	.002024291
495	245025	121287375	22.2485955	7.9104599	.002020202
496	246016	122023936	22.2710575	7.9157832	.002016129

No.	Squares.	Cubes.	Square Roots.	Cube Roots.	Reciprocals
497	247009	122763473	22,2934968	7.9210994	.002012072
498	248004	123505992	22.3159136	7.9264085	.002008032
499	249001	124251499	22.3383079	7.9317104	.002004008
500	250000	125000000	22.3606798	7.9370053	.002000000
501 502	251001 252.04	125751501 126506008	22,3830293 22,4053565	7.9422931 7.9475739	.001990008
503	253009	127263527	22.4276615	7.9528477	.001988072
504	254016	128024064	22.4499443	7.9581144	.001984127
505 506	255025 256036	128787625 129554216	22.4722051 22.4944438	7.9633743 7.9686271	.001980198
507	257049	130323843	22.5166605	7.9738731	.001972387
508	258064	131096512	22.5388553	7.9791122	.001968504
509	259081	131872229	22.5610283	7.9843144	.001964637
510	260100	132651000	22.5831796	7.9895697	.001960784
511 512	261121 262144	133432831 134217728	22.6053091 22.6274170	7.9947883 8.0000000	.001950947
513	263169	135005697	22.6495033	8.0052049	.001949318
514	264196	135796744	22.6715681	8.0104032	.001945525
515 516	265225 266256	136590875 137388096	22.6936114 22.7156334	8.0155946 8.0207794	.001941748
517	267289	138188413	22.7376340	8.0259574	.001934236
518	268324	138991832	22.7596134	8.0311287	.001930502
519	269361	139798359	22.7815715	8.0362935	.001926782
520	270400	140608000	22,8035085	8.0414515	.001923077
521 522	271441 272484	141420761 142236648	22.8254244 22.8473193	8.0466030 8.0517479	.001919386
523	273529	143055667	22.8691933	8.0568862	.001912046
524	274576	143877824	22.8910463	8.0620180	.001908397
525 526	275625 276676	144703125 145531576	22.9128785 22.9346899	8.0671432	.001904762
527	277729	146363183	22.9564806	8.0722620 8.0773743	.001897533
528	278784	147197952	22.9782506	8.0824800	.001893939
529	279841	148035889	23.0000000	8.0875794	.001890359
530	280900	148877000	23.0217289	8.0926723	.001886792
531 532	281961 283024	149721291 150568768	23.0434372 23.0651252	8.0977589 8.1028390	.001883239
533	284089	151419437	23.0867928	8.1079128	.001876173
534	285156	152273304	23.1084400	8.1129803	.001872659
535 536	286225 287296	153130375 153990656	23.1300670 23.1516738	8.1180414 8.1230962	.001869159
537	288369	154854153	23.1732605	8.1281447	.001862197
538	289444	155720872	23.1948270	8.1331870	.001858736
539	290521	156590819	23.2163735	8.1382230	.001855288
540 541	291600 292681	157464000 158340421	23.2379001 23.2594067	8.1432529 8.1482765	.001851852
542	293764	159220088	23.2808935	8.1532939	.001845018
543	294849	160103007	23.3023604	8.1583051	.001841621
544 545	295936 297025	160989184 161878625	23.3238076 23.3452351	8.1633102 8.1683092	.001838235
546	298116	162771336	23.3666429	8.1733020	.001831502
547	299209	163667323	23.3880311	8.1782888	.001828154
548 549	300304 301401	164566592 165469149	23.4093998 23.4307490	8.1832695 8.1882441	.001824818
550	302500	166375000	23.4520788	8.1932127	.001831494
551	303601	167284151	23.4733892	8.1981753	.001814882
552	304704	168196608	23.4946802	8.2031319	.001811594
553	305809 306916	169112377 170031464	23.5159520 23.5372046	8.2080825 8.2130271	.001808318
555	308025	170953875	23.5584380	8.2179657	.001801802
556	309136	171879616	23.5796522	8.2228985	.001798561
557 558	310249 311364	172808693 173741112	23.6008474 23.6220236	8.2278254 8.2327463	.001795332

No.	Squares.	Cubes.	Square Roots.	Cube Roots.	Reciprocals.
559	312481	174676879	23.6431808	8.2376614	.001788909
560 561 562 563 564 565 566 567 568 569	313600 314721 315844 316969 318096 319225 320356 321489 322624 323761	175616000 176558481 177504328 178453547 179406144 180362125 181321496 182284263 183250432 184220000	23.6643191 23.6854386 23.7065392 23.7276210 23.7486842 23.7697286 23.7907545 23.8117618 25.8527506 25.8537209	8.2425706 8.2474740 8.2528715 8.2572633 8.2621492 8.2670294 8.2719039 8.2767726 8.2816355 8.2864928	.001785714 .001788531 .001779359 .001776199 .001769912 .001766784 .00176668 .001760563
570 571 572 573 574 575 576 577 578 579	324900 326041 327184 328329 329476 330625 331776 332929 334084 335241	185193000 186169411 187149248 188132517 189119224 190109375 191102976 192100083 193100552 194104539	23.8746728 23.8956063 23.9165215 23.9374184 23.5582971 23.9791576 24.000000 24.0208243 24.0416306 24.0624188	8.2918444 8.2961903 8.3010304 8.3058651 8.3106941 8.3155175 8.2203353 8.2251475 8.3299542 8.3347553	.001754386 .001751313 .001748252 .001745201 .001742160 .001739130 .001738111 .001733102 .001730104 .001727116
580 581 582 583 584 585 586 586 587 588 589	336400 337561 338724 339889 341056 342225 343396 344569 345744 346921	195112000 196122941 197137368 198155287 199176704 200201625 201230056 202262003 203297472 204336469	24.0831891 24.1039416 24.1246762 24.1453929 24.1660919 24.1867732 24.2074369 24.228829 24.2487113 24.2693222	8.3395509 8.3448410 8.3491256 8.5539047 8.5586784 8.5684466 8.3682095 8.5729668 8.3777188 8.3824653	.001724138 .001721170 .001718213 .001715266 .001715289 .001709402 .001706485 .001706578 .00170680
590 591 592 593 594 595 596 597 598 599	348100 349281 350464 351649 352836 354025 355216 356409 357604 35801	205379000 206425071 207474688 208527857 209584584 210644875 211708736 212776173 213847192 214921799	24.2899156 24.3104916 24.3310501 24.3515913 24.3721152 24.3926218 24.4131112 24.435834 24.4540285 24.4744765	8.2872065 8.3919423 8.5966729 8.4013981 8.4061180 8.4108326 8.4155419 8.4202460 8.424448 8.4296383	.001694915 .001692047 .001689189 .001686341 .001686592 .001680672 .001677852 .001672941 .001669449
600 601 602 603 604 605 606 607 608 609	360000 361201 362404 363609 364816 366025 367236 368449 369664 370881	216000000 217081801 218167208 219256227 220348864 221445125 222545016 223648543 224755712 225866529	24. 4948974 24. 5153013 24. 5356883 24. 5764115 24. 5967478 24. 6170673 24. 637300 24. 6576560 24. 6779254	8.4848267 8.4390098 8.4436877 8.4483605 8.4530281 8.4576906 8.4623479 8.4670001 8.4716471 8.4762893	.001666667 .001663894 .001661130 .001658875 .001658875 .001652893 .001650165 .001647446 .001644737 .001642036
610 611 612 613 614 615 616 617 618 619	372100 373321 374544 375769 376996 378225 379456 380689 381924 383161 3834400	226981000 228099131 229220923 230346397 231475544 232608375 253744896 234885113 236020032 237176659 238828000	24.6961781 24.7184142 24.7386338 24.7586338 24.7790234 24.7991935 24.8193473 24.8596058 24.8797106 24.8997992	8,4809261 8,4855579 8,4901848 8,4948065 8,4994233 8,5040350 8,5086417 8,5132435 8,5178403 8,5224321 8,5270189	.001639344 .001636681 .001633987 .001631321 .001628064 .001623377 .001624746 .001618123 .001615509 .001612903

No.	Squares.	Cubes.	Square Roots.	Cube Roots.	Reciprocals.
004	385641	239483061	24.9198716	8.5316009	.001610306
621 622	386884	240641848	24,9399278	8.5361780	.001607717
623	388129	241804367	24.9599679	8.5407501	.001605136
624	389376	242970624	24.9799920	8.5453173	.001602564
625	390625	244140625	25.0000000	8.5498797	.001600000
626	391876	245314376	25.0199920	8,5544372	.001597444
627	393129	246491883	25.0399681	8.5589899	.001594896
628	394384	247673152	25.0599282	8.5635377	.001592357
629	395641	248858189	25.0798724	8.5680807	.001589825
630	396900	250047000	25,0998008	8.5726189	.001587302
631	398161	251239591	25.1197134	8.5771523	.001584786
632	399424	252435968	25.1396102	8.5816809	.001582278
633	400689	253636137	25.1594913	8.5862047	.001579779
634	401956	254840104	25.1793566	8.5907238	.001577287
635	403225	256047875	25.1992063	8.5952380	.001574803
636	404496	257259456	25.2190404	8.5997476	.001572327
637	405769	258474853 259694072	25.2388589 25.2586619	8.6042525 8.6087526	.001569859
638 639	407044 408321	260917119	25.2784493	8.6132480	.001567398
	Contract of the last		ALL CONTRACTOR OF THE PARTY OF	11010074900073	CONTRACTOR DESCRIPTION
640	409600	262144000	25.2982213	8.6177388	.001562500
641	410881	263374721	25.3179778	8.6222248	.001560062
642	412164	264609288	25.3377189	8.6267063	.001557632
643	413449	265847707 267089984	25.3574447 25.3771551	8.6311830	.001555210
644 645	414736 416025	268336125	25.3968502	8.6356551 8.6401226	.001552795 .001550388
646	417316	269586136	25.4165301	8.6445855	.001547988
647	418609	270840023	25,4361947	8.6490437	.001545595
648	419904	272097792	25.4558441	8.6534974	.001543210
649	421201	273359449	25.4754784	8.6579465	.001540832
650	422500	274625000	25,4950976	8.6623911	.001538462
651	423801	275894451	25.5147016	8.6668310	.001536098
652	425104	277167808	25.5342907	8.6712665	.001533742
653	426409	278445077	25,5538647	8.6756974	.001531394
654	427716	279726264	25.5734237	8.6801237	.001529052
655	429025	281011375	25.5929678	8.6845456	.001526718
656	430336	282800416	25.6124969	8.6889630	.001524390
657	431649	283593393	25.6320112	8.6933759	.001522070
658	432964	284890312	25.6515107	8.6977843	.001519757
659	434281	286191179	25.6709953	8.7021882	.001517451
660	435600	287496000	25.6904652	8.7065877	.001515152
661	436921	288804781	25.7099203	8.7109827	.001512859
662	438244	290117528	25.7293607	8.7153734	.001510574
663	439569	291434247	25.7487864	8.7197596	.001508296
664 665	440896 442225	292754944 294079625	25.7681975	8.7241414	.001506024
666	443556	295408296	25.7875939 25.8069758	8.7285187 8.7328918	.001503759
667	444889	296740963	25.8263431	8.7372604	.001501502
668	446224	298077632	25.8456960	8.7416246	.001497006
669	447561	299418309	25,8650343	8.7459846	.001494768
670	448900	300763000	25.8843582	-2000 49 38 88 72 - 23 12	A CHARLES TO STATE OF THE PARTY
671	450241	302111711	25.9036677	8.7503401 8.7546913	.001492537
672	451584	303464448	25.9229628	8.7590383	.001490313
673	452929	304821217	25.9422435	8.7633809	.001485884
674	454276	306182024	25.9615100	8.7677192	.001483680
675	455625	307546875	25.9807621	8.7720532	.001481481
676	456976	308915776	26.0000000	8.7763830	.001479290
677	458329	310288733	26.0192237	8.7807084	.001477105
678	459684	311665752	26.0384331	8.7850296	.001474926
679	461041	313046839	26.0576284	8.7893466	.001172754
680	462400	314432000	26.0768096	8.7936593	,001470588
681	463761	315821241	26.0959767	8.7979679	.001468429
682	465124	317214568	26.1151297	8.8022721	.001466276

No.	Squares.	Cubes.	Square Roots.	Cube Roots.	Reciprocals.
683 684 685 686 687 688 689	466489 467856 469225 470596 471969 473344 474721	318611987 320013504 321419125 322828856 324242703 325660672 327082769	26,1342687 26,1533937 26,1725047 26,1916047 26,2106848 26,2297541 26,2488095	8.8065722 8.8108681 8.8151598 8.8194474 8.8237307 8.8280099 8.8322850	.001464129 .001461988 .001459854 .001457726 .001455604 .001453488 .001451379
690 691 692 693 694 695 696 697 698	476100 477481 478864 480249 481636 483025 484416 485809 487204	328509000 329930371 331373888 332812557 334255384 335702375 337153536 338608873 340068392	26.2678511 26.2868789 26.3058929 26.3248932 26.3438797 26.3628527 26.3818119 26.4007576 26.4196896	8.8365559 8.8408227 8.8450854 8.8450854 8.8493440 8.8535985 8.8578489 8.8620952 8.8663375 8.8705757	.001449275 .001447178 .001445087 .001443001 .001449022 .001438849 .001436782 .001434720 .001432665
699 700 701 702 703 704 705 706 707 708	488601 490000 491401 492804 494209 495616 497025 498436 499849 501264	341532099 343000000 344472101 345948408 347428927 348913664 350402625 351895816 353393243 354894912	26.4386081 26.4575131 26.4764046 26.4952826 26.5141472 26.5329983 26.5518361 26.5706605 26.6882694	8.8748099 8.8790400 8.8832661 8.8874882 8.8917063 8.8959204 8.9043366 8.9043366 8.9083387 8.9127369	,001430615 .001428571 .001426534 .001424501 .001422475 .001420455 .001418440 .001416431 .001414427 .001413429
709 710 711 712 713 724 715 716 717 718 719	502681 504100 505521 506944 508369 509796 511225 512656 514089 515524 516961	356400829 357911000 359425431 360944128 362467097 363994344 365525875 367061696 368601813 370146232 371694959	26 6270539 26 6458252 26 6645833 26 6833281 26 7020598 26 7207784 26 7394830 26 7768557 26 77955220 26 8141754	8,9169311 8,9211214 8,9259078 8,9294902 8,9336687 8,9378433 8,9420140 8,9401609 8,9503438 8,9545029 8,9586581	.001410437 .001408451 .001406470 .001404494 .001402525 .001400560 .001398601 .001394700 .001394700 .001392758 .001390821
720 721 722 723 724 725 726 727 728 729	518400 519841 521284 522729 524176 525625 527076 528529 529984 531441	373249000 374805361 376807048 377933067 379503424 381078125 382657176 384240583 385828352 387420489	26. 8328157 26. 8514432 26. 8700577 26. 8886593 26. 9072481 26. 9258240 26. 9443872 26. 9629375 26. 9814751 27. 0000000	8.9628095 8.9669570 8.9711007 8.9752406 8.9793766 8.9835089 8.9876373 8.9917620 8.9958829 9.0000000	001388889 001386963 001385042 001383126 001381215 001377310 001377310 0013775516 001373626 001371742
730 731 732 733 734 735 736 737 738	532900 534361 535824 537289 538756 540225 541696 543169 544644 546121	389017000 390617891 392223168 398832837 395446904 397065375 398688256 400315553 401947272 403583419	27.0185122 27.0370117 27.0554985 27.0739727 27.0924344 27.1108834 27.1293199 27.1477439 27.1661554 27.1845544	9.0041134 9.0082229 9.0123288 9.0164309 9.0205293 9.0246230 9.0287149 9.0328021 9.0368857 9.0409655	.001369863 .001367989 .001366120 .001364256 .001362398 .001360544 .001358696 .001355014 .001353180
740 741 742 743 744	547600 549081 550564 552049 553536	405224000 406869021 408518488 410172407 411830784	27,2029410 27,2213152 27,2396769 27,2580263 27,2763634	9.0450419 9.0491142 9.0531831 9.0572482 9.0613098	.001351351 .001349528 .001347709 .001345895 .001344086

No.	Squares.	Cubes.	Square Roots.	Cube Roots.	Reciprocals.
			ON 00 10001		
745	555025	413493625	27.2946881	9.0653677	.001342282
746	556516	415160936	27.3130006	9.0694220	.001340483
747	558009	416832723	27.3313007 27.3495887	9.0734726 9.0775197	.001338688
748	559504 561001	418508992 420189749	27.3678644	9.0815631	.001336898
749	The second second			DECEMBER OF THE PARTY OF	
750	562500	421875000	27.3861279	9.0856030	.001333333
751	564001	423564751	27.4043792	9.0896392	.001331558
752	565504	425259008	27.4226184	9.0936719	.001329787
753	567009	426957777	27.4408455	9.0977010	.001328021
754	568516	428661064	27.4590604	9.1017265	001326260
755	570025	430368875	27.4772633	9.1057485	.001324503
756	571536 573049	432081216 433798093	27.4954542 27.5136330	9.1097669 9.1137818	.001322751
757	574564	435519512	27.5317998	9.1177931	.001321004
758	576081	437245479	27.5499546	9.1218010	.001317523
759	ERC	Market Street		The same of the sa	
760	577600	438976000	27.5680975	9.1258053	.001315789
761	579121	440711081	27.5862284	9.1298061	.001314060
762	580644	442450728	27.6043475	9.1338034	.001312336
763	582169	444194947	27.62:4546	9.1377971	.001310616
764	583696	445943744	27.6405499	9.1417874	.001308901
765	585225	447697125	27.6586334 27.6767050	9.1457742	.001307190
766	586756 588289	449455096 451217663	27.6947648	9.1497576 9.1587375	.001305483
767 768	589824	452984832	27.7128129	9.1577139	.001302083
769	591361	454756609	27.7308492	9.1616869	.001300390
	WATER STREET	THE RESERVE OF THE PARTY OF THE		Contract Contract	No.
770	592900	456533000	27.7488739	9.1656565	.001298701
771	594441	458314011	27,7668868	9.1696225	.001297017
772	595984	460099648	%1.104000U	9.1735852	.001295337
773	597529	461889917 463684824	27.8028775	9.1775445	.001293661
774	599076	465484375	27.8208555 27.8388218	9.1815003 9.1854527	.001291990
775 776	600625 602176	467288576	27.8567766	9.1894018	.001288660
777	603729	469097433	27.8747197	9.1933474	.001287001
778	605284	470910952	27.8926514	9.1972897	.001285347
779	606841	472729139	27.9105715	9.2012286	,001283697
A 4 (40000000000000000000000000000000000	NAME OF TAXABLE	474552000			
780	608400 609961	476379541	27.9284801 27.9463772	9.2051641 9.2090962	.001282051
781 782	611524	478211768	27.9642629	9.2130250	.001230410
783	613089	480048687	27.9821372	9.2169505	.001277139
784	614656	481890304	28.0000000	9.2208726	.0012775510
785	616225	483736625	28.0178515	9.2247914	.001273885
786	617796	485587656	28.0356915	9.2287068	.001272265
787	619369	487443403	28.0535203	9.2326189	.001270648
788	620944	489303872	28.0713377	9.2365277	.001269036
789	622521	491169069	28.0891438	9.2404333	.001267427
790	624100	493039000	28.1069386	9.2443355	.001265823
791	625681	494913671	28.1247222	9.2482344	.001263623
792	627264	496793088	28.1424946	9.2521300	.001262626
793	628849	498677257	28.1602557	9.2560224	.001261034
794	630436	500566184	28.1780056	9.2599114	.001259446
795	632025	502459875	28.1957444	9.2637973	,001257862
796	633616	504358336	28.2134720	9.2676798	.001256281
797	635209	506261573	28.2311884	9.2715592	.001254705
798	636804	508169592	28.2488938	9.2754352	.001253133
799	638401	510082399	28.2665881	9.2793081	.001251564
800	640000	512000000	28.2842712	9.2831777	.001250000
801	641601	513922401	28.3019434	9.2870440	.001248439
802	643204	515849608	28.3196045	9.2909072	.001246883
803	644809	517781627	28.3372546	9.2947671	.001245330
804	646416	519718464	28.3548938	9.2986239	.001243781
805	648025	521660125	28.3725219	9.3024775	.001242236
806	649636	523606616	28.3901391	9.3063278	.001240695

No.	Squares.	Cubes.	Square Roots.	Cube Roots.	Reciprocal
807	651249	525557943	28,4077454	9.3101750	.001239157
808	652864	527514112	28.4253408	9.3140190	.001237624
809	654481	529475129	28.4429253	9.3178599	.001236094
810	656100	531441000	28.4604989	9.3216975	.001234568
811	657721	533411731	28.4780617	9.3255320	.001233046
812	659344	535387328	28.4956137	9.3293634	.001231523
813 814	660969	537367797 539853144	28.5131549 28.5306852	9.3331916	.001230013
815	662596 664225	541343375	28.5482048	9.3370167 9.3408386	.00122850
816	665856	543338496	28.5657137	9.3446575	.00122549
817	667489	545338513	28.5832119	9:3484731	.00122399
818	669124	547343432	28.6006993	7.3522857	.00122249
819	670761	549353259	28.6181760	9.3560952	.00122100
820	672400	551368000	28.6356421	9.3599016	.00121951
821	674041	553387661	28.6530976	9.3637049	.00121802
822	675684	555412248	28.6705424	9.3675051	.00121654
823	677329	557441767	28.6879766 28.7054002	9.3713022 9.3750963	.00121506
824 825	678976 680625	559476224 561515625	28.7228132	9.3788873	.00121339
826	682276	563559976	28.7402157	9.3826752	.00121065
827	683929	565609283	28.7576077	9.3864600	.00120919
828	685584	567663552	28.7749891	9.3902419	.00120772
829	687241	569722789	28.7923601	9.3940206	.00120627
830	688900	571787000	28.8097206	9.3977964	.00120481
831	690561	573856191	28.8270706	9.4015691	.00120336
832	692224	575930368	28.8444102	9.4053387	.00120192
833	693889	578009537	28.8617394	9.4091054	.00120048
834 835	695556	580093704	28.8790582 28.8963666	9.4128690 9.4166297	.00119904
836	697225 698896	582182875 584277056	28.9136646	9.4203873	.00119700
837	700569	586376253	28.9309523	9.4241420	.00119474
838	702244	588480472	28.9482297	9.4278936	.00119331
839	703921	590589719	28.9654967	9.4316423	.00119189
840	705600	592704000	28.9827535	9.4353880	.00119047
841	707281	594823321	29.0000000	9.4391307	.00118906
842	708964	596947688	29.0172363	9.4428704	.00118764
843	710649	599077107	29.0344623	9.4466072	.00118624
844 845	712336 714025	601211584 603351125	29.0516781 29.0688837	9.4503410 9.4540719	.00118483
846	715716	605495736	29.0860791	9.4577999	.00118203
847	717409	607645423	29.1032644	9.4615249	.00118063
848	719104	609800192	29.1204396	9.4652470	.00117924
849	720801	611960049	29.1376046	9.4689661	.00117785
850	722500	614125000	29.1547595	9.4726824	.00117647
851	724201	616295051	29.1719043	9.4763957	.00117508
852	725904	618470208	29.1890390	9.4801061	.00117370
853	727609	620650477	29.2061637	9.4838136	.00117233
854	729316 731025	622835864 625026375	29.2232784 29.2403830	9.4875182	.001170960
855 856	732736	627222016	29.2574777	9.4912200 9.4949188	.00116822
857	734149	629422793	29.2745623	9.4986147	.00116686
858	736164	631628712	29.2916370	9.5023078	.001165501
859	737881	633839719	29.3087018	9.5059980	.00116414
860	739600	636056000	29.3257566	9.5096854	.001162791
861	741321	638277381	29.3428015	9.5133699	.001161440
862	743044	640503928	29.3598365	9.5170515	.001160098
863	744769	642735647	29.3768616	9.5207303	.001158749
864 865	746496 748225	644972544	29.3938769 29.4108823	9.5244063 9.5280794	.001157407
866	748225	647214625 649461896	29.4278779	9.5317497	.001154734
867	751689	651714363	29.4418637	9.5354172	.001153403
868	753424	653972032	29,4618397	9.5390818	.001152074

	2	0.1	Square	Cuba Doots	Desimposis
No.	Squares.	Cubes.	Roots.	Cube Roots.	Reciprocals.
869	755161	656234909	29.4788059	9,5427437	.001150748
4-398-01110	THE RESERVE TO STATE OF THE PARTY OF THE PAR		29.4957624	9.5464027	.001149425
870	756900 758641	658503000 660776311	29.4957024	9.5500589	.001148106
871 872	760384	663054848	29.5296461	9.5537123	.001146789
873	762129	665338617	29.5465734	9.5573630	.001145475
874	763876	667627624	29.5634910	9.5610108	.001144165
875	765625	669921875	29.5803989	9.5646559	.001142857
876	767376	672221376	29.5972972	9.5682982	.001141553
877	769129	674526133	29.6141858	9.5719377	.001140251
878	770884	676836152	29.6310648	9.5755745	.001138952
879	772641	679151439	29.6479342	9.5792085	.001137656
880	774400	681472000	29,6647939	9.5828397	.001136364
881	776161	683797841	29.6816442	9.5864682	.001135074
882	777924	686128968	29.6984848	9.5900939	.001133787
883	779689	688465387	29.7153159	9.5937169	.001132503
884	781456	690807104	29.7321375	9.5973373	.001131222
885	783225	693154125	29.7489496	9.6009548	.001129944
886	784996	695506456	29.7657521	9.6045696	.001128668
887	786769	697864103	29.7825452	9.6081817	.001127396
888	788544	700227072	29.7993289	9.6117911	.001126126
889	790321	702595369	29.8161030	9.6153977	.001124859
890	792100	704969000	29.8328678	9.6190017	.001123596
891	793881	707347971	29.8496231	9.6226030	.001122334
892	795664	709732288	29.8663690	9.6262016	.001121076
893	797449	712121957	29.8831056	9.6297975	.001119821
894	799236	714516984	29.8998328	9.6333907	.001118568
895	801025	716917375	29.9165506	9.6369812	.001117318
896	802816	719323136	29.9332591	9.6405690	.001116071
897	804609	721734273	29.9499583	9.6441542	.001114827
898 899	806404 808201	724150792 726572699	29.9666481 29.9833287	9.6477367 9.6513166	.001113586
100000000000000000000000000000000000000	PRINCIPLE STATE OF THE SECOND	THE RESERVE TO SERVE	THE RESERVE TO SERVE THE PARTY OF THE PARTY	HARRY THE	
900	810000	729000000	30.0000000	9.6548938	.001111111
901	811801	731432701	30.0166620	9.6584684	.001109878
902	813604	733870808	30.0333148	9.6620403	.001108647
903	815409	736314327	30.0499584	9.6656096	.001107420
904 905	817216 819025	738763264 741217625	30.0665928 30.0832179	9.6691762	.001106195
906	820836	743677416	30.0998339	9.6727403 9.6763017	.001104972
907	822649	746142643	30.1164407	9.6798604	.001103733
908	821464	748613312	30.1330383	9.6834166	.001101322
909	826281	751089429	30.1496269	9.6869701	.001100110
910	828100	753571000	30.1662063	47001012 D 1 10 FC +	THE RESERVE OF THE PARTY OF THE
910	829921	756058031	30.1827765	9.6905211 9.6940694	.001098901
912	831744	758550528	30.1993377	9.6976151	.001097095
913	833569	761048497	30.2158899	9.7011583	.001095290
914	835396	763551944	30.2324329	9.7046989	.001094092
915	837225	766060875	30.2489669	9.7082369	.001092896
916	839056	768575296	30.2654919	9.7117723	.001091703
917	840889	771095213	30.2820079	9.7153051	.001090513
918	842724	773620632	30.2985148	9.7188354	.001089325
919	844561	776151559	30.3150128	9.7223631	.001088139
920	846400	778688000	30.3315018	9.7258883	.001086957
921	848241	781229961	30.3479818	9.7294109	.001085776
922	850084	. 783777448	30.3644529	9.7329309	.001084599
923	851929	786330467	30.3809151	9.7364484	.001083423
924	853776	788889024	30.3973683	9.7399634	.001082251
925	855625	791453125	30.4138127	9.7434758	.001081081
926	857476	794022776	30.4302481	9.7469857	.001079914
927	859329	796597983	30.4466747	9.7504930	.001078749
928 929	861184 863041	799178752 801765089	30.4630924	9.7539979	.001077586
930	864900	804357000	30.4795013 30.4959014	9.7575002 9.7610001	.001076426
900	004900	003001000	410666.00	9.7010001	.001019209

No.	Squares.	Cubes.	Square Roots.	Cube Roots.	Reciprocals
931	866761	806954491	30.5122026	9.7644974	.001074114
932	868624	809557568	30.5286750	9.7679922	.001072961
933	870489	812166237	30.5450487	9.7714845	.001071811
934	872356	814780504	30.5614136	9.7749743	.001070664
935 936	874225	817400375	30.5777697	9.7784616	.001069519
937	876096 877969	820025856	30.5941171	9.7819466	.001068376
938	879844	822656953 825293672	30.6104557	9.7854288	.001067236
939	881721	827936019	30.6267857 30.6431069	9.7889087 9.7923861	.001066098
940	ALC: THE SECOND		THE RESERVE OF THE PERSON NAMED IN	THE PERSON NAMED IN COLUMN	
941	883600 885481	830584000 833237621	30.6594194	9.7958611	.001063830
942	887364	835896888	80.6757233 30.6920185	-9.7993536 9.8028036	,001062699
943	889219	838561807	30.7083051	9.8062711	.001061571
944	891136	841232384	80.7245830	9.8097362	.001059322
945	893025	813908625	30.7408523	9.8131989	.001058201
946	894916	846590536	80.7571130	9.8166591	.001057082
947	896809	849278123	80.7733651	9.8201169	.001055966
948 949	898704	851971392	30.7896086	9.8235723	.001054852
	900601	854670349	30.8058436	9.8270252	.001053741
950	902500	857375000	30.8220700	9.8304757	.001052632
951	904401	860085351	30.8382879	9.8839238	.001051525
952 953	906304 908209	862801408	30.8544972	9.8373695	.001050420
954	910116	865523177 868250664	30.8706981 30.8868904	9.8408127	.001049318
955	912025	870983875	30.9030743	9.8442536 9.8476920	.001048218
956	913936	873722816	30.9192497	9.8511280	.001047120
957	915849	876467493	30.9354166	9.8545617	.001044932
958	917764	879217912	30.9515751	9.8579929	.001048841
959	919681	881974079	30.9677251	9.8614218	.001042753
960	921600	884736000	30.9838668	9.8648483	.001041667
961	923521	887503681	31.0000000	9.8682724	.001040583
962	925444	890277128	31.0161248	9.8716941	.001089501
963 964	927369 929296	893056347	31.0822413	9.8751135	.001088422
965	931225	895841344 898632125	31.0483494 31.0644491	9.8785305 9.8819451	.001037344
966	933156	901428696	81.0805405	9.8853574	.001035263
967	935089	904231063	31.0966236	9.8887673	.001084126
968	937024	907039232	31.1126984	9.8921749	.001088058
969	938961	909853209	81.1287648	9.8955801	.001081992
970	940900	912673000	81.1448230	9.8989830	.001030928
971	942841	915498611	31.1608729	9.9023835	.001029866
972	944784	918330048	31,1769145	9.9057817	.001028807
973	946729	921167317	81.1929479	9.9091776	.001027749
974	948676	924010424	31.2089731	9.9125712	.001020694
975 976	950625 952576	926859375 929714176	31.2249900 31.2409987	9.9159624 9.9198513	.001025641
977	954529	932574833	81.2569992	9.9227879	.001023541
978	956484	985441852	31.2729915	9.9261222	.001022495
079	958441	988313789	31.2880757	9.9295042	.001021450
080	960400	941192000	31.3049517	9.9328839	.001020408
981	962361	944076141	81.3209195	9.9862613	.001019368
982	964324	946966168	31.3368792	9.9396363	.001018330
983	966289	949862087	81.8528008	9,9430092	.001017294
84	968256	952763904	81.3687743	9.9463797	.001016260
85	970225	955671625	81.8847097	9.9497479	.001015228
086 087	972196	958585256 961504803	31.4006369	9.9531138	.001014199
988	974169 976144	961504808	31.4165561 31.4324673	9.9564775 9.9598389	.001018171
189	978121	967361669	81.4483704	9.9631981	.001012140
990	- CO.	STATE OF THE PARTY	The state of the state of	Control of the Contro	
91	980100 982081	970299000 973242271	81.4642654 81.4801525	9.9665549 9.9699095	.001010101 .001009082
92	984064	976191488	81.4960815	9,9732619	.001008065

No.	Squares.	Cubes.	Square Roots,	Cube Roots.	Reciprocals.
993	989049	979149557	31.5119025	9.9766130	.001007049
994	55N/36	982107784	31.5277655	9.9799500	.00700060835
995	990025	985004875	31.5436306	9.9833055	.001005085
996	999016	988947996	31.5594677	9,9866488	.002004026
997	994009	9910009973	31.5753168	9.9899900	.001000M00
998	999994	90-10111002	31.5011380	9.9933259	10010000004
969	90(8)04	997002009	31.6069613	9.9995656	1001001001
1000	1000000	1000000000	31.022766	10.0000000	.000000000
1001	1003001	1003003001	31.6385840	10.0033322	.0009990010
1003	100/900/4	1006013008	31.6543836	10.0069622	_0009980040
1003	1005009	1009027027	31.6701752	10.0099899 10.0133155	.0009070090
1005	1010025	1015075125	31.7017349	10.0196359	.0006650249
1006	1013135	1018108216	31.7175(8)	10.0199601	.0009040858
1007	10(4)49	1021147343	31.7333533	10.0232791	.0000980487
1008	1019064	1024192512	31.7490157	10.0267858	.000000000035
1(9)0	1019091	1027243729	31.7647903	10.0299104	.0009999803
1010	1020100	103/911000	31.7804972	10.0932228	.0009000990
1011	1022121	1003364331	31.7962362	10.0865330	.0099891197
1012	1021114	1095433728	31.8119474	10.0308410	-00008S1423
1013	1005109	1089509197	31.8276999	10.0431400	.0000871068
1014	1028196	1045230244	31.84339966	10.0454506	.0000861983
1015	1030225	1045678375 1048773066	31.8590646 31.8747549	10.0497521	.00008582217
1017	1084289	1051871913	31.89)4374	10.0530514	.0000842500 .0000842500
1018	103/324	1054977802	31.9061123	10.0506435	.0006953183
1019	1008061	1058089859	31.9217794	10.06294964	_0009813543
1030	1040400	1061208000	31.9574388	10.0662271	.00006089922
1021	1042441	1064392361	31.9530906	10.0695156	.6009794319
1023	1044684	1067463648	31.9687347	10.0729(3)	.0009784736
1003	1046529	1070509167	31.9843712	10.0760863	.0009775171
1034	1048576	1073741824	32.(00)000	10.0790684	.0009765625
1025	1050625	1070830625	\$2.0156213 \$2.0812348	10.0835484	.0000756098.
1027	1054729	1083209383	32 0165407	10.090310	.0009746589
1008	1056784	1980303952	32 0924391	10.0924755	.0000727626
1029	1058841	10/9/547399	32,0780298	10.0957460	.0009718173
1090	1060900	1092727000	32.0996131	10.0990163	.0009708738
1081	1062361	1095012791	32,1091887	10.1023835	.0009699921
1032	1065024	1099104788	32.1247568	10.1055487	.00 9689622
1063	1067089	1102302937	32.1408173	10.1088117	.0009680542
1034	1069156	1105507304	32 1228204	10.113)(35	.0009671130
1005	1071225	1108717875	32 1714159	10.1153314	.000661836
1037	1073296	1111934656 1115157653	32 1869539 32 3034844	10.1185882	.0000652510
1038	1077444	1118386872	35 518/001	10.1250953	.00006333011
1039	1079521	1121622319	32 2335223	10.1283457	.0009624539
1040	1061600	1124864000	32.2490810	10.1315941	.0009615385
1041	1089681	1198111981	32.9545316	710.1348408	.00000000148
1043	1085764	1131399088	32.2800248	10.1380845	.0009596929
1043	1087849	1134696507	32.2055105	10.1413356	.0009587738
1044 1045	1089936	1137898184	32.3109888	10.1445667	.0009578544
1046	1094116	1141106125	32.3254598 32.3419233	10.1478047	.0009569838
1047	1090209	1147730823	32.3573794	10.1510406 10.1542744	.0008550229
1048	1098304	1151022502	32,3798981	10.1575002	.0009541985
1049	1100401	1154330649	32,3%9995	10.16)(350	.0009539588
1050	1109500	1157025000	32.4087085	10.1639636	.0009523810
1051	1104601	1160995651	32,4191301	10.1671893	.0000514748
1052	1106704	1164252608	32.4345495	10.1704129	.0008505703
1053	1108809	116.5.56.	32.4499615	10.1736344	.0009496576
1054	1110916	1170905464	32.4653662	10.1768539	.0009487006

TABLE IX.-LOGARITHM OF NUMBERS FROM 0 TO 1000.

No.	0	1	2	3	4	5	6	7	8	9
-	-							0.45.46		
0	0	00000	30103	47712	60206	69897	77815	84510	90309	95424
10	00000	00432	00860	01284	01703	02119	02530	02938	03342	03743
11	04139	04532	04922	05307	05690	06070	06446	06819	07188	07555
12	07918	08279	08637	08990	09342	09691	10037	10380	10721	11059
13	11394	11727	12057	12385	12710	13033	13354	13672	13988	14301
14	14613	14922	15229	15533	15836	16137	16435	16732	17026	17319
15	17609	17898	18184	18469	18752	19033	19312	19590	19866	20140
14 15 16	20412	20683	20952	21219	21484	21748	22011	22272	22531	22789
17 18 19	23045	23300	23553	23805	24055	24304	24551	24797	25042	25285
18	25527	25768	26007	26245	26482	26717	26951	27184	27416	27646
19	27875	28103	28330	28556	28780	29003	29226	29447	29667	29885
20	30103	30320	30535	30749	30963	31175	.31386	31597	31806	32015
21	32222	32428	32633	32838	33041	33244	33445	33646	33846	34044
22	34242	34439	34635	34830	35025	35218	35411	35603	35793	35984
23	36173	36361	36549	36736	36922	37107	37291	37475	37658	37840
24	38021	38202	38382	38561	38739	38916	39094	39270	39445	39619
25	39794	39967	40140	40312	40483	40654	40824	40993	41162	41330
26	41497	41664	41830	41996	42160	42325	42488	42651	42813	42975
27 28	43136	43297	43157	43616	43775	43933	44091	44248	44404	44560
28	44716	43297 44871	45025	45179	45332	45484	45637	45788	45939	46090
29	46240	46389	46538	46687	46835	46982	47129	47276	47422	47567
30	47712	47857	48001	48144	48287	48430	48572	48714	48855	48996
31	49136	49276	49415	49554	49693	49831	49969	50106	50243	50379
31 32	50515	50651	50786	50920	51055	51189	51322	51455	51587	51720
33	51851	51983	52114	52244	52375	52504	52634	52763	52892	53020
34	53148	53275	53403	53529	53656	53782	53908	54033	54158	54283
35	54407	54531	54654	54777	54900	55022	55145	55267	55388	55509
36	55630	55751	55871	55991	56110	56229	56348	56467	56585	56703
37	56820	56937	57054	57171	57287	57403	57519	57634	57749	57863
38	57978	58093	58206	58320	58433	58546	58659	58771	58883	58995
89	59106	59218	59328	59439	59550	59660	59770	59879	59989	60097
40	60206	60314	60423	60531	60638	60745	60853	60959	61066	61172
41	61278	61384	61490	61595	61700	61805	61909	62014	62118	62221
42	62325	62428	62531	62634	62737	62839	62941	63043	63144	63246
43	63347	63448	63548	63649	63749	63849	63949	64048	64147	64246
44	64345	64444	64542	64640	64738	64836	64933	65031	65128	65225
45	65321	65418	65514	65609	65706	65801	65896	65992	66087	66181
46	66276	66370	66464	66558	66652	66745	66839	66932	67025	67117
47	67210	67302	67394	67486	67578	67669	67761	67852	67943	68034
48	68124	68215	68305	68395	68485	68574	68664	68753	68842	68931
49	69020	69108	69197	69285	69373	69461	69548	69636	69723	69810
50	69897	69984	70070	70157	70243	70329	70415	70501	70586	70672
DOLL OF THE	3000	-	V	CE CHI	1 691	Marine.	23/33	CHECKEN I	11-34	

BALLS I	1 1		19/201		200		1		1	
No.	0	1	2	3	4	5	6	7	8	9
	POPPE	70842	70927	71012	71096	71181	71265	71349	71433	Pri Pri Pr
51	70757	71684	71767	71850	71933	72016	72099	72181	72263	71517 72346
52	72428	72509	72591	72673	72754	72835	72916	72997	73078	
53	73239	73320	73399	73480	73560	73639	73719	73799	73878	73159
54	74036	74115	74194	74273	74351	74429	74507	74586	74663	73957
55 56	74819	74896	74974	75051	75128	75205	75282	75358	75435	74741
56	75587	75664	75740	75815	75891	75967	76042	76118	76193	75511
57	70007		76492	76567	76641	76716	76790	76864		76268
58	76343	76418		77305	77379		77525		76938	77012
59	77085	77159	77232			77452		77597	77670	77743
60	77815	77887	77960	78032	78104	78176	78247	78319	78390	78462
61	78533	78604	78675	78746	78817	78888	78958	79029	79099	79169
62	79239	79309	79379	79449	79518	79588	79657	79727	79796	79865
63	79934	80003	80072	80140	80209	80277	80346	80414	80482	80550
64	80618	80686	80754	80821	80889	80956	81023	81090	81158	81224
65	81291	81358	81425	81491	81558	81624	81690	81757	81823	81889
66	81954	82020	82086	82151	82217	82282	82347	82413	82478	82543
67	82607	82672	82737	82802	82866	82930	82995	83059	83123	83187
68	83251	83315	83378	83442	83506	83569	83632	83696	83759	83822
69	83885	83948	84011	84073	84136	84198	84261	84323	84386	84448
70	84510	84572	84634	84696	84757	84819	84880	84942	85003	85065
	04510	04012	01001	01000	01101		D4000	01012	00000	60000
71 72 73	85126	85187	85248	85309	85370	85431	85491	85552	85612	85673
72	85733	85794	85854	85914	85974	86034	86094	86153	86213	86273
73	86332	86392	86451	86510	86570	86629	86688	86747	86806	86864
74 75 76 77	86923	86982	87040	87099	87157	87216	87274	87332	87390	87448
75	87506	87564	87622	87680	87737	87795	87852	87910	87967	88024
76	88081	88138	88196	88252	88309	88366	88423	88480	88536	88593
77	88649	88705	88762	88818	88874	88930	88986	89042	89098	89154
78	89209	89265	89321	89376	89432	89487	89542	89597	89653	89708
79	89763	89818	89873	89927	89982	90037	90091	90146	90200	90255
78 79 80	90309	90363	90417	90472	90526	90580	90634	90687	90741	90795
01	90848	90902	90956	91009	91062	91116	91169	91222	91275	01900
81 82	91381	91434	91487	91540	91593	91645	.91698	91751	91803	91328
00	91908	91960	92012	92065	92117	92169	92221	92273		91855
83	92428	92480	92531	92583	92634	92686	92737	92789	92324 92840	92376
84	92426	92993	93044	93095	93146	93197	93247	93298		92891
85		92995	93044			93197	00000		93349	93399
86	93450	93500	93551	93601	93651	93702	93752	93802	93852	93902
87	93952	94002	94052	94101	94151	94201	94250	94300	94349	94398
88	94448	94498	94547	94596	94645	94694	94743	94792	94841	94890
89	94939	94988	95036	95085	95134	95182	95231	95279	95328	95376
90	95424	95472	95521	95569	95617	95665	95713	95761	95809	95856
91	95904	95952	95999	96047	96095	96142	96190	96237	96284	96332
92	96379	96426	96473	96520	96567	96614	96661	96708	96755	96802
93	96848	96895	96942	96988	97035	97081	97128	97174	97220	97267
94	97313	97359	97405	97451	97497	97543	97589	97635	97681	97727
95	97772	97818	97864	97909	97955	98000	98046	98091	98137	98182
96	98227	98272	98318	98363	98408	98453	98498	98543	98588	98632
97	98677	96722	98767	98811	98856	98900	98945	98989	99034	99078
98	99123	99167	99211	99255	99300	99344	99388	99432	99476	99520

NOTE TO TABLES OF TRIGONOMETRIC FUNCTIONS.

In the following Tables the values of Sines, Cosines, Tangents, Cotangents, Versines, and Exsecants are carried only to 5 places of decimals; the Table of Secants and Cosecants, however, is given to 7 places of decimals, and from it more accurate determinations of the Sines, etc., may be obtained, if for any special purpose they be required. For, by Secs. 231 and 232,

$$\sin A = \frac{1}{\csc A}; \qquad \cos A = \frac{1}{\sec A}; \qquad \tan A = \frac{\sec A}{\csc A};$$

$$\operatorname{vers} A = 1 - \frac{1}{\sec A}; \quad \operatorname{exsec} A = \sec A - 1; \quad \cot A = \frac{\csc A}{\sec A}.$$
284

	0°	1°	11	2	0 .	3	0	4	0 1	
1	Sine Cosin	Sine C	osin	Sine	Cosin	Sine	Cosin	Sine	Cosin	
1			99985	.03490	.99939	.05234	.99863	.06976	.99756	60
1 2		.01774 .9	9984	.03519	.99938	.05263	.99861	.07005	.99754	59 58
1	3 .00087 One.	.01832 .9	9983	.03577	.99936	.05321	.99858	.07063	.99750	57
1			99983	.03606	.99935	.05350	.99857	.07092	.99748	56
1			99982	.03635	.99934	.05379	.99855	.07121	.99746	55 54
	.00204 One.	.01949 .9	99981	.03693	.99932	.05437	.99852	.07179	.99742	53
1 8			99980	.03723	.99931	.05466	.99851	.07208	.99740	52
1			99980	.03752	.99929	.05495	.99849	.07266	.99738	51 50
1			99979	.03810	.99927	.05553	.99846	.07295	.99734	49
1 15	.00349 .99999	.02094 .9	99978	.03839	.99926	.05582	.99844	.07324	.99731	48
1:			99977	.03868	.99925	.05611	.99842	.07353	.99729	47
14		.02152 .9	99977	.03897	.99924	.05640	.99841	.07382	.99727	46 45
1	6 .00465 .99999	.02211 .9	99976	.03955	.99922	.05698	.99838	.07440	.99723	44
1			99975	.03984	.99921	.05727	.99836	.07469	.99721	43
111			$09974 \mid 09974 \mid$.04013	.99919	.05756	.99834	.07498	.99719	42 41
2			99973	.04071	.99917	.05814	.99831	.07556		40
2			99972	.04100	.99916	.05944	.99829	.07585	.99712	39
2	2 .00640 .99998		99972	.04129	.99915	.05873	.99827	.07614	.99710	38
2			99971	.04159	.99913	.05902	.99826	.07643	.99708	37 36
2			99969	.04217	.99911	.05960	.99822	.07701	.99703	35
2			99969	.04246	.99910	.05989	.99821	.07730	.99701	34
2			99968 99967	.04275	.99909	.06018	.99819	.07759		33
2	00844 .99996	.02589 .	99966	.04333	.99906	.06076	.99815	.07817		31
3	0 .00873 .99996	.02618 .	99966	.04362	.99905	.06105	.99813	.07846	.99692	30
3			99965	.04391	.99904	.06134	.99812	.07875		29
3			99964 99963	.04420	.99902	.06163		.07904	.99687	28 27
3	4 .00989 .99995	.02734 .	99963	.04478	.99900	.06221	.99806	.07962	.99683	26
3			99962	.04507	.99898	.06250	.99804	.07991	.99680	25 24
3			99961 99960	.04536	.99897	.06279	.99803	.08020		23
3	3 .01105 .99994	.02850 .	99959	.04594	.99894	.06337	.99799	.08078	.99673	22
3			99959 99958	.04623	.99893	06366 06395		.08107		21 20
4		The state of the s	1000			.06424		1		19
4			99957 99956	.04682	.99890	.06424		.08165		13
4	3 .01251 .99992	.02996 .	99955	.04740	.99888	.06482	.99790	.08223	.99661	17
4			99954 99953	.04769	.99886	.06511	.99788	.08252	.99659	16
4			99952	.04190	.99883	.06569	.99784	.08310		14
4	7 .01367 .99991	.03112 .	99952	.04856	.99882	.06598	.99782	.08339	.99652	13
4			99951 99950	.04885	.99881	.06627	.99780	.08368		12 11
5			99949	.04943	.99878	.06685	.99776	.08426		10
5			99948	.04972	.99876	.06714	.99774	.08455		9
5	2 .01513 .99989	.03257	99947	.05001	.99875	.06743	.99772	.08484	.99639	8
5 5			99946 99945	.05030	.99873	.06773	.99770	.08513		7 6
5.	5 .01600 .99987	.03345 .9	99944	.05088	.99870	.06831	.99766	.08571	.99632	5
5			99943	.05117	.99869	.06860	.99764	.08600	.99630	4
5			99942 99941	.05146	.99867	.06889	.99762	.08629	.99627	3 2
5	9 .01716 .99985	.03461 .	99940	.05205	.99864	.06947	.99758	.08687	.99622	2
6	-	-	99939	.05234	.99863	.06976	.99756	.08716	.99619	0
,	Cosin Sine	Cosin	Sine	Cosin	Sine	Cosin	Sine	Cosin	Sine	,
	89°	880		8	70	8	3°	8	5°	
-								-	THE RESERVE AND ADDRESS.	

	5°	6°	70	1 00	00	
1				8.	9°	,
-	Sine Cosin					
0	.08716 .99619	.10453 .99452	.12187 .99255	.13917 .99027	.15643 .98769	60
1	.08745 .99617	.10482 .99449	.12216 .99251	.13946 .99023	.15672 .98764	59
3	.08774 .99614 .08803 .99612	.10511 .99446 .10540 .99443	.12245 .99248	.13975 .99019	.15701 .98760	58
4	.08831 .99609	.10569 .99440	.12274 .99244 .12302 .99240	.14004 .99015	.15730 .98755	57
5	.08860 .99607	.10597 .99437	.12331 .99237	.14061 .99006	.1575£ .98751 .15787 .98746	56
6	.08889 .99604	.10626 .99434	.12360 .99233	.14090 .99002	.15816 .98741	54
6 7	.08918 .99602	.10655 .99431	.12389 .99230	.14119 .98998	.15845 .98737	53
8	.08947 .99599	.10684 .99428	.12418 .99226	.14148 .98994	.15873 .98732	52
9	.08976 .99596	.10713 .99424	.12447 .99222	.14177 .98990	.15902 .98728	51
10	.09005 .99594	.10742 .99421	.12476 .99219	.14205 .98986	.15931 .98723	50
11	.09034 .99591	.10771 .99418	.12504 .99215	.14234 .98982	.15959 .98718	49
12	.09063 .99588	.10800 .99415	.12533 .99211	.14263 .98978	.15988 .98714	48
13	.09092 .99586	.10829 .99412	.12562 .99208	.14292 .98973	.16017 .98709	47
14 15	.09121 .99583 .09150 .99580	.10858 .99409 .10887 .99406	.12591 .99204	.14320 .98969	.16046 .98704	46
16	.09179 .99578	.10887 .99406	.12620 .99200 .12649 .99197	.14349 .98965	.16074 .98700	45
17	.09208 .99575	.10945 .99399	.12678 .99193	.14378 .98961 .14407 .98957	.16103 .98695 .16132 .98690	44 43
18	.09237 .99572	.10973 .99396	.12706 .99189	.14436 .98953	.16160 .98686	42
19	.09266 .99570	.11002 .99393	.12735 .99186	.14464 .98948	.16189 .98681	41
20	.09295 .99567	.11031 .99390	.12764 .99182	.14493 .98944	.16218 .98676	40
21	.09324 .99564	.11060 .99386	.12793 .99178	.14522 .98940	.16246 ,98671	39
22	.09353 .99562	.11089 .99383	.12822 .99175	.14551 .98936	.16275 .98667	38
23	.09382 .99559	.11118 .99380	.12851 .99171	.14580 .98931	.16304 .98662	37
24	.09411 .99556	.11147 .99377	.12880 .99167	.14608 .98927	.16333 .98657	36
25 26	.09440 .99553	.11176 .99374	.12908 .99163	.14637 .98923	.16361 .98652	35
27	.09469 .99551 .09498 .99548	.11205 .99370 .11234 .99367	.12937 .99160	.14666 .98919	.16390 .98648	34
28	.09527 .99545	.11234 .99367 .11263 .99364	.12966 .99156 .12995 .99152	.14695 .98914 .14723 .98910	.16419 .98643 .16447 .98638	33 32
29	.09556 .99542	.11291 .99360	.13024 .99148	.14723 .98910 .14752 .98906	.16476 .98633	31
30	.09585 .99540	.11320 .99357	.13053 .99144	.14781 .98902	.16505 .98629	30
31	.09614 .99537	.11349 .99354	.13081 .99141			29
32	.09642 .99534	.11378 .99351	.13110 .99137	.14810 .98897	.16533 .98624 .16562 .98619	28
33	.09671 .99531	.11407 ,99347	.13139 .99133	.14867 .98889	.16591 .98614	27
34	.09700 .99528	.11436 ,99344	.13168 ,99129	.14896 .98884	.16620 .98609	26
35	.09729 .99526	.11465 .99341	.13197 .99125	.14925 .98880	.16648 .98604	25
36	.09758 .99523	.11494 .99337	.13226 .99122	.14954 .98876	.16677 .98600	24
37	.09787 .99520 .09816 .99517	.11523 .99334 .11552 .99331	.13254 .99118	.14982 .98871	.16706 .98595	23 22
39	.09845 .99514	.11552 .99331	.13283 .99114	.15011 .98867 .15040 .98863	.16734 .98590 .16763 .98585	21
40	.09874 .99511	.11609 .99324	.13341 .99106	.15040 .98858	.16792 .98580	20
						-
41 42	.09903 .99508 .09932 .99506	.11638 .99320 .11667 .99317	.13370 .99102	.15097 .98854 .15126 .98849	.16820 .98575 .16849 .98570	19 18
43	.09961 ,99503	.11696 .99314	.13399 .99098 .13427 .99094	.15126 .98849 .15155 .98845	.16849 .98570	17
44	.09990 ,99500	.11725 .99310	.13456 .99091	.15184 .98841	.16906 .98561	16
45	.10019 .99497	.11754 99307	,13485 .99087	.15212 .98836	.16935 .98556	15
46	.10048 .99494	.11783 .99303	.13514 .99083	.15241 .98832	.16964 .98551	14
47	.10077 .99491	.11812 .99300	.13543 .99079	.15270 .98827	.16992 .98546	13
48	.10106 .99488	.11840 .99297	.13572 .99075	.15299 .98823	.17021 .98541	12
49 50	.10135 .99485 .10164 .99482	.11869 .99293	13600 .99071	.15327 .98818 .15356 .98814	.17050 .98536 .17078 .98531	11 10
N. P.			.13629 .99067			
51	.10192 .99479	.11927 .99286	.13658 .99063	.15385 .98809	.17107 .98526	9
52 53	.10221 .99476 .10250 .99473	.11956 .99283 .11985 .99279	.13687 .99059	.15414 .98805	.17136 .98521 .17164 .98516	8 7
54	.10279 .99470	.11985 .99279 .12014 .99276	.13716 .99055 .13744 .99051	.15442 .98800 .15471 .98796	.17193 .98511	6
55	.10308 .99467	.12043 .99272	.13773 .99047	.15500 .98791	.17222 .98506	5
56	.10337 .99464	.12071 .99269	.13802 .99043	.15529 .98787	.17250 .98501	
57	10366 .99461	.12100 .99265	.13831 .99039	.15557 .98782	.17279 .98496	3
58	.10395 .99458	.12129 .99262	.13860 .99035	.15586 .98778	.17308 .98491	2
59	.10424 .99455	.12158 .99258	.13889 .99031	.15615 .98773	.17336 .98486	0
60	.10453 .99452	.12187 .99255	.13917 .99027	.15643 .98769	.17365 .98481	-
-,	Cosin Sine	Cosin Sine	Cosin Sine	Cosin Sine	Cosin Sine	,
	84°	83°	820	81°	80°	
	0.7	00	0.0	OI	00	

-				0.30.00.00.00.00.00.00.00.00.00.00.00.00		
1,	10°	11°	12°	13°	140	
	Sine Cosin	Sine Cosin	Sine Cosin	Sine Cosin	Sine Cosin	
0	.17365 .98481	.19081 .98163	.20791 .97815	.22495 .97437	.24192 .97030 60	
1	.17393 .98476	.19109 .98157 .19138 .98152	.20820 .97809 .20848 .97803	.22523 .97430 .22552 .97424	.24220 .97023 59 .24249 .97015 58	
3	.17422 .98471 .17451 .98466	.19167 .98146	.20877 .97797	.22580 .97417	.24249 .97015 58 .24277 .97008 57	
4	.17479 .98461	.19195 .98140	.20905 .97791	.22608 .97411	.24305 .97001 56	
5	.17508 .98455	.19224 .98135	.20933 .97784	.22637 .97404	.24333 .96994 5	5
6	.17537 .98450	.19252 .98129	.20962 .97778	.22665 497398	.24362 .96987 5	
7	.17565 .98445 .17591 .98440	.19281 .98124 .19309 .98118	.20990 .97772 .21019 .97766	.22693 .97391 22722 .97384	.24390 .96980 58 .24418 .96973 58	
8 9	.17623 .98435	.19338 .98112	.21047 .97760	.22750 .97378	.24418 .96973 55 .24446 .96966 5	
10	.17651 ,98430	.19356 .98107	.21076 .97754	.22778 .97371	.24474 .96959 50	
11	.17680 .98425	.19395 .98101	.21104 .97748	.22807 .97365	.24503 .96952 49)
12	.17708 .98420	.19423 .98096	.21132 .97742	.22835 .97358	.24531 .96945 48	
13	.17708 .98420 .17737 .98414 .17766 .98109 .17794 .98404	.19452 .98090 .19481 .98084	.21161 .97735 .21189 .97729	.22863 .97351 .22892 .97345	.24559 .96937 47	
14 15	.17794 .98404	.19509 .98079	.21218 .97723	.22892 .97345 .22920 .97338	.24587 .96930 46 .24615 .96923 48	
16	.17823 .98399	.19538 .98073	.21246 .97717	.22948 .97331	.24644 .96916 44	
17	.17852 .98394	.19566 .98067	.21275 .97711	.22977 .97325	.24672 .96909 48	3
18	.17880 .98389	.19595 .98061	.21303 .97705	.23005 .97318	.24700 .96902 49	
19 20	.17909 .98383 .17937 .98378	.19623 .98056 .19652 .98050	.21331 .97698 .21360 .97692	.23033 .97311 .23062 .97304	.24728 .96894 41 .24756 .96887 40	
		The second secon				
21 22	.17966 .98373 .17995 .98368	.19680 .98044 .19709 .98039	.21388 .97686 .21417 .97680	.23090 .97298 .23118 .97291	.24784 .96880 39 .24813 .96873 38	
23	.18023 .98362	.19737 .98033	.21445 .97673	.23146 .97284	.24813 .96873 38 .24841 .96866 37	
24	.18052 .98357	.19766 .98027	.21474 .97667	.23175 .97278	.24869 .96858 36	
25	.18081 .98352	.19794 .98021	.21502 .97661	.23203 .97271	.24897 .96851 33	5
26	.18109 .98347	.19823 .98016	.21530 .97655	.23231 .97264	.24925 .96844 34	
27 28	.18138 .98341 .18166 .98336	.19851 .98010 .19880 .98004	.21559 .97648 .21587 .97642	.23260 .97257 .23288 .97251	.24954 .96837 33 .24982 .96829 33	
29	.18195 .98331	.19908 .97998	.21616 .97636	.23316 .97244	.25010 .96822 31	
30	.18224 .98325	.19937 .97992	.21644 .97630	.23345 .97237	.25038 .96815 30	
31	.18252 .98320	.19965 .97987	.21672 .97623	.23373 .97230	.25066 .96807 29	
32	.18281 .98315	.19994 .97981	.21701 .97617	.23401 .97223	.25094 .96800 28	
33	.18309 .98310 .18338 .98304	.20022 .97975 .20051 .97969	.21729 .97611 .21758 .97604	.23429 .97217 .23458 .97210	.25122 .96793 27 .25151 .96786 26	
35	.18367 .98299	.20079 .97963	.21786 .97598	.23486 .97203	.25151 .96786 26 .25179 .96778 25	
36	.18395 .98294	.20108 .97958	.21814 .97592	.23514 .97196	.25207 .96771 24	1
37	.18424 .98288	.20136 .97952	.21843 .97585	.23542 .97189	.25235 .96764 23	3
38	.18452 .98283 .18481 .98277	.20165 .97946	.21871 .97579	.23571 .97182	.25263 .96756 22	
40	.18481 .98277 .18509 .98272	.20193 .97940 .20222 .97934	.21899 .97573 .21928 .97566	.23599 .97176 .23627 .97169	.25291 .96749 21 .25320 .96742 20	
41	.18538 .98267	.20250 .97928	.21956 .97560	.23656 .97162	.25348 .96734 19	
42	.18567 .98261	.20279 .97922	.21985 .97553	.23684 .97155	.25376 .96727 18	
43	.18595 .98256	.20307 .97916	.22013 .97547	.23712 .97148	.25404 .96719 17	7
44 45	.18624 .98250	.20336 .97910	.22041 .97541	.23740 .97141	.25432 .96712 16	
45 46	.18652 .98245 .18681 .98240	.20364 .97905 .20393 .97899	.22070 .97534 .22098 .97528	.23769 .97134 .23797 .97127	.25460 .96705 15 .25488 .96697 14	
47	.18710 .98234	.20421 .97893	.22126 .97521	.23825 .97120	.25516 .96690 13	
48	.18738 .98229	.20450 .97887	.22155 .97515	.23853 .97113	.25545 .96682 12	3
49	.18767 .98223	.20478 .97881	.22183 .97508	.23882 .97106	.25573 .96675 11	
50	.18795 .98218	.20507 .97875	.22212 .97502	.23210 .97100	.25601 .96667 10	
51 52	.18824 .98212 .18852 .98207	.20535 .97869 .20563 .97863	.22240 .97496 .22268 .97489	.23938 .97093 .23966 .97086	.25629 .96660 9 .25657 .96653 8	
53	.18881 .98201	.20592 .97857	.22297 .97483	.23966 .97086 .23995 .97079	.25657 .96653 8 .25685 .96645 7	
54	.18910 .98196	.20620 .97851	.22325 .97476	.24023 .97072	.25713 .96638 6	5
55	.18938 .98190	.20649 .97845	.22353 .97470	.24051 .97065	.25741 .96630 5	,
56 57	.18967 .98185	.20677 .97839	.22382 .97463 .22410 .97457	.24079 .97058	.25769 .96623 4 .25798 .96615 3	
58	.19024 .98174	.20706 .97833 .20734 .97827	.22410 .97457 .22438 .97450	.24108 .97051 .24136 .97044	.25798 .96615 3 .25826 .96608 2	
59	.19052 .98168	.20763 .97821	.22467 .97444	.24164 .97037	.25854 .96600 1	
60	.19081 .98163	.20791 .97815	.22495 .97437	.24192 .97030		
1,	Cosin Sine	Cosin Sine	Cosin Sine	Cosin Sine	Cosin Sine	6
	79°	78°	770	76°	75°	
-						

	15°						
	,	15°	16°	17°	18°	19°	,
		Sine Cosin	Sine Cosin	Sine Cosin	Sine Cosin	Sine Cosin	
ì	0	.25882 .96593	.27564 .96126	.29237 .95630	.30902 .95106	.32557 .94552	60
	1 2	.25910 .96585 .25938 .96578	.27592 .96118 .27620 .96110	.29265 .95622 .29293 .95613	.30929 .95007 .30957 .95088		59 58
ì	3	.25966 .96570	.27648 .96102	.29321 .95605	.30985 .95079		57
	4	.25994 .96562	.27676 .96094	.29348 .95596	.31012 .95070	.32667 .94514	56
	5	.26022 .96555 .26050 .96547	.27704 .96086 .27731 .96078	.29376 .95588 .29404 .95579	.31040 .95061 .31068 .95052		55
	6 7	.26079 .96540	.27759 .96070	.29432 .95571	.31095 .95043		54 53
	8	.26107 .96532	.27787 .96062	.29460 .95562	.31123 .95033	.32777 .94476	52
	9	.26135 .96524 .26163 .96517	.27815 .96054 .27843 .96046	.29487 .95554 .29515 .95545	.31151 .95024 .31178 .95015		51
H							
	11 12	.26191 .96509 .26219 .96502	.27871 .96037 .27899 .96029	.29543 .95536 .29571 .95528	.31206 .95006 .31233 .94997		49 48
	13	.26247 .96494	.27927 .96021	.29599 .95519	.31261 .94988	.32914 .94428	47
	14	.26275 .96486	.27955 .96013	.29626 .95511	.31289 .94979		46
1	15 16	.26303 .96479 .26331 .96471	.27983 .96005 .28011 .95997	.29654 .95502 .29682 .95493	.31316 .94970 .31344 .94961		45 44
ı	17	.26359 .96463	.28039 .95989	.29710 .95485	.31372 .94952		43
	18	.26387 .96456	.28067 .95981	.29737 .95476	.31399 .94943	.33051 .94380	42
	19 20	.26415 .96448 .26443 .96440	.28095 .95972 .28123 .95964	.29765 .95467 .29793 .95459	.31427 .94933 .31454 .94924		41 40
			Contract to the last to the la	A CONTRACTOR OF THE PARTY OF TH	The second second		
	21 22	.26471 .96433 .26500 .96425	.28150 .95956 .28178 .95948	.29821 .95450 .29849 .95441	.31482 .94915 .31510 .94906		39 38
١	23	.26528 .96417	.28206 .95940	.29876 .95433	.31537 .94897	.33189 .94332	37
	24	.26556 .96410	.28234 .95931	.29904 .95424	.31565 .94888	.33216 .94322	36
	25 26	.26584 .96402 .26612 .96394	.28262 .95923 .28290 .95915	.29932 .95415 .29960 .95407	.31593 .94878 .31620 .94869		35
1	27	.26640 .96386	.28318 .95907	.29987 .95398	.31648 .94860		33
	28	.26668 .96379	.28346 .95898	.30015 .95389	.31675 .94851	.33326 .94284	32
	29 30	.26696 .96371 .26724 .96363	.28374 .95890 .28402 .95882	.30043 .95380 .30071 .95372	.31703 .94842 .31730 .94832		31
	31						29
	32	.26752 .96355 .26780 .96347	.28429 .95874 .28457 .95865	.30098 .95363 .30126 .95354	.31758 .94823 .31786 .94814		28
	33	.26808 .96340	.28485 .95857	.30154 .95345	.31813 .94805	.33463 .94235	27
	34	.26836 .96332	.28513 .95849	.30182 .95337	.31841 .94795	.33490 .94225	26
	35 36	.26864 .96324 .26892 .96316	.28541 .95841 .28569 .95832	.30209 .95328 .30237 .95319	.31868 .94786 .31896 .94777	.33518 .94215 .33545 .94206	25 24
9	37	.26920 .96308	.28597 .95824	.30265 .95310	.31896 .94777 .31923 .94768		23
	38	.26948 .96301	.28625 .95816	.30292 .95301	.31951 .94758	.33600 .94186	23
1	39 40	.26976 .96293 .27004 .96285	.28652 .95807 .28680 .95799	.30320 .95293 .30348 .95284	.31979 .94749 .32006 .94740		21 20
	41	.27032 .96277		.30376 .95275	.32034 .94730	The second second	19
	41	.27060 .96269	.28708 .95791 .28736 .95782	.30403 .95266	.32034 .94730 .32061 .94721		13
	43	.27088 .96261	.28764 .95774	.30431 .95257	.32089 .94712	.33737 .94137	17
	44	.27116 .96253	.28792 .95766	.30459 .95248	.32116 .94702		16 15
	45 46	.27144 .96246 .27172 .96238	.28820 .95757 .28847 .95749	.30486 .95240 .30514 .95231	.32144 .94693 .32171 .94684		10
	47	.27200 .96230	.28875 .95740	.30542 .95222	39199 94674	.33846 .94098	13
	48	.27228 .96222	.28903 .95732	.30570 .95213	.32227 .94665		12
	49 50	.27256 .96214 .27284 .96206	.28931 .95724 .28959 .95715	.30597 .95204	.32254 .94656 .32282 .94646		11 10
	51	.27312 .96198	.28987 .95707	.30653 .95186	.32309 .94637	.33956 .94058	9
	52	.27340 .96190	.29015 .95698	.30680 .95177	.32337 .94627	.33983 .91019	8
	53	.27368 .96182	.29042 .95690	.30708 .95168	.32364 .94618	.34011 .94039	8 7 6
	54 55	.27396 .96174 .27424 .96166	.29070 .95681 .29098 .95673	.30736 .95159 .30763 .95150	.32392 .94609 .32419 .94599	.34038 .94029 .34065 .94019	5
1	56	.27452 .96158	.29095 .95664	.30791 .95142	.32447 .94590	.34093 .94009	4 3
	57	.27480 .96150	.29154 .95656	.30819 .95133	.32474 .93580	.34120 .93999	3
	58 59	.27508 .96142 .27536 .96134	.29182 .95647 .29209 .95639	.30846 .95124 .30874 .95115	.32502 .94571 .32529 .94561	.34147 .93989 .34175 .93979	2 1
	60	.27564 .96126	.29237 .95630	.30902 .95106	.32557 .94552	.34202 .93969	0
	-	Cosin Sine	Cosin Sine	Cosin Sine	Cosin Sine	Cosin Sine	,
	'	740	73°	72°	71°	70°	
u	Second .	Name of the Owner, when the Parket	of selection of the second land and and	STATE OF STREET	THE RESERVE THE PERSON NAMED IN	And the second second second second	-

	2	0°	2	10	2	20	2:	3°	2	10	
1	Sine	Cosin	Sine	Cosin	Sine	Cosin	Sine	Cosin	Sine	Cosin	'
0	.34202	.93969	.35837	.93358	.37461	.92718	.39073	,92050	.40674	.91355	60
	.34229	.93959	.35864	.93348	.37488	.92707	.39100	.92039	.40700	.91343	59
1 2 3	.34257	.93949	.35891	.93337	.37515	.92697	.39127	.92028	.40727	.91331	58
	.34284	.93939	.35918	.93327	.37542	.92686	.39153	.92016	.40753	.91319	57
4	.34311	.93929	.35945	.93316	.37569	.92675	.39180	.92005	.40780	.91307	56
5	.34339	.93919		.93306	.37595	.92664	.39207	.91994		.91295	55
6	.34366	.93909		.93295	.37622	.92653	.39234	.91982	.40833	.91283	54 53
8	.34393	.93899	.36027	.93274	.37676	.92631	.39287	.91971	.40860	.91272	52
9	.34448	.93879	.36081	.93264	.37703	.92620	.39314	.91938	.40913	.91248	51
10	.34475	.93869	.36108	.93253	.37730	.92609	.39341	.91936	.40939	.91236	50
11	.34503	.93859	.36135	.93243	.37757	.92598	.39367	.91925	.40966	.91224	49
12	.34530	.93849	.36162	.93232	.37784	.92587	.39394	.91914	.40992	.91212	48
13	,34557	.93839	.36190	.93222	.37811	.92576	.39421	.91902	.41019	.91200	47
14	.34584	.93829	.36217	.93211	.37838		.39448		.41045	.91188	46
15	.34612	.93819	.36244	.93201	.37865		.39474		.41072	.91176	45
16	.34639	.93809	.36271	.93190	.37892		.39501	.91868	.41098	.91164	
17	.34666	.93799	.36298	.93180	.37919	.92532	.39528		.41125	.91152	43
18	.34694 .34721	.93789	.36325	.93169	.37946	.92521	.39555	.91845	.41151	.91140	42
20	.34748	.93769	.36379	.93139	.37999		.39608	.91822	.41178	.91116	40
						1	77.00	The same of		DESCRIPTION	1
21	.34775	.93750	.36406		.38026		.39635		.41231	.91104	39
22 23	.34803 .34830	.93748	.36434	.93127	.38053		.39661 .39688	.91799	.41257	.91092 .91080	38
24	.34857	.93728	.36488	.93106	.38107	.92455	.39715	.91775	.41310	.91068	36
25	.34884	.93718	.36515		.38134		.39741	.91764	.41337	.91056	35
26	.34912		.36542	.93084	.38161		.39768	.91752	.41363		34
27	.34939		.36569	.93074	.38188		.39795		.41390		33
28	.34966		.36596	.93063	.38215	.92410	.39822		.41416	.91020	32
29	.34993		.36623	.93052	.28241		.39848	.91718	.41443	.91008	31
30	.35021	.93667	.36650	1	.38268	Part of the last	.39875	A COUNTY OF THE PARTY OF THE PA	.41469		30
31	.35048		.36677		.38295		.39902	.91694	.41496		29
32	.35075		.36704		.38349	.92355	.39928	.91683	.41522	.90972	28 27
34	.35130		.36758	.92999	.38376	.92343	.39982		,41575	.90948	26
35	.35157	.93616	.36785		.38403	.92332	.40008		41602		25
36	.35184		.36812	.92978	.38430		.40035	.91636	.41628	.90924	24
37	.35211	93596	.36839	.92967	.38456	.92310	.40062	.91625	.41655	.90911	23
38	.35239	.93585	.36867	.92956	.38483	.92299	.40088		.41681	.90899	22
39	.35266		.36894		.38510		.40115		.41707	.90887	21
40	.35293	1	1000000	.92935	.38537	1	.40141		.41734	1	20
41	.35320		.36948		.38564	.92265	.40168		.41760		
42 43	.35347	.93544	.36975		.38591	.92254	.40195	.91566	.41787	.90851	18
44	.35402	.93534	.37029	.92902	.38617	.92243	.40221	.91555	.41813	.90839	16
45	.35429	.93514	.37056	.92881	.38671	.92220	.40275	.91531	.41866	.90814	15
46	.35456	.93503	.37083	.92870	.38698		.40301	.91519	41892		
47	.35484	.93493	.37110	.92859	.38725		.40328	.91508	.41919	.90790	13
48	.35511	.93483	.37137	.92849	.38752	.92186	.40355	.91496	.41945	.90778	12
49	.35538		.37164		.38778	.92175	.40381	.91484	.41972	.90766	11
50	.35565	0.00	.37191	.92827	.38805	-	.40408		.41998	100000	1
51	.35592		.37218		.38832	.92152	.40434		.42024		9 8 7 6 5 4 3
52	.35619	.93441	.37245	.92805	.38859	.92141	.40461	.91449	.42051		8
53 54	.35647 .35674	.93431	.37272		.38886		.40488	.91437	.42077		17
55	.35701	.93420	.37326		.38912		.40514		.42104		0
56	.35728	.93400	.37353		.38966		.40567	.91414	.42156		1
57	.35755	.93389	.37380		.38993		.40594	.91390	.42183		3
58	.35782	.93379	.37407	.92740	.39020		.40621	.91378	42209	.90655	2
59	.35810	.93368	.37434	.92729	.39046	.92062	.40647	.91366	.42235	.90643	2
60	.35837	.93358	.37461	.92718	.39073	.92050	.40674	.91355	.42262	.90631	0
1,	Cosin	Sine	Cosin	Sine	Cosin	Sine	Cosin	Sine	Cosin	Sine	-
TA I	R	90	Q	80	0	70	0	6°	0	50	,
	0.	1	0	9	0		0	0	0	9	

-	0.5		080		
1	25°	26°	270	28°	290
_	Sine Cosin	Sine Cosin	Sine Cosin	Sine Cosin	Sine Cosin
0	.42262 .90631	.43837 .89879	.45399 .89101	.46947 .88295	.48481 .87462 60
1	.42288 .90618 .42315 .90606	.43863 .89867 .43889 .89854	.45425 .89087 .45451 .89074	.46973 .88281 .46999 .88267	.48506 .87448 59 .48532 .87434 58
3	42341 .90594	.43916 .89841	.45477 .89061	.47024 .88254	.48557 .87420 57
4	.42367 .90582	.43942 .89828	.45503 .89048	.47050 .88240	.48583 .87406 56
5	.42394 .90569	.43968 .89816	.45529 .89035	.47076 .88226	.48608 .87391 55
6 7	.42420 .90557 .42446 .90545	.43994 .89803 .44020 .89790	.45554 .89021 .45580 .89008	.47101 .88213 .47127 .88199	.48634 .87377 54
8	.42473 .90532	.44020 .89790 .44046 .89777	.45606 .88995	.47127 .88199 .47153 .88185	.48659 .87363 53 .48684 .87349 52
9	.42499 .90520	.44072 .89764	.45632 .88981	.47178 .88172	.48710 .87335 51
10	.42525 .90507	.44098 .89752	.45658 .88968	.47204 .88158	.48735 .87321 50
11	.42552 .90495	.44124 .89739	.45684 .88955	.47229 .88144	.48761 .87306 49
12	.42578 .90483	.44151 .89726	.45710 .88942 .45736 .88928	.47255 .88130 .47281 .88117	.48786 .87292 48
13	.42604 .90470 .42631 .90458	.44177 .89713	.45736 .88928 .45762 .88915	.47281 .88117	.48811 .87278 47
14	.42631 .90458 .42657 .90446	.44203 .89700 .44229 .89687	.45762 .88915 .45787 .88902	.47306 .88103 .47332 .88089	.48837 .87264 46 .48862 .87250 45
16	.42683 .90433	.44255 .89674	.45813 .88888	.47358 .88075	.48888 .87235 44
17	.42709 .90421	.44281 .89662	4.45839 .88875	.47383 .88062	.48913 .87221 43
18	.42736 .90408	.44307 .89649	.45865 .88862	.47409 .88048	.48938 .87207 42
19 20	.42762 .90396 .42788 .90383	.44333 .89636 .44359 .89623	.45891 .88848 .45917 .88835	.47434 .88034 .47460 .88020	.48964 .87193 41 .48989 .87178 40
1					
21 22	.42815 .90371 .42841 .90358	.44385 .89610 .44411 .89597	.45942 .88822 .45968 .88808	.47486 .88006 .47511 .87993	.49014 .87164 39 .49040 .87150 38
23	.42867 .90346	.44437 .89584	45994 .88795	.47537 .87979	49065 .87136 37
24	.42894 .90334	.44464 .89571	.46020 .88782	47562 87965	.49090 .87121 36
25	.42920 .90321	.44490 .89558	.46046 .88768	.47588 .87951 .47614 .87937	.49116 .87107 35
26 27	.42946 .90309 .42972 .90296	.44516 .89545 .44542 .89532	.46072 .88755 .46097 .88741	47614 .87937	.49141 .87093 34 .49166 .87079 33
28	.42999 .90284	.44568 .89519	.46123 .88728	.47639 .87923 .47665 .87909	49192 .87064 32
29	.43025 .90271	.44594 .89506	.46149 .88715	.47690 .87896	.49217 .87050 31
30	.43051 .90259	.44620 .89493	.46175 .88701	.47716 .87882	.49242 .87036 30
31	.43077 .90246	.44646 .89480	.46201 .88688	.47741 .87868	.49268 .87021 29
32	.43104 .90233	.44672 .89467	.46226 .88674	.47767 .87854	.49293 .87007 28
33	.43130 .90221 .43156 .90208	.44698 .89454 .44724 .89441	.46252 .88661 .46278 .88647	.47793 .87840 .47818 .87826	.49318 .86993 27 .49344 .86978 26
35	.43182 .90196	.44750 .89428	46304 .88634	47844 .87812	49369 .86964 25
36	.43209 .90183	.44776 .89415	.46330 .88620	.47869 .87798	.49394 .86949 24
37	.43235 .90171	.44802 .89402	.46355 .88607	.47895 .87784	.49419 .86935 23
38	.43261 .90158 .43287 .90146	.44828 .89389 .44854 .89376	.46381 .88593 .46407 .88580	.47920 .87770 .47946 .87756	.49445 .86921 22 .49470 .86906 21
40	43313 .90133	.44880 .89363	.46433 .88566	.47971 .87743	49495 .86892 20
41	.43340 .90120	.44906 .89350	.46458 .88553	.47997 .87729	.49521 .86878 19
42	.43366 .90108	.44932 .89337	.46484 .88539	.48022 .87715	.49546 .86863 18
43	.43392 .90095	.44958 .89324	.46510 .88526	.48048 .87701	.49571 .86849 17
44	.43418 .90082	.44984 .89311	.46536 .88512	.48073 .87687	.49596 .86834 16 .49622 .86820 15
45 46	.43445 .90070	.45010 .89298 .45036 .89285	.46561 .88499 .46587 .88485	.48099 .87673 .48124 .87659	.49622 .86820 15 .49647 .86805 14
47	.43497 .90045	45062 .89272	.46613 .88472	.48150 .87645	49672 86791 13
48	.43523 .90032	.45088 .89259	.46639 .88458	.48175 .87631	.49697 .86777 12
49	.43549 .90019	.45114 .89245	.46664 .88445	.48201 .87617	.49723 .86762 11
50	.43575 .90007	.45140 .89232	.46690 .88431	.48226 .87603	.49748 .86748 10
51	.43602 .89994 .43628 .89981	.45166 .89219	.46716 .88417 .46742 .88404	.48252 .87589 .48277 .87575	.49773 .86733 9 .49798 .86719 8
52 53	.43628 .89981 .43654 .89968	.45192 .89206 .45218 .89193	.46742 .88404 .46767 .88390	.48303 .87561	.49798 .86719 8 .49824 .86704 7 .49849 .86690 6
54	.43680 .89956	.45243 .89180	.46793 .88377	.48328 .87546	.49849 .86690 6
55	.43706 .89943	.45269 .89167	.46819 .88363	.48354 .87532	.49874 .86675 5 .49899 .86661 4
56	.43733 .89930	.45295 .89153	.46844 .88349 .46870 .88336	.48379 .87518 .48405 .87504	.49899 .86661 4 .49924 .86646 8
57 58	.43759 .89918 .43785 .89905	.45321 .89140 .45347 .89127	.46896 .88322	.48405 .87504 .48430 .87490	49950 86632 2
59	.43811 .89892	.45373 .89114	.46921 .88308	.48456 .87476	.49975 .86617 1
_60	.43837 .89879	.45399 .89101	.46947 .88295	.48481 .87462	.49950 .86632 2 .49975 .86617 1 .50000 .86603 0
1,	Cosin Sine	Cosin Sine	Cosin Sine	Cosin Sine	Cosin Sine
1	64°	63°	62°	61°	60°
-	THE RESERVE THE PARTY OF THE PA				

Sine Cosin Sine Cosin Sine Cosin Sine Cosin	1		000	010		00	20	0.0	20 1	0.	10 1	-
	I	,		1		-		-				1
1 5.0025 86588 51529 85702 59017 84749 54848 88851 55948 82871 58 3 50076 86539 51579 85672 59066 84739 54537 88819 55592 82855 57 4 50101 86545 51604 85657 53901 84743 54561 83904 55061 82835 556 5 5 5 5 5 5 5 5		_			- I					-	-	-
2 50050 86573 51554 85687 5906 8473 54513 88891 55909 82855 57 4 55010 8054 4 51004 85657 5906 8473 54561 8890 56606 8289 56 5 50126 86530 51628 85642 53115 84738 54586 83878 55040 82825 55 6 50151 86515 51663 85627 5314 84712 54610 83772 55046 82820 55 6 50201 88146 51703 85507 5314 84712 54610 83772 55046 8280 54 8 50201 88146 51703 85507 5314 8466 54638 83704 56112 82773 52 9 50227 88471 51728 85585 55214 8466 54683 83724 56136 82707 51 0 50252 88457 51753 85567 55282 8466 54683 83724 56136 82707 51 0 50252 88457 51753 85567 55282 84666 54683 83724 56136 82707 51 0 50252 88457 51753 85567 55282 84666 54683 83724 56136 82707 51 0 50252 88457 51753 85567 55282 84606 54683 83724 56136 82707 51 0 50252 88457 51753 85567 53282 84629 5472 54000 54000 54000 5400 5400 5400 5400	1			.51504 .8			.84805	54464	.83867			
3 5.0076 ,86559 ,51579 ,85672 ,5906 ,84739 ,54587 ,83819 ,55902 ,82855 57 4 50101 ,85545 ,51004 ,85657 ,59019 ,84743 ,54561 ,85804 ,50016 ,85825 55 6 .50151 ,86515 ,51628 ,85627 ,53140 ,84712 ,54610 ,85772 ,5004 ,82822 55 7 50176 ,86501 ,51678 ,83612 ,53164 ,84697 ,54635 ,83756 ,5004 ,82826 55 8 .50201 ,86486 ,51703 ,85507 ,53189 ,84611 ,54658 ,83749 ,56112 ,82773 ,53189 ,84611 ,51728 ,83582 ,53214 ,8466 ,54683 ,83744 ,56136 ,82757 ,511 0 ,50232 ,86457 ,51728 ,85581 ,53234 ,8466 ,54683 ,83744 ,56136 ,82757 ,51 11 ,50277 ,86442 ,51778 ,85551 ,53263 ,84635 ,54732 ,83692 ,56184 ,82724 12 ,50302 ,86427 ,51803 ,85536 ,53288 ,84630 ,54708 ,83692 ,56184 ,82724 13 ,50327 ,86413 ,51828 ,85521 ,53312 ,84604 ,54781 ,85600 ,56228 ,85902 ,86184 14 ,50552 ,86369 ,51502 ,85506 ,53337 ,84586 ,54905 ,83645 ,5626 ,82675 ,46 15 ,50377 ,86344 ,51877 ,85401 ,53361 ,84573 ,54829 ,83629 ,56260 ,82675 ,46 15 ,50377 ,86344 ,51877 ,85401 ,53361 ,84573 ,54829 ,83629 ,56260 ,82653 16 ,50403 ,86369 ,51902 ,85476 ,53358 ,8457 ,54854 ,88613 ,50305 ,8943 18 ,50453 ,86340 ,51927 ,85461 ,53411 ,84542 ,54878 ,83597 ,55329 ,82936 19 ,50478 ,86925 ,51902 ,85466 ,53413 ,54604 ,54781 ,88567 ,56339 ,82610 19 ,50478 ,86925 ,51977 ,85431 ,53400 ,84511 ,54962 ,83554 ,56339 ,82610 19 ,50478 ,86925 ,51977 ,85431 ,53400 ,84511 ,54962 ,83554 ,56401 ,82577 10 ,50478 ,86925 ,51977 ,85431 ,53400 ,8444 10 ,50503 ,86310 ,52002 ,85416 ,53418 ,8445 ,54961 ,83545 ,54649 ,82544 ,38 12 ,50503 ,86281 ,52651 ,83355 ,3534 ,84464 ,54999 ,83517 ,56449 ,82544 ,38 12 ,50508 ,86287 ,52108 ,83355 ,35334 ,84464 ,54999 ,83517 ,56449 ,82544 ,38 12 ,50508 ,86287 ,52276 ,8350 ,53538 ,84484 ,55024 ,83501 ,56478 ,8252 13 ,50578 ,86280 ,5276 ,8350 ,53538 ,84484 ,55024 ,83501 ,56478 ,8252 13 ,50578 ,86280 ,5276 ,8350 ,53538 ,84484 ,5499 ,83517 ,56449 ,82544 ,38 13 ,50578 ,86280 ,55276 ,83504 ,53505 ,83858 ,8450 ,56404 ,82517 14 ,50508 ,86281 ,52576 ,83504 ,53505 ,84460 ,55492 ,83845 ,56404 ,82517 15 ,50588 ,86281 ,55276 ,83504 ,83505	1	2		51554 .8	5687			.54513	.83835			
5 5.0126 86530 5.01028 85642 55115 84728 54586 83788 56040 82822 55 6 650511 86515 1.5653 85367 5.53140 84712 5.54610 83772 56064 82805 58 85061 85064 82805 53 85061 85064 82805 53 85061 85064 82805 53 85061 85064 82805 53 85061 85064 82805 53 85061 85064 82805 53 85061 85064 82805 53 85061 85064 82805 53 85061 85064 82805 53 85061 85064 82805 53 85061 85064 82805 53 85061 85064 82805 53 85061 85064 82805 53 85061 85064 82805 54705 83 85061 85064 82805 54705 83 85061 85064 82805 54705 83 85061 85064 82805 54705 83 85062 56106 82741 50 50023 86427 51803 85536 53288 84650 54703 83602 56160 82741 50 50027 86442 51778 85351 53203 84650 54703 83602 56164 82724 49 12 50302 86427 51803 85356 53237 84588 54805 54705 83062 56164 82724 49 12 50302 86427 51802 85050 53237 84588 54805 83645 56252 82602 82602 8471 14 50352 86303 51828 85506 5337 84588 54805 83645 56252 82602 82602 8471 14 50352 86303 51802 83406 53361 85430 54804 54781 83600 56232 82602 82605 15 50028 8460 54781 83600 56232 82602 82605 8471 15 50037 86325 51907 85461 53341 84549 54785 83602 56236 82803 5460 84511 85060 5623 82600 850	1	3		.51579 .8	5672	.53066	.84759	.54537	.83819	.55992	.82855	57
6 , 50151 , 86515 , 51653 , 85627 , 53140 , 84712 , 54610 , 85772 , 50064 , 82806 54 7 , 50176 , 86501 , 51678 , 85612 , 53164 , 84697 , 54685 , 83740 , 56112 , 82773 52 9 , 50227 , 86471 , 51728 , 85585 , 53214 , 8466 , 54685 , 83740 , 56112 , 82773 52 10 , 50252 , 86457 , 51728 , 85567 , 55238 , 84660 , 54685 , 83740 , 56112 , 82773 52 11 , 50277 , 86442 , 51778 , 85567 , 55238 , 84630 , 54708 , 83708 , 56160 , 82741 50 12 , 50302 , 86427 , 51803 , 85536 , 53288 , 84630 , 54738 , 83692 , 56160 , 82704 13 , 50327 , 86432 , 51803 , 85536 , 53288 , 84630 , 54781 , 83660 , 56232 , 82992 , 47 14 , 50352 , 86433 , 51832 , 85560 , 53327 , 84588 , 54905 , 83676 , 56208 , 82708 13 , 50327 , 86434 , 51828 , 85521 , 53312 , 84604 , 54781 , 83660 , 56232 , 82992 , 47 14 , 50352 , 86393 , 51892 , 85566 , 53327 , 84588 , 54905 , 83645 , 50266 , 82675 15 , 50377 , 86341 , 51877 , 85491 , 53361 , 84573 , 54829 , 83629 , 50280 , 82659 , 45 16 , 50103 , 86396 , 51902 , 85476 , 53386 , 84557 , 54848 , 88613 , 56305 , 82643 17 , 50428 , 86354 , 51927 , 85481 , 53460 , 84511 , 54927 , 83563 , 56305 , 82643 18 , 50453 , 86340 , 51922 , 85461 , 53453 , 84520 , 54902 , 85841 , 56353 , 82640 20 , 50503 , 86310 , 52002 , 85416 , 53435 , 84485 , 54961 , 88577 , 56449 , 82544 21 , 50528 , 86295 , 52002 , 85416 , 53438 , 84495 , 54961 , 88577 , 56449 , 82544 22 , 50503 , 86281 , 52051 , 85385 , 53533 , 84464 , 54909 , 88517 , 56449 , 82544 23 , 50578 , 86266 , 52076 , 83570 , 53558 , 84483 , 55048 , 83485 , 54061 , 82577 , 84584 25 , 50028 , 89327 , 52076 , 83570 , 53558 , 84481 , 55042 , 83641 , 83641 , 83642 , 83641 , 53642 , 83641 , 83642 , 83641 , 83642 , 83641 , 83642 , 83641 , 83642 , 83641 , 83642 , 83641 , 83642 , 83641 , 83642 , 83641 , 83642 , 83641 , 83642 , 83641 , 83642 , 83641 , 83642 , 83641 , 83642 , 83641 , 83642 , 83641 , 83642	1						.84743					
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11	1			.51728 .8								
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14	1				35521		.84604	54781	.83660		82692	
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17 50428 86354 5.51927 8.5461 5.3411 8.1542 5.4509 8354 5.6632 8.2010 42 19 50478 86325 5.1977 8.5431 5.3460 84511 5.4927 83565 5.6377 8.2593 41 20 50503 86310 5.2002 8.5416 5.3484 8.4495 5.4951 83549 5.66401 8.2577 40 21 5.5058 86295 5.2026 8.5401 5.5353 8.4184 5.49975 88533 5.6425 8.2514 8.2544 38 22 5.0553 86281 5.2051 8.5385 5.53534 8.4464 5.4999 8.3517 5.6449 8.2544 38 23 5.0578 8.0266 5.2076 8.5370 5.3558 8.4448 5.5024 8.3501 5.6473 8.2524 3.2525 5.3535 8.4483 5.5048 8.3465 5.6407 8.25141 8.2525 5.5028 8.0897 5.2101 8.5355 5.3585 8.4433 5.5048 8.3465 5.6407 8.2513 36 25 5.0028 8.0267 5.2101 8.5355 5.3585 8.4433 5.5048 8.3465 5.6407 8.2513 36 25 5.0028 8.0267 5.2101 8.3525 5.3532 8.4402 5.5007 8.3433 5.6545 8.2514 8.2325 5.3532 8.4402 5.5007 8.3433 5.6545 8.2515 8.2525 8.3525 8.3523 8.4402 5.5007 8.3433 5.6545 8.2245 8.2525 8.2527 5.5370 8.3370 5.5145 8.3421 5.6563 8.2446 39 5.05704 8.010 8.2525 8.5257 5.5370 8.3370 5.5145 8.3421 5.6563 8.2442 31 30 5.0764 8.0163 5.2225 8.5279 5.5370 8.3355 5.5149 8.3405 5.66617 8.2429 31 30 5.0763 8.0163 5.2225 8.5279 5.5370 8.3355 5.5048 8.3355 5.6064 8.222 3.250 8.5244 5.53730 8.4339 5.5144 8.3389 5.6644 8.2413 30 31 5.0779 8.0185 5.2225 8.5275 5.5370 8.3355 5.5149 8.3401 5.65633 8.2446 3.334 5.0764 8.0163 5.2225 8.5275 8.5370 8.3350 8.3444 5.5319 8.3356 5.6668 8.2300 8.2340 8.5074 8.0085 8.0085 8.0085 8.2446 3.3361 8.3429 5.55169 8.3404 5.6661 8.2225 8.2236 8.2541 8.2543 5.5066 8.3340 5.56713 8.2363 9.254 8.2545 8.2545 8.2508 8.2547 8.5308 8.3245 5.55169 8.3404 5.56617 8.2249 8.2545 8.254	1			.51877 .8	5491	.53361			.83629	.56280	.82659	
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21		19	.50478 .86325	.51977 .8	35431	.53460	.84511	.54927	.83565	.56377	.82593	41
22 50553 80281 52051 85385 53538 84484 55024 83501 56449 8254 88 23 50578 80206 52076 85370 53558 84484 55024 83501 56473 82528 37 24 50603 80251 52101 85355 53588 84483 55024 83501 56473 82528 37 25 50028 80237 52151 85355 53538 84437 55002 83469 56521 82495 32 26 50654 80222 525151 85325 53532 84402 55097 83439 56521 82495 32 27 50079 80307 52175 85310 53056 84186 55121 83437 56569 82462 33 28 50704 86192 52200 85294 53681 84370 55145 83421 56593 8246 32 29 50729 80178 52225 85279 53705 84355 55149 83405 56617 82429 31 30 50754 80163 52225 85279 53705 84355 55109 83405 56617 82429 31 30 50754 80163 52225 85249 53754 84324 55218 83373 56664 8248 32 22 50804 86133 52290 85234 53770 84306 55242 83356 56685 82360 29 23 50804 86133 52290 85234 53770 84306 55242 83356 56685 82360 29 24 50804 80133 52299 85234 53779 84306 55242 83356 56668 82360 29 25 50804 8613 52349 85930 55385 84277 55291 83340 56763 82340 234 55736 84324 55209 8234 56736 82340 256713 82362 23 25 50804 8613 52349 85030 55385 84277 55291 8334 56736 82347 26 35 50879 80809 52374 85188 55385 84277 55291 8334 56736 82347 26 35 50809 86019 52349 85030 55385 84277 55291 8334 56736 82347 26 35 50809 86019 52349 85173 553877 84245 55330 83292 56784 8234 24 37 50929 86059 52423 85157 53902 84230 55363 83276 55808 82247 26 38 50944 8045 52448 85142 53926 8414 55389 8320 56760 8230 25 38 50909 86000 52423 85157 53902 84230 55363 83276 55808 82241 24 37 50929 86005 52423 85112 53975 84182 55496 83223 56984 82241 24 37 5109 88907 52473 85112 53975 84182 55496 83212 56904 82231 19 44 51104 88965 52474 85081 54094 84135 55590 83179 56952 82194 14 51029 86000 52423 85112 53975 84182 55406 83223 56980 82248 20 41 51034 88936 55247 85081 54094 84135 55590 83179 56952 82194 14 4 51104 88966 52474 85085 54404 84518 55496 83024 57688 82241 19 4 51129 85941 52621 85035 54094 84135 55509 83096 57074 82115 12 4 51129 85941 52621 85035 54096 84097 55664 83082 57074 82115 12 5 513194 88866 52745 84959 54220 84025 55664 83085 57074 82115 12 5 513194 88866 52745 84959 54220	1	20	.50503 .86310	.52002 .8	35416	.53484	.84495	.54951	.83549	.56401	.82577	40
23 50578 80296 52074 8550 53558 84448 55048 83485 56497 8219 35 24 50003 80251 52101 85355 53588 84493 55048 83485 56497 8219 35 25 50028 80237 52126 85340 53607 84417 55072 83469 56521 82495 35 26 50634 80222 52151 85325 53585 84402 55097 83453 56545 82478 32 27 50679 80207 52175 85310 53555 81386 55121 83437 56569 82462 33 28 50704 86102 52200 85294 53685 84386 55121 83437 56569 82462 33 29 50729 86178 52225 85279 53705 84350 55124 83421 56593 82446 33 30 50754 86163 52225 8527 53705 84350 55169 83405 56617 82429 31 30 50754 86163 52225 8527 53705 84350 55169 83405 56617 82429 31 30 50754 86163 52225 8529 53705 84350 55169 83405 56617 82429 31 30 50754 86163 52225 85249 53705 84350 55104 83389 56641 82413 30 31 50779 86148 52225 85249 53757 84308 55242 8336 56689 82380 28 32 50804 86133 52290 85234 53779 84308 55242 8336 56689 82380 28 33 50829 86119 52349 85203 53828 84277 55291 83324 56736 82302 25 34 50854 86104 52349 85203 53828 84277 55291 83324 56736 82302 25 36 50879 86089 52374 85188 53855 84261 55330 83292 56784 82314 27 35 50879 86089 52423 85157 53902 84230 55366 83276 56898 82297 23 38 509079 86030 52423 85157 53902 84230 55366 83276 56898 82297 23 38 509079 86030 52423 85157 53902 84230 55366 83276 56898 82297 23 38 509079 86030 52423 85157 53902 84230 55366 83276 56898 82297 23 38 509079 86030 52423 85112 53975 84182 55496 83212 56904 82231 19 40 51004 86015 52498 85112 53975 84182 55496 83212 56904 82231 19 42 51044 85966 52478 85061 54004 84167 55460 83212 56904 82231 19 43 51079 85970 52572 85066 54009 84167 55460 83212 56904 82231 19 44 51104 88966 52572 85066 54009 84167 55460 83212 56904 82231 19 45 51129 85041 55621 85005 54446 84051 55567 83177 57024 82148 18 45 51129 85066 52248 85112 53975 84182 55560 83179 56052 82198 17 44 51104 88966 52572 85066 54009 84167 55460 83212 56004 82231 19 50 51224 85866 52574 85081 54074 84151 55544 83195 56098 82248 20 51 51304 85866 52574 84989 54420 84585 55564 83098 57071 82115 12 50 51234 85866 52574 84989 54420 84088 55564 83098 57071 82115 12 55 5												
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28 50704 86192 5220 85294 53681 84370 55145 83421 56693 82446 39 507529 86178 52225 85270 53705 84355 55169 83465 56617 82429 31 30 50754 86163 52250 85264 53730 84330 55194 83389 56641 82413 30 31 50779 86148 52250 85246 53730 84330 55194 83389 56641 82413 30 32 50804 86133 52290 85234 53773 84308 55194 83389 56641 82413 30 32 50804 86133 52290 85234 53773 84308 55242 8353 56665 82396 28 33 50829 86119 52324 83218 53804 84292 55266 83340 56736 82396 28 35 50879 86089 52374 85188 53853 84261 55315 83938 56766 82390 22 53566 85004 86133 55807 86089 52374 85188 53853 84261 55315 83938 56766 82390 25 53 50879 86089 52374 85188 53853 84261 55315 83938 56766 82390 25 53 50879 86089 52374 85185 53535 84261 55315 83938 56766 82390 25 53 50879 86089 52374 85157 53902 84230 55315 83938 56766 82390 25 53 50879 86089 52423 85157 53902 84230 55363 83276 55608 82297 23 38 50079 86030 52423 85157 53902 84230 55363 83276 55608 82297 23 39 50079 86030 52423 85157 53902 84230 55363 83276 55608 82297 23 40 51004 86015 52448 85112 53926 84124 55388 83200 56882 82284 20 40 51004 86015 52448 85112 53975 84188 55442 83244 56856 82264 20 40 51004 86015 52448 85112 53975 84188 55442 83244 56856 82264 20 42 51054 85985 52547 85081 54024 84151 55444 83195 56928 82248 20 44 551129 85944 55621 850355 54097 84135 55509 83179 56052 82198 17 44 51104 85956 52572 85066 54004 84135 55509 83179 56052 82198 17 44 51104 85966 52597 85051 54073 84120 55533 83163 56976 82181 19 44 51104 85966 52597 85051 54073 84120 55533 83163 56976 82181 10 50 51224 85866 52454 84989 54414 84029 55563 8304 57074 82132 13 48 51294 85866 52456 84989 54171 84057 55664 83062 57098 82181 10 50 51224 85866 52456 84989 54171 84057 55664 83062 57098 82181 10 50 51224 85866 52456 84989 54171 84057 55664 83062 57098 82181 10 50 51224 85866 52456 84989 54171 84057 55664 83066 5771 82132 13 55671 83096 55708 83077 57191 82082 10 55551 83131 57074 82132 13 55671 83096 55708 83076 5771 82132 13 55671 83096 55708 83076 5771 82132 13 55671 83096 55745 84989 55868 84889 55868 839	1	26		.52151 .8	35325			.55097		.56545		
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36 5.9094 80079 . 52399 8.5173 5.5877 8.8245 5.5330 8.3292 5.6764 8.2314 24 37 5.0929 80059 .52323 8.5157 5.5302 8.4230 5.5363 8.3276 5.6808 8.2297 23 38 5.0954 80045 5.2448 8.5124 5.7352 8.414 5.5388 8.3290 5.6832 8.2297 23 39 5.0979 80030 5.2473 8.5127 5.3951 8.4198 5.5442 8.3244 5.6856 8.2297 23 39 5.0979 80030 5.2473 8.5127 5.3951 8.4198 5.5442 8.3244 5.6856 8.2248 20 41 5.1029 80000 5.52498 8.5112 5.3975 8.4183 5.5436 8.3228 5.6882 8.2248 21 42 5.1054 8.5985 5.5247 8.5086 5.4000 8.4167 5.5460 8.3212 5.6904 8.2248 20 42 5.1054 8.5985 5.5247 8.5081 5.4024 8.4151 5.5448 8.3195 5.6928 8.2214 18 4.51024 8.5985 5.2527 8.5066 5.4049 8.4135 5.5509 8.3179 5.69528 8.2214 18 4.51129 8.5041 5.5249 8.5051 5.54073 8.4120 5.5538 8.3163 5.69678 8.2181 16 4.51129 8.5041 5.5264 8.5035 5.4097 8.4104 5.5557 8.3147 5.7000 8.2165 15 4.6 5.1154 8.5926 5.5646 8.5020 5.4122 8.4088 5.5581 8.3131 5.7024 8.2148 14 5.1129 8.5061 5.54078 8.4000 5.54122 8.4088 5.5581 8.3131 5.7024 8.2148 14 5.1129 8.5066 5.2408 8.4085 5.5407 8.4104 5.5557 8.3147 5.7000 8.2165 15 4.6 5.1154 8.5926 5.5646 8.5020 5.4122 8.4088 5.55605 8.3115 5.7047 8.2132 13 4.8 5.1204 8.5866 5.2208 8.4989 5.4127 8.4057 5.5660 8.3088 5.57071 8.2132 13 4.9 5.1223 8.5881 5.52720 8.4974 5.4195 8.4045 5.5664 8.3082 5.7076 8.2088 10 5.1254 8.5866 5.2745 8.4959 5.4220 8.4025 5.5678 8.3066 5.7119 8.2082 10 5.51254 8.5866 5.2745 8.4959 5.4220 8.4025 5.5678 8.3066 5.7119 8.2082 10 5.51254 8.5866 5.2745 8.4958 5.4220 8.4025 5.5678 8.3066 5.7119 8.2082 10 5.51254 8.5866 5.2745 8.4958 5.4220 8.4025 5.5678 8.3066 5.7119 8.2082 10 5.51254 8.5866 5.2745 8.4958 5.4220 8.4025 5.5678 8.3066 5.7119 8.2082 10 5.51254 8.5866 5.2745 8.4958 5.4220 8.4025 5.5678 8.3066 5.7119 8.2082 10 5.51254 8.5866 5.2745 8.4958 5.4220 8.4025 5.5678 8.3066 5.7119 8.2082 10 5.51254 8.5866 5.2745 8.4958 5.4220 8.4025 5.5678 8.3066 5.7119 8.2082 10 5.51254 8.5866 5.2745 8.4958 5.4220 8.4025 5.5678 8.3066 5.7119 8.2082 10 5.5124 8.5866 5.2744 8.4868 5.5448 8.4867 5.55798 8.3098 5.5738 8.3098 5.5748 8.3098 5.5748 8.		32	.50804 .86133	.52299 .8	35234	.53779	.84308	.55242	.83356	.56689	.82380	28
36 5.9094 80079 . 52399 8.5173 5.5877 8.8245 5.5330 8.3292 5.6764 8.2314 24 37 5.0929 80059 .52323 8.5157 5.5302 8.4230 5.5363 8.3276 5.6808 8.2297 23 38 5.0954 80045 5.2448 8.5124 5.7352 8.414 5.5388 8.3290 5.6832 8.2297 23 39 5.0979 80030 5.2473 8.5127 5.3951 8.4198 5.5442 8.3244 5.6856 8.2297 23 39 5.0979 80030 5.2473 8.5127 5.3951 8.4198 5.5442 8.3244 5.6856 8.2248 20 41 5.1029 80000 5.52498 8.5112 5.3975 8.4183 5.5436 8.3228 5.6882 8.2248 21 42 5.1054 8.5985 5.5247 8.5086 5.4000 8.4167 5.5460 8.3212 5.6904 8.2248 20 42 5.1054 8.5985 5.5247 8.5081 5.4024 8.4151 5.5448 8.3195 5.6928 8.2214 18 4.51024 8.5985 5.2527 8.5066 5.4049 8.4135 5.5509 8.3179 5.69528 8.2214 18 4.51129 8.5041 5.5249 8.5051 5.54073 8.4120 5.5538 8.3163 5.69678 8.2181 16 4.51129 8.5041 5.5264 8.5035 5.4097 8.4104 5.5557 8.3147 5.7000 8.2165 15 4.6 5.1154 8.5926 5.5646 8.5020 5.4122 8.4088 5.5581 8.3131 5.7024 8.2148 14 5.1129 8.5061 5.54078 8.4000 5.54122 8.4088 5.5581 8.3131 5.7024 8.2148 14 5.1129 8.5066 5.2408 8.4085 5.5407 8.4104 5.5557 8.3147 5.7000 8.2165 15 4.6 5.1154 8.5926 5.5646 8.5020 5.4122 8.4088 5.55605 8.3115 5.7047 8.2132 13 4.8 5.1204 8.5866 5.2208 8.4989 5.4127 8.4057 5.5660 8.3088 5.57071 8.2132 13 4.9 5.1223 8.5881 5.52720 8.4974 5.4195 8.4045 5.5664 8.3082 5.7076 8.2088 10 5.1254 8.5866 5.2745 8.4959 5.4220 8.4025 5.5678 8.3066 5.7119 8.2082 10 5.51254 8.5866 5.2745 8.4959 5.4220 8.4025 5.5678 8.3066 5.7119 8.2082 10 5.51254 8.5866 5.2745 8.4958 5.4220 8.4025 5.5678 8.3066 5.7119 8.2082 10 5.51254 8.5866 5.2745 8.4958 5.4220 8.4025 5.5678 8.3066 5.7119 8.2082 10 5.51254 8.5866 5.2745 8.4958 5.4220 8.4025 5.5678 8.3066 5.7119 8.2082 10 5.51254 8.5866 5.2745 8.4958 5.4220 8.4025 5.5678 8.3066 5.7119 8.2082 10 5.51254 8.5866 5.2745 8.4958 5.4220 8.4025 5.5678 8.3066 5.7119 8.2082 10 5.51254 8.5866 5.2745 8.4958 5.4220 8.4025 5.5678 8.3066 5.7119 8.2082 10 5.51254 8.5866 5.2745 8.4958 5.4220 8.4025 5.5678 8.3066 5.7119 8.2082 10 5.5124 8.5866 5.2744 8.4868 5.5448 8.4867 5.55798 8.3098 5.5738 8.3098 5.5748 8.3098 5.5748 8.				.52324 .8	35218			.55266	.83340	.56713		27
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41 .51029 .86000 .52522 .85066 .54000 .84167 .55460 .83212 .56904 .82231 19 42 .51054 .85985 .52547 .85081 .54024 .84151 .55484 .83195 .56928 .82214 18 43 .51079 .85970 .52572 .85066 .54049 .84135 .55500 .83179 .56952 .82181 16 44 .51104 .85956 .52527 .85051 .54073 .84120 .55533 .83163 .56976 .82181 16 45 .51129 .85041 .52621 .85035 .54097 .84104 .55557 .83147 .57000 .82165 16 46 .51154 .85956 .52646 .85020 .544122 .84088 .55581 .83131 .57024 .82148 14 47 .51179 .85911 .58671 .85005 .54146 .84072 .55605 .83115 .57047 .82148 14 48 .51204 .85896 .52696 .84989 .54171 .84057 .55605 .83115 .57047 .82132 13 48 .51229 .88581 .52720 .84974 .54195 .84041 .55664 .83062 .57095 .82098 11 50 .51254 .85866 .52745 .84959 .54220 .84025 .55678 .83066 .57119 .82082 10 51 .51279 .85851 .52770 .84943 .54244 .84009 .55702 .83050 .57143 .80082 .57055 .52046 .84988 .54269 .83994 .55726 .83034 .57167 .82048 .53 53 .51329 .85821 .52819 .84913 .54234 .84009 .55702 .83050 .57143 .8006 .58046 .5	H											
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43 5.1079 8.9070 5.2572 85066 5.4049 8.4135 5.5500 8.9179 5.6052 8.2198 17 44 5.1149 8.5941 5.2521 8.5035 5.4073 8.4120 5.5533 8.3163 5.6976 8.2181 16 45 5.1139 8.5041 5.2621 8.5035 5.4097 8.4104 5.5557 8.3147 5.7002 8.2165 15 46 5.1154 8.5926 5.2646 8.5020 5.4142 8.4088 5.5561 8.3131 5.7024 8.2182 13 47 5.1179 8.5911 5.2671 8.5005 5.4146 8.4072 5.5605 8.3131 5.7024 8.2182 13 48 5.1204 8.5896 5.2666 8.4089 5.4171 8.4057 5.5663 8.3088 5.7071 8.2132 13 49 5.1229 8.5881 5.2720 8.4974 5.4195 8.1041 5.5654 8.3082 5.7071 8.2115 12 50 5.1254 8.5866 5.2745 8.4959 5.4220 8.4025 5.5648 8.3066 5.7113 8.2082 10 51 5.1279 8.8561 5.2770 8.4943 5.4244 8.4009 5.5702 8.3080 5.7143 8.2062 10 52 5.1304 8.5836 5.2794 8.4928 5.4269 8.3094 5.5726 8.3034 5.7167 8.2082 10 53 5.1329 8.5821 5.2819 8.4913 5.4238 8.3978 5.5726 8.3034 5.7167 8.2048 8.55 5.51379 8.5928 5.5669 8.3048 5.7167 8.2082 7 54 5.1344 8.5806 5.2544 8.4827 5.4317 8.3966 5.5739 8.3965 5.7232 8.3999 5.5555 5.51379 8.5795 5.2690 8.4882 5.4442 8.3946 5.5739 8.3965 5.7232 8.3999 5 55 5.1379 8.5792 5.2690 8.4882 5.4442 8.3946 5.5829 8.3995 5.7232 8.1999 5 56 5.1404 8.5777 5.2593 8.4866 5.4366 8.3930 5.5823 8.2969 5.7322 8.1982 4 57 5.5149 8.5762 6.2518 8.4831 5.4249 8.3916 5.5823 8.2996 5.7338 8.1999 5 58 5.1454 8.5747 5.2923 8.4880 5.4446 8.8885 5.5895 8.2920 5.7334 8.1932 7 60 5.5154 8.5747 5.2924 8.4820 5.4446 8.8885 5.5895 8.2920 5.7334 8.1932 7 60 5.5154 8.5747 5.2922 8.4885 5.4446 8.8885 5.5895 8.2920 5.7334 8.1932 7 60 5.5154 8.5747 5.2922 8.4885 5.4446 8.8885 5.5895 8.2920 5.7334 8.1935 0 60 5.5154 8.5747 5.2922 8.4885 5.4446 8.8885 5.5895 8.2920 5.7334 8.1935 0 60 5.5154 8.5747 5.2922 8.4885 5.4446 8.8885 5.5895 8.2920 5.7334 8.1935 0 60 5.5154 8.5747 5.2922 8.4885 5.4446 8.8885 5.5895 8.2920 5.7334 8.1935 0 60 5.5154 8.5747 5.2922 8.4885 5.4446 8.8885 5.5895 8.2920 5.7334 8.1935 0 60 5.5154 8.5747 5.2922 8.4885 5.4446 8.8885 5.5895 8.2920 5.7334 8.1935 0 60 5.5154 8.5747 5.2922 8.4885 5.4446 8.8885 5.5895 8.2920 5.7334 8.1935 0 60 5.5154 8.5747 5.2922 8.4885 5.444	1		.51054 .85985				.84151			.56928		
44 .51104 .85956 .52957 .85051 .54073 .84120 .5533 .83163 .56976 .82181 54 45 .511529 .85041 .55281 .85085 .54097 .84104 .55557 .83147 .57000 .8216 56 46 .51154 .85926 .52646 .85020 .54122 .84088 .55551 .83131 .57024 .82148 14 47 .51179 .85911 .52671 .85005 .54146 .84072 .55605 .83115 .57047 .82132 13 48 .51294 .85896 .52696 .84989 .54471 .84057 .55609 .8308 .57071 .82115 12 49 .51229 .85881 .52720 .84974 .54195 .84041 .55654 .83082 .57095 .82088 11 50 .51254 .85866 .52745 .84959 .54220 .84025 .55678 .83066 .57119 .82082 10 51 .51297 .85851 .52770 .84943 .54244 .84009 .55702 .83050 .57143 .82065 10 52 .51304 .85886 .52744 .84928 .54259 .83994 .55726 .83034 .57167 .82048 8 53 .51329 .85821 .52819 .84913 .54293 .83978 .55706 .83034 .57167 .82048 8 53 .51329 .85821 .52819 .84913 .54293 .83978 .55750 .83017 .57191 .82082 10 54 .51354 .85806 .52444 .84897 .54317 .83962 .55775 .8301 .57215 .82015 6 55 .51379 .85792 .52869 .84882 .54342 .83946 .55729 .82985 .57238 .81999 5 56 .51404 .85777 .52893 .84866 .54366 .83830 .55823 .82999 .57262 .81982 4 57 .51429 .85762 .52918 .84851 .54391 .83915 .55823 .82993 .57262 .81982 4 58 .51454 .85747 .52943 .84866 .54464 .83887 .55817 .83993 .55821 .55823 .57262 .81982 4 59 .51479 .85732 .52967 .84820 .54440 .83883 .55823 .82993 .57361 .81949 2 59 .51479 .85732 .52967 .84820 .54446 .83883 .55895 .82920 .57334 .81932 6 515544 .85717 .52992 .84805 .54446 .83885 .55895 .82904 .57358 .81915 0 50 .51504 .85717 .52992 .84805 .54446 .83885 .5599 .53904 .57358 .81915 0 50 .51504 .85717 .52992 .84805 .54446 .83885 .5599 .55904 .57358 .81915 0 50 .51504 .85717 .52992 .84805 .54446 .83885 .5599 .55904 .57358 .81915 0 50 .51504 .85717 .52992 .84805 .54446 .83885 .5599 .55904 .57358 .81915 0 50 .51504 .85717 .52992 .84805 .54446 .83885 .5599 .55904 .57358 .81915 0 50 .51504 .85717 .52992 .84805 .54446 .83865 .55919 .83904 .57358 .81915 0 50 .51504 .85717 .52992 .84805 .54446 .83885 .5599 .55904 .57358 .81915 0 50 .51504 .85717 .52992 .84805 .54446 .83865 .55919 .53904 .57358 .81915 0		43	.51079 .85970	.52572 .8	35066	.54049	.84135	.55509	.83179	.56952	.82198	17
46 .51154 .85926 .52946 .85020 .54122 .84088 .55581 .83131 .57024 .82148 .14 47 .51179 .85911 .52671 .85005 .54146 .84072 .55605 .83115 .57047 .82135 .12 48 .51204 .85896 .52966 .84989 .54171 .84057 .55620 .83088 .57071 .82115 .12 49 .51229 .85881 .52720 .84974 .54195 .84041 .55624 .83082 .57095 .82098 .11 50 .51254 .85866 .52745 .84959 .54220 .84025 .55678 .83066 .57119 .82082 .10 51 .51279 .85851 .52770 .84943 .54244 .84009 .55702 .83050 .57143 .82065 .9 52 .51304 .85836 .52794 .84928 .54269 .83994 .55726 .83034 .57167 .82048 .8 53 .51329 .85821 .52819 .84913 .54293 .83978 .55726 .83034 .57167 .82048 .8 53 .51329 .85821 .52819 .84913 .54293 .83978 .55726 .83034 .57167 .82048 .8 54 .51354 .85806 .52844 .84897 .54317 .83962 .55775 .8301 .57215 .82015 .6 55 .51379 .85792 .52869 .84882 .54342 .83946 .55799 .82985 .57238 .81999 .5 56 .51404 .85777 .52933 .84866 .54366 .83930 .55823 .82999 .57262 .81982 .5 57 .51429 .85762 .52318 .84851 .54391 .83915 .55823 .83999 .57262 .81982 .5 58 .51454 .85747 .52943 .84850 .54440 .83883 .55847 .82935 .57360 .81962 .3 58 .51454 .85717 .52992 .84805 .54446 .83867 .55919 .82904 .57334 .81932 . Cosin Sine Cosin Sine Cosin Sine Cosin Sine Cosin Sine						.54073	.84120	.55533				
48 . 51179 . 85911 . 58671 . 85005 . 54146 . 84072 . 55605 . 83115 . 57047 . 82132 13 48 . 51204 . 85896 . 52696 . 84989 . 54171 . 84057 . 55630 . 83008 . 57071 . 82151 23 . 51229 . 85881 . 52720 . 84974 . 54195 . 84041 . 55664 . 83082 . 57095 . 82098 . 11 50 . 51229 . 85881 . 52720 . 84974 . 54195 . 84042 . 55664 . 83082 . 57095 . 82098 . 11 50 . 51254 . 85866 . 52745 . 84959 . 54220 . 84025 . 55678 . 83066 . 57119 . 82082 . 10 . 51279 . 85881 . 52770 . 84943 . 54244 . 84000 . 55702 . 83050 . 57143 . 82065 . 52 . 51304 . 85836 . 52794 . 84928 . 54269 . 83994 . 55726 . 83034 . 57147 . 82048 . 853 . 51329 . 88821 . 52819 . 84913 . 54293 . 83978 . 55726 . 83034 . 57147 . 82048 . 853 . 51329 . 85821 . 52819 . 84913 . 54293 . 83978 . 55775 . 83001 . 57215 . 82015 . 55 . 51379 . 85799 . 52869 . 84882 . 54342 . 83946 . 55779 . 83995 . 57238 . 81999 . 55 . 51479 . 85777 . 52893 . 84866 . 54366 . 83930 . 55823 . 82969 . 57262 . 81982 . 57 . 51429 . 85762 . 52918 . 84851 . 54491 . 83915 . 55847 . 82935 . 57266 . 81965 . 358 . 51454 . 85747 . 52943 . 84856 . 54415 . 88899 . 55871 . 82936 . 57310 . 81949 . 2 . 51504 . 85717 . 52992 . 84805 . 54446 . 83887 . 55919 . \$2904 . 57358 . 81915 . 0 . 51504 . 85717 . 52922 . 84805 . 54446 . 83887 . 55919 . \$2904 . 57358 . 81915 . 0 . 51504 . 85717 . 52922 . 84805 . 54446 . 83867 . 55919 . \$2904 . 57358 . 81915 . 0 . 50510				.52646			84088		83147	57000	82148	
48 5.51204 88896 52766 84989 5.54171 84057 55639 83008 5.7071 82115 1249 5.51229 83881 52720 84974 5.54195 84041 5.5654 83928 5.7071 82115 1250 5.51254 85866 5.2745 84959 5.54220 84025 5.5654 83928 5.7095 82098 11 50 51254 85866 5.2745 84959 5.54220 84025 5.5654 83926 5.7119 82082 10 51 5.51279 88851 5.2770 84943 5.54244 84009 5.5709 83050 5.7143 82065 9 52 5.51304 8.8893 5.2704 8.4928 5.4259 83994 5.5726 83034 5.7167 82048 85 5.51329 85821 5.2819 84913 5.54239 83978 5.5726 83034 5.7167 82032 7 54 5.51379 85795 5.2569 84882 5.54432 83946 5.5739 82985 5.7238 81999 5 55 5.51379 85795 5.2869 84882 5.54432 83946 5.5739 82985 5.7238 81999 5 56 5.51404 85777 5.5293 84866 5.4366 83930 5.5823 82965 5.7232 81982 4 57 5.5149 85765 5.82015 6.5218 84851 5.4231 83915 5.5847 82935 5.7232 81982 4 57 5.5149 85762 5.2918 84836 5.54446 88867 5.5847 82936 5.7351 81949 2 5.54479 88753 5.2928 84880 5.54446 88867 5.5919 82904 5.7351 81949 2 5.54479 88753 5.2928 84880 5.54446 88867 5.5919 82904 5.7358 81915 0 50 50 50 50 50 50 50 50 50 50 50 50		47	.51179 .85911	.52671 .8	35005		.84072		,83115			13
50 .51254 .85866 .52745 .84959 .54220 .84025 .55678 .89066 .57119 .82082 10 51 .51279 .85851 .52770 .84943 .54244 .84009 .55702 .83050 .57143 .82065 9 52 .51304 .85836 .52794 .84928 .54269 .83994 .55726 .83034 .57167 .82048 8 53 .51329 .85821 .52819 .84913 .54293 .83978 .55726 .83041 .57171 .82048 8 54 .51334 .88060 .52344 .84887 .54317 .83962 .55775 .83001 .57215 .82015 6 55 .51379 .85792 .52869 .84882 .54442 .83946 .55739 .82985 .57238 .81999 .5 56 .51404 .85777 .52953 .84866 .54366 .83930 .55823 .82969 .57202 .81982 4 57 .51429 .85762 .52918 .84851 .54291 .83915 .55847 .82935 .57286 .81965 3 58 .51454 .85747 .52943 .84836 .54415 .83869 .55823 .82960 .57310 .81949 2 59 .51504 .85732 .52967 .84820 .54440 .83867 .55919 .82904 .57358 .81915 0 60 .51504 .85717 .52992 .84805 .54446 .83867 .55919 .82904 .57358 .81915 0 60 .51504 .85717 .52992 .84805 .54446 .83867 .55919 .82904 .57358 .81915 0 60 .51504 .85717 .52992 .84805 .54446 .83867 .55919 .82904 .57358 .81915 0 60 .51504 .85717 .52992 .84805 .54446 .83867 .55919 .82904 .57358 .81915 0			.51204 .85896	.52696 .8	34989	.54171	.84057	.55630	.83098	.57071	.82115	12
51 .51279 .85851 .52770 .84943 .54244 .84009 .55702 .83050 .57143 .82065 9 52 .51304 .88836 .52794 .84928 .54269 .83994 .55750 .83044 .57167 .82048 8 54 .51324 .85800 .52844 .84987 .54317 .83962 .55775 .83011 .57191 .82032 7 54 .51334 .85800 .52844 .84897 .54317 .83962 .55775 .83011 .57215 .82015 6 55 .51379 .88792 .52869 .84882 .54442 .83946 .55799 .82985 .57238 .81999 5 56 .51429 .88762 .52918 .84851 .54391 .83915 .58247 .82963 .57262 .81965 3 58 .51434 .85747 .52943 .84856 .54415 .83899 .55871 .82933 .57286 <td< th=""><th></th><th></th><th></th><th></th><th></th><th></th><th>.81041</th><th></th><th></th><th>.57095</th><th></th><th></th></td<>							.81041			.57095		
52	۱					1000		The same of the		A	The same of the	
53 51329 88821 58819 84013 54923 83978 55775 83017 57191 82032 7 54 51354 85806 52844 84897 54317 83962 55775 83011 57215 82015 6 55 51379 85792 52869 84882 54342 83946 55799 82985 57238 81999 5 56 51404 85777 52933 84866 54366 83930 55823 82969 57202 81982 4 57 51429 85762 52918 84851 54391 83915 55847 82935 57262 81982 4 58 51454 85747 52943 84836 54415 83899 55871 82936 57310 81949 2 59 51504 85717 52992 84805 54446 83867 55919 82904 57358 81915 0 Cosin Sine Cosin Sine Cosin Sine Cosin Sine				52704								9
54 .51354 .88906 .52844 .84897 .54317 .83962 .55779 .83001 .57215 .82015 6 55 .51379 .85792 .52869 .84882 .54342 .83946 .55799 .82985 .57238 .81999 5 56 .51404 .85777 .52933 .84866 .54366 .83930 .55823 .82969 .57238 .81982 4 57 .51429 .85762 .52948 .84851 .54391 .83915 .55871 .82953 .57366 .81965 3 59 .51479 .85732 .52907 .84805 .54446 .83887 .55895 .82902 .57334 .81932 1 60 .51504 .85717 .52992 .84805 .54464 .83867 .55919 .82904 .57358 .81915 0 Cosin Sine Cosin Sine Cosin Sine Cosin Sine		53	.51329 .85821		84913					.57191		7
55 .51373 .85792 .52809 .84882 .54342 .83946 .55739 .82965 .57238 .81999 5 55 .51404 .85777 .52893 .84866 .54366 .83930 .55823 .82969 .57262 .81982 4 57 .51429 .85762 .52918 .84851 .54291 .83915 .53847 .82953 .57286 .81965 3 .586747 .85732 .52918 .84856 .54415 .83899 .55871 .82936 .57310 .81949 2 .59 .51479 .85732 .52907 .84820 .54440 .83883 .55895 .82902 .57334 .81932 1 .60 .51504 .85717 .52992 .84805 .54464 .83867 .55919 .82904 .57358 .81915 0 .75919			.51354 .85806	.52844 .8	34897	.54317	.83962	.55775	.83001	.57215	.82015	6
57 .51429 .85762 .52918 .84851 .54391 .83915 .55847 .82953 .57286 .81965 3 58 .51454 .85747 .52943 .84836 .54415 .88899 .55871 .82966 .57310 .81949 2 59 .51479 .85732 .32907 .84820 .54440 .83883 .55895 .82902 .57334 .81932 1 60 .51504 .85717 .52992 .84805 .54464 .83867 .55919 .82904 .57358 .81915 0 Cosin Sine Cosin Sine Cosin Sine Cosin Sine	ľ							.55799	.82985	.57238		5
58								55847	82969	57986	81982	3
59 .51479 .85732 .52967 .84820 .54440 .83883 .55895 .82920 .57334 .81932 1 60 .51504 .85717 .52992 .84805 .54464 .83867 .55919 .82920 .57358 .81915 0 Cosin Sine Cosin Sine Cosin Sine Cosin Sine Cosin Sine		58	.51454 .85747	.52943 .8	34836	.54415	.83899	.55871	.82936	.57310		2
Cosin Sine Cosin Sine Cosin Sine Cosin Sine Cosin Sine			.51479 .85732	.52967 .8	34820	.54440	.83883	.55895	.82920	.57334	.81932	1
, and a second s		00		-	THE RESIDENCE	-	A STATE OF THE PARTY NAMED IN		-	-	1	0
59° 58° 57° 56° 55°		,				Cosin	Sine	Cosin	Sine	Cosin	Sine	,
			59°	58°		5'	70	5	6°	5	50	

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	,	-	5°	-	6°	3'	7°	3	8°	39	9°	,
1		Sine	Cosin	Sine	Cosin	Sine	Cosin	Sine	Cosin	Sine	Cosin	
1	0	.57358	.81915	.58779	.80902	.60182	.79864	.61566	.78801	.62932	.77715	60
183	1	.57381	.81899 .81882	.58802	.80885	.60205	.79846	.61589	.78783	.62955	.77696	59
10	2 3	.57429	.81865	.58849	.80850	.60251	.79811	.61612	.78747	.63000	.77678	58 57
	4	.57453	.81848	.58873	.80833	.60274	.79793	.61658	.78729	.63022	.77641	56
-	5	.57477	.81832	.58896	.80816	.60298	.79776	.61681	.78711	.63045	.77623	55
	6 7	.57501 .57524	.81815	.58920	.80799	.60321	.79758	.61704	.78694	.63068	.77605	54
	8	.57548	.81782	.58967	.80765	.60367	.79741	.61726 .61749	.78676	.63090	.77586	53 52
	9	.57572	.81765	.58990	.80748	.60390	.79706	.61772	.78640	.63135	.77550	51
0	10	.57596	.81748	.59014	.80730	.60414	.79688	.61795	.78622	.63158		50
	11	.57619	.81731	.59037	.80713	.60437	.79671	.61818	.78604	.63180	.77513	40
1	12	.57643	.81714	.59061	.80696	.60460	.79653	.61841	.78586	.63203		48
	13 14	.57667	.81698 .81681	.59084	.80679 .80662	.60483	.79635 .79618	.61864	.78568 .78550	.63225	.77476	47
	15	.57715	.81664	.59131	.80644	.60529	79600	.61909	.78532	.63271	.77439	45
	16	.57738	.81647	.59154	.80627	.60553	.79583	.61932	.78514	.63293	.77421	44
	17	.57762	.81631	.59178	.80610	.60576	.79565	.61955	.78496	.63316	.77402	43
1	18	.57786	.81614 .81597	.59201	.80593	.60599	.79547 .79530	.61978	.78478 .78460	.63338	.77384 .77366	42
	20	.57833	.81580	.59248	.80558	.60645	.79512	.62024	.78442	.63383	.77347	40
	21	.57857	.81563	.59272	.80541	.60668		.62046	.78424	.63406	.77329	39
1 3	22	.57881	.81546	.59295	.80524	.60691	.79477	.62069	.78405	.63428	.77310	38
1 5	23	.57904	.81530	.59318	.80507	.60714	.79459	.62092	.78387	.63451	.77292	37
	24	.57928	.81513	.59342	.80489	.60738	.79441	.62115	.78369	.63473	.77273	36
	25 26 27 28	.57952 .57976	.81496 .81479	.59365	.80472	60761	.79424	.62138	.78351	.63496	.77255	35
13	27	.57999	.81462	.59412	.80438	60807	.79388	.62183	.78315	.63540	.77218	33
1	28	.58023	.81445	.59436	.80420	.60830	.79371	.62206	.78297	.63563	.77199	32
1	29 30	.58047	.81428	.59459	.80403	60853	.79353	.62229	.78279	.63585	.77181	31
1	130	.58070	.81412	.59482	.80386	.60876	.79335	.62251	.78261	.63608	.77162	30
1	81	.58094 .58118	.81395	.59506	.80368	.60899	.79318	.62274	.78243	.63630	.77144	29 28
	52 33	.58141	.81378 .81361	.59529	.80351	.60922	.79300 .79282	.62297	.78225 .78206	.63653	.77125	27
	34	.58165	.81344	.59576	.80316	60968	.79264	.62342	.78188	.63698	.77088	26
	35	.58189	.81327	.59599	.80299	.60991	.79247	.62365	.78170	.63720	.77070	25
	36	.58212 .58236	.81310	.59622	.80282	.61015	.79229 .79211	.62388	.78152	.63742	.77051	24 23
	38	.58260	.81276	.59669	.80264	.61061	79193	.62433	.78116	.63787	.77014	22
1 :	39	.58283	.81259	.59693	.80230	.61084	.79176	.62456	.78098	.63810	.76996	21
1	40	.58307	.81242	.59716	.80212	.61107	.79158	.62479	.78079	.63832	.76977	20
	41	.58330	.81225	.59739	.80195	.61130		.62502	.78061	.63854	.76959	19
1	42	.58354	.81208	.59763	.80178	.61153	.79122	.62524	.78043	.63877	.76940	18
	43 44	.58378	.81191	.59786	.80160	.61176	.79105	.62547	.78025 .78007	.63899	.76921 .76903	17 16
	45	.58425	.81157	.59832	.80125	.61222	.79069	.62592	.77988	.63944	.76884	15
1	46	.58449	.81140	.59856	.80108	.61245	.79051	.62615	.77970	.63966	.76866	14
	47	.58472	.81123	.59879	.80091	.61268	.79033	.62638	.77952	.63989	.76847	13
	48	.58496	.81106	.59902	.80073	.61291	.79016 .78998	.62660	.77934 .77916	.64011	.76828 .76810	12
	50	.58543		.59949		.61337	.78980	.62706	.77897		.76791	10
	51	.58567	.81055	.59972	.80021	.61360	.78962	.62728	.77879	.64078	.76772	9
	52	.58590	.81038	.59995	80003	.61383	.78944	.62751	.77861	.64100	.76754	-8
	53	.58614	.81021	.60019	.79986	.61406	.78926	.62774	.77843	.64123	.76735	8 7 6
	54	.58637	.81004	.60042	.79968 .79951	.61429	.78908 .78891	.62796 .62819	.77824 .77806	.64145	.76698	5
	56	.58684	.80970	.60089	79934	.61474	.78873	.62842	.77788		.76679	4
	57	.58708	.80953	.60112	.79916	.61497	.78855	.62864	.77769	.64212	.76661	3
1	58 59	.58731	.80936	.60135	79899	.61520	.78837	.62887	.77751	.64234	.76642	2
	60	.58755	.80919	.60158	.79881 .79864	.61543	.78819	.62909	.77733	.64256	.76604	0
1	-	Cosin		Cosin	Sine	Cosin	Sine	Cosin		Cosin	place in constant of	-
	,			-			-			-		,
1		5	4°	5	30	52°		5	10	50°		

1	-	4:	00 1	4	10	1 4	20	4:	30	1 4	10	
-	,	-		-		-	-	-				,
-	_	Sine	Cosin	Sine	Cosin	Sine	Cosin	Sine	Cosin	Sine	Cosin	
	0	.64279	.76604	.65606	.75471 .75452	.66913	.74314 .74295	.68200	.73135 .73116	.69466	.71934 .71914	60 59
	1 2	.64301	.76586 .76567	.65628 .65650	75433	.66956	74276	.68242	73096		.71894	58
	3	.64346	76548	.65672	.75414	.66978	.74256	.68264	.73076	.69529	.71873	57
	4	.64368	.76530	.65694	75395	.66999	.74237	.68285	.73056	.69549		
	5	.64390	.76511	.65716	.75375	.67021	.74217	.68306	.73036	.69570	.71833	
	6	.64412	.76492	.65738	06660	.67043	.74198 .74178	.68327	.73016 .72996	.69591	.71813 .71792	
	7 8	.64435	.76473 .76455	.65759	.75337 .75318	67086	.74159	.68370	.72976	.69633	.71772	52
1	9	.64479	.76436	.65803	75299	.67107	.74139	.68391	.72957	.69654	.71752	51
1	10	.64501	.76417	.65825	.75280	.67129	.74120	.68412	.72937	.69675	.71732	50
	11	.64524	.76398	.65847	.75261	.67151	.74100	.68434	.72917	.69696	.71711	49
	12	.64546	.76380	.65869	.75241	.67172	.74080	.68455	.72897	.69717	.71691	48
	13	.64568	.76361	.65891	.75222	.67194	.74061	.68476	.72877	.69737	.71671	47
Н	14	.64590	76342	.65913	.75203	.67215	.74041	.68497	.72857	.69758	.71650 .71630	46
	15 16	.64612	.76323	.65935 .65956	.75184	.67258	.74002	.68539	.72817	69800	71610	
	17	.64657	.76286	.65978	.75146	67280	.73983	.68561	72797	.69821	.71590	43
	18	.64679	.76267	.66000	.75126	.67301	.73963	.68582	.72777 .72757	.69842	.71569	42
	19	.64701	.76248	.66022	.75107	.67323	.73944	.68603	.72757	.69862	.71549	41
	20	.64723	.76229	.66044	.75088	.67344	.73924	.68624	.72737	.69883	.71529	1
1	21	.64746	.76210	.66066	.75069	.67366	.73904	.68645	.72717	.69904	.71508	
1	22	.64768	.76192	.66033	.75050	.67387	.73885	.68666	.72697	.69925	.71488	
H	23 24	.64790	.76173 .76154	.66109	.75030	.67409	.73865	.68688	.72677	.69946	.71468 .71447	37
	25	.64834	.76135	.66153	.74992	.67452	.73826	.68730	72637	.69987	71427	
	26	.64856	.76116	.66175	.74973	.67473	.73806	.68751	.72617	70008	.71407	34
	27	.64878	.76097	.66197	.74953	.67495	.73787	.68772	.72597	.70029	.71386	33
	28	.64901	.76078	.66218	74934	.67516	.737671	.68793	.72577	.70049	.71366	
	29	.64923	.76059	.66240	.74915	.67538	.73747	.68814	.72557 .72537	.70070	.71345	
1	30	.64945	33	.66262	.74896	.67559	.73728	.68835	21.0	.70091	.71325	
1	31	.64967	.76022	.66284	.74876	.67580	.73708	.68857	.72517	.70112	.71305	29
1	32	.64989	.76003 .75984	.66306	.74857 .74838	.67602	.73688 .73669	.68878	.72497 .72477	70132	.71284 .71264	28 27
	34	.65033		.66349	.74818	.67645	.73649	.68920	.72457	.70174	.71243	26
	35	.65055			.74799	.67666	.73629	.68941	.72437	.70195	.71223	35
1	36	.65077	.75927	.66393	.74780	.67688	.73610	.68962	.72417	.70215	.71203	24
	37	.65100	.75908	.66414	.74760	.67709	.73590	.68983	.72397	.70236	.71182	23
1	38	.65122	.75889	.66436	.74741	.67730 .67752	73570	.69004	.72377 .72357	70257	.71162 .71141	22 21
	40	.65166	.75851	.66480	.74703	.67773	.73531	.69046	72337	70298	.71121	20
1	41	.65188	.75832	.66501	.74683	.67795	.73511	.69067	.72317	.70319	.71100	19
1	42	.65210	.75813	.66523	.74664	.67816	.73491	.69088	.72297	.70319	71080	18
	43	:65232	.75794	.66545	.74644	.67837	.73472	.69109	.72277	.70360	.71080 .71059	17
1	44	.65254	.75775	.66566	.74625	.67859	.73452	.69130	.72257	.70381	.71039	16
1	45	.65276	.75756	.66588	.74606	.67880	.73432	.69151	.72236	.70401	.71019	
1	46	.65298	75738	.66632	.74586	67901	.73413	.69172	.72216	.70422	.70998	
	48	.65342	.75719	.66653	.74567	.67923	.73393 .73373	.69193	.72196	.70443	.70978 .70957	13 12
1	49	.65364	.75680	.66675	.74528	67965	.73353	.69235	.72156	.70484		11
1	50	.65386	.75661	.66697	.74509	.67987	.73333	.69256	.72136	.70505	.70916	
1	51	.65408	.75642	.66718	.74489	.68008	.73314	.69277	.72116	.70525	.70896	9
3	52	.65430	.75623	.66740	.74470	.68029	.73294	.69298	.72095	.70546	.70875	8
	53	.65452	.75604	.66762	.74451	.68051	.73274	.69319	.72075	.70567	.70855	7
	54 55	.65474 .65496	.75585	.66783	.74431	68072	.73254	.69340	.72055	.70587	.70834	6
	56	.65518	.75566 .75547	.66827	.74412	.68093	.73234	.69361	.72035 .72015	.70608	.70813 .70793	5 4
	57	.65540	.75528	.66848	.74373	.68136	.73195	.69403	.71995	.70649	.70772	3
	58	.65562	.75509	.66870	.74353	.68157	.73175	.69424	.71974	70670	.70752	2
	59	.65584	.75490	.66891	.74334	.68179	.73155	.69445	.71954 .71934	.70690	.70731	1
	60	.65606	.75471	.66913	.74314	.68200	.73135	.69466		.70711	.70711	0
	,	Cosin	Sine	Cosin	Sine	Cosin	Sine	Cosin	Sine	Cosin	Sine	,
-		4	90	4	8°	4	70	4	6°	450		1
1	-				-	90				10		1

		TS	

100	164	902	SECA	NTS.		40	
	0°	1°	2°	3°	4°	5°	
0	1.0000000	1.0001523	1.0006095	1 0013723	1.0024419	1.0038198	60
1	1.0000000	1.0001574	1.0006198	1.0013877	1.0024623	1 0038454	59
2 3	1.0000002	1.0001627	1.0006300	1.0014030	1.0024829	1.0038711	58
4	1.0000004	1.0001679	1.0006404	1.0014185	1.0025035	1.0038969	57
5	1.0000011	1.0001788	1.0006509	1.0014341	1.0025241	1.0039486	56
6	1.0000015						
7	1.0000015	1.0001843 1.0001900	1.0006721 1.0006828	1.0014655	1.0025658	1.0039747	54 53
8	1.0000027	1.0001957	1.0006936	1.0014972	1.0026078	1.0040000	52
9	1.0000034	1.0002015	1.0007045	1.0015132	1.0026289	1.0040533	51
10	1 0000042	1.0002073	1.0007154	1.0015293	1 0026501	1.0040796	50
11	1.0000051	1.0002133	1.0007265	1.0015454	1.0026714	1.0041061	49
12	1.0000061	1.0002194	1.0007376	1.0015617	1.0026928	1.0041326	48
13	1.0000072	1.0002255	1.0007489	1.0015780	1 0027142	1.0041592	47
14 15	1.0000083	1.0002317	1.0007602	1.0015944	1.0027358 1.0027574	1.0041859	46
	A CONTROL OF THE					A CONTRACTOR OF THE PARTY OF TH	
16 17	1.0000108	1.0002444	1.0007830	1.0016275	1.0027791	1.0042396	44 43
18	1.0000122	1.0002575	1.0008063	1.0016442	1.0028009	1.0042000	42
19	1.0000153	1.0002641	1.0008180	1.0016778	1.0028448	1.0043208	41
20	1.0000169	1.0002708	1.0008298	1.0016947	1.0028669	1.0043480	40
21	1.0000187	1.0002776	1.0008417	1.0017117	1.0028890	1.0043753	39
22	1.0000205	1.0002845	1.0008537	1.0017288	1.0029112	1.0044028	38
23	1.0000224	1.0002915	1.0008658	1.0017460	1.0029336	1.0044302	37
24 25	1.0000244	1.0002986	1.0008779	1.0017633	1.0029560	1.0044578 1.0044855	36
200	JOSEPH STREET	1.0003058	1.0008902	1.0017806	The second second		35
26	1.0000286	1.0003130	1.0009025	1.0017981	1.0030010	1.0045132	34
27 28	1.0000308	1.0003203	1.0009149	1.0018156	1.0030237	1.0045411	33
29	1 0000356	1.0003352	1.0009400	1.0018509	1.0030693	1.0045970	31
30	1.0000381	1.0003428	1.0009527	1.0018687	1.0030922	1.0046251	30
31	1.0000407	1.0003505	1.0009654	1.0018866	1.0031152	1.0046533	29
32	1.0000433	1.0003582	1.0009783	1.0019045	1.0031383	1.0046815	28
33	1.0000461	1.0003660	1.0009912	1.0019225	1.0031615	1.0047099	27
34	1.0000489 1.0000518	1.0003739 1.0003820	1.0010042 1.0010173	1.0019407	1.0031847	1.0047383	26
100				1.0019589	1.0032081		25
36	1.0000548	1.0003900	1.0010305	1.0019772	1.0032315	1.0047955	24
38	1.0000579 1.0000611	1.0003982 1.0004065	1.0010438 1.0010571	1.0019956 1.0020140	1.0032551	1.0048530	23 22
39	1.0000644	1.0004148	1.0010705	1.0020326	1.0033024	1.0048819	21
40	1.0000677	1.0004232	1.0010841	1.0020512	1.0033261	1.0049108	20
41	1.0000711	1.0004317	1.0010977	1.0020699	1.0033500	1.0049399	19
42	1.0000746	1.0004403	1.0011114	1.0020887	1.0033740	1.0049690	18
43	1.0000782	1.0004490	1.0011251	1.0021076	1.0033980	1.0049982	17
44	1.0000819	1.0004578	1·0011390 1·0011529	1.0021266	1.0034221 1.0034463	1.0050275	13
45	1.0000857						
46	1.0000895	1.0004756	1.0011670	1.0021648	1.0034706 1.0034950	1.0050864	14
47	1.0000935	1.0004846	1.0011811	1.0022034	1.0035195	1.0051456	13
49	1.0001016	1.0005029	1.0012096	1.0022228	1.0035440	1.0051754	111
50	1.0001058	1.0005121	1.0012239	1.0022423	1.0035687	1.0052052	10
51	1.0001101	1.0005215	1.0012384	1.0022619	1.0035934	1.0052351	9
52	1.0001144	1.0005309	1.0012529	1.0022815	1 0036182	1.0052651	8
53	1.0001189	1.0005405	1.0012676	1.0023013	1.0036431	1·0052952 1·0053254	6
54	1.0001234	1.0005501	1.0012823	1.0023211	1.0036932	1.0053557	5
56	1.0001327	1.0005696	1.0013120	1.0023610	1.0037183	1.0053860	4
57	1.0001375	1.0005794	1.0013269	1.0023811	1.0037436	1.0054164	3
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59	1.0001473	1.0005994	1.0013571	1.0024216	1.0037943	1.0054776	1
60	1.0001523	1.0006095	1.0013723	1.0024419	1.0038198	1.0055083	0
1	89°	88°	87°	86°	85°	84°	1
1			-]

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6° 1.0055083 1.0055093 1.0055099 1.0056099 1.0056031 1.0056031 1.00572:6 1.00572:6 1.0057855 1.0058200 1.005817 1.005817 1.0058184 1.0059153 1.0059153 1.0059792 1.0000113 1.0060085 1.0060085 1.0060757 1.0061081 1.0061081 1.0061731 1.0062057	7° 1-0075098 1-0075199 1-0075820 1-0076182 1-0076545 1-0076908 1-0077973 1-0077973 1-0078372 1-0078372 1-0078371 1-0079110 1-0079140 1-0079150 1-0080252 1-0080955 1-00809568 1-0081343 1-0081343 1-0081718 1-0082094 1-0082471	8° 1-0098276 1-0098689 1-0099103 1-0099518 1-0109351 1-0100769 1-0101187 1-0101607 1-0102027 1-010249 1-0103294 1-0103294 1-0103294 1-0103718 1-0104143 1-0104143 1-0104958 1-0105489 1-0105489 1-0105489 1-0105489 1-0105489	9° 1:0124651 1:0125183 1:0125586 1:0126524 1:0126953 1:0126524 1:012993 1:0127466 1:0127939 1:0128413 1:0138886 1:0129837 1:0130314 1:0130791 1:0131270 1:0131270 1:0132711 1:0133194	10° 1-0154266 1-0164787 1-0155310 1-0155833 1-0156883 1-0157408 1-0157408 1-0157934 1-0158463 1-0159991 1-0169052 1-0160050 1-016052 1-0161647 1-0162181 1-0162716 1-0163252 1-0163252 1-0163252 1-0163252	11° 1-0187167 1-0187743 1-0188321 1-0188321 1-0188478 1-0190059 1-0190640 1-0191222 1-0191805 1-0192389 1-0192389 1-0194146 1-0194731 1-0195322 1-0195502 1-0195502	57
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83°	820	81°	80°	700	780	1
61	-02	01	-00	10	10	P. PEC
	1-0063701 1-0064032 1-0064364 1-0064364 1-0063603 1-0065036 1-0065039 1-0066039 1-0066039 1-0066039 1-0066039 1-0067054 1-00677054 1-00677054 1-0067105 1-0068403 1-0069453 1-0069453 1-007049 1-0070443 1-007103	1 0063701 1 0085135 1 0064037 1 0085904 1 0064697 1 0086290 1 0065364 1 0087964 1 0065366 1 0087964 1 0065366 1 0087452 1 00663762 1 0087452 1 0066039 1 0087452 1 0066039 1 0087452 1 0066039 1 0087452 1 00660754 1 0088233 1 0067054 1 0089303 1 0068753 1 0089408 1 0068753 1 0098902 1 0068763 1 009996 1 0068419 1 0090592 1 0068763 1 0090592 1 00695763 1 0090592 1 00695763 1 0092183 1 00695763 1 0092183 1 00701963 1 0092184 1 00701963 1 0092183 1 00701963 1 0092583 1 00711963 1 0092584 1 00711963 1 0093386 1 00711963 1 0093386 1 00712948 1 0094596 1 00712948 1 0094596 1 0072948 1 009596 1 0072948 1 009596 1 007386 1 007199 1 009598 1 0071993 1 009284 1 0071993 1 0093386 1 0071993 1 0093496 1 0095408 1 0095408 1 0095408 1 0095408 1 0095408 1 009631 1 009631 1 009631 1 0097453 1 0097453 1 0097453 1 0097453 1 0097453 1 0097453 1 0097453 1 0097453	1-0063701 1-0085135 1-0106747 1-0064032 1-0085904 1-0110621 1-0064087 1-0086290 1-0111061 1-0065306 1-0087064 1-0111941 1-0065306 1-0087064 1-0111941 1-0065306 1-0087064 1-0111941 1-00665702 1-0087452 1-0112837 1-00660376 1-0087452 1-0113870 1-0066704 1-0088623 1-0113715 1-0067054 1-0088623 1-0113715 1-0067054 1-0089015 1-0114100 1-006376 1-0089019 1-0115050 1-0068763 1-0089080 1-0115050 1-0068763 1-0089080 1-0115050 1-0068763 1-0089080 1-0115050 1-0068763 1-0089080 1-0115050 1-0068763 1-0090196 1-0115502 1-0068763 1-0090196 1-0115502 1-0068763 1-0090196 1-0115502 1-0068763 1-0090196 1-0115502 1-0068763 1-0090196 1-0115502 1-0068763 1-0090196 1-0115502 1-0068763 1-0090196 1-0115502 1-0068763 1-0090196 1-0115502 1-0068763 1-0090196 1-0115061 1-0068763 1-0090198 1-0116601 1-0068763 1-0090198 1-0116601 1-0068763 1-0090198 1-0116601 1-0068763 1-0091386 1-0116801 1-00701404 1-0092584 1-0118663 1-00701404 1-0092584 1-0118663 1-0071034 1-0093788 1-0119118 1-0071103 1-0093788 1-0119118 1-0071201 1-0093788 1-011903248 1-0072201 1-0093601 1-012089 1-007380 1-0099815 1-0121609 1-0074850 1-0099815 1-0121809 1-0074850 1-0099826 1-0121809 1-0074850 1-0097863 1-0124651 1-0075008 1-0097863 1-0124651 1-0075008 1-0098276 1-0124651	1-0063701 1-0085135 1-0109747 1-0137574 1-0064032 1-0085904 1-0110622 1-0138568 1-0064032 1-0085904 1-0110622 1-0138568 1-0064087 1-0086290 1-0111061 1-0138065 1-0065366 1-0087061 1-0111949 1-0140040 1-0065366 1-0087061 1-0111949 1-0140040 1-00665702 1-0087453 1-0112874 1-0112874 1-0140536 1-00663676 1-0087453 1-0112874 1-0140536 1-00660376 1-0088232 1-0113277 1-0141530 1-00660376 1-0088232 1-0113775 1-0141530 1-0067054 1-0089408 1-0114606 1-0142528 1-0067054 1-0089408 1-0114606 1-0142528 1-0067389 1-0089408 1-0114606 1-0142528 1-0067389 1-0089408 1-0114504 1-0084763 1-0089408 1-0114504 1-0084763 1-0089408 1-0114606 1-0144533 1-0068453 1-00969592 1-0115502 1-0144033 1-0068453 1-0091386 1-0116851 1-0145536 1-0068453 1-001386 1-0116851 1-0145536 1-0069468 1-0091386 1-0116851 1-0145536 1-0070444 1-002553 1-0118909 1-0146056 1-0070444 1-002553 1-0118909 1-0147064 1-0070444 1-0098484 1-0118663 1-0147572 1-0070434 1-0093788 1-0119178 1-0148034 1-00702801 1-0093788 1-0119178 1-0148034 1-0072801 1-0093788 1-0119178 1-014903 1-0073801 1-0095815 1-0129489 1-0156436 1-0073801 1-0095815 1-0122793 1-0151673 1-0074380 1-0095861 1-0122793 1-0151673 1-0074098 1-0095861 1-0122793 1-0151673 1-0074098 1-0095861 1-0124855 1-0154266 1-0075408 1-0097863 1-012485 1-0154266 1-0075408 1-0097863 1-012485 1-0154266 1-0075408 1-0097863 1-012485 1-0154266 1-0075408 1-0097863 1-012485 1-0154266 1-0075408 1-0098783 1-012485 1-0154266 1-0075408 1-0098783 1-012485 1-0154266 1-0075408 1-0098783 1-012485 1-0154266 1-0075408 1-0098783 1-012485 1-0154266 1-0075408 1-0098783 1-012485 1-0154266 1-0075408 1-0098783 1-012485 1-0154266 1-0075408 1-0098783 1-012485 1-0154266 1-0075408 1-0098783 1-012485 1-0154466 1-	1-0063701	1-0063701

-				SECA	ANTS.			
1	,	12°	13°	14°	15°	16°	17°	7.
1		1.0223406	1.0263041	1.0306136	1.0352762	1.0402994	1.0456918	60
1	0	1.0224039	1.0263731	1.0306884	1.0353569	1.0103863	1.0457848	59
ı	1 2	1.0224673	1.0264421	1.0307633	1.0354378	1.0404732	1.0458780	58
1	3	1.0225307	1.0265113	1.0308383	1.0355187	1.0405602	1 0459712	57
1	4	1.0225942	1.0265806	1.0309134	1.0355998	1.0406473	1.0460646	56
1	5	1.0226578	1.0266499	1.0309886	1.0356809	1.0407346	1.0461581	55
1	6	1.0227216	1.0267194	1.0310639	1.0357621	1.0408219	1.0462516	51
ı	7	1.0227854	1.0267889	1.0311393	1.0358435	1.0409094	1.0463453	53
1	8	1.0228493	1.0268586	1.0312147	1.0359249	1.0409969	- 1.0464391	52
1	9	1.0229133	1.0269283	1.0312903	1.0360065	1.0410845	1.0465330	51
1	10	1.0229774	1.0269982	1.0313660	1.0360881	1.0411723	1.0466270	50
1	11	1.0230416	1.0270681	1 0314418	1.0361699	1.0412601	1.0467211	49
1	12	1.0231059	1.0271381	1.0315177	1.0362517	1.0413481	1.0468153	48
1	13	1.0231703	1.0272082	1.0315936	1.0363337	1.0414362	1.0469096	47
1	14	1.0232348	1.0273488	1.0317459	1.0364157	1.0415243	1.0470040	46
1	15				1.0364979	1.0416126	1-0470986	45
1	16	1.0233641	1.0274192	1.0318222	1.0365801	1.0417009	1.0471932	44
Į	17	1.0234288	1.0274897	1.0318985	1.0366625	1.0417894	1.0472879	43
ı	18	1.0234937	1.0275603	1.0319750	1.0367449	1.0418780	1.0473828	42
1	19 20	1.0235587	1.0276310 1.0277018	1.0320516	1.0369101	1.0419667	1.0474777	41
1								
1	21	1-0236889	1.0277727	1.0322050	1.0369929	1.0421443	1.0476679	39
1	22	1.0237541	1.0278437	1.0322818	1.0370757	1.0422333	1.0477632	38
1	23	1.0238195 1.0238849	1·0279148 1·0279860	1.0323588	1.0371587	1.0423224	1.0478586	37
9	24 25	1.0239504	1.0280573	1.0325130	1.0373249	1.0425009	1.0480496	36
1								
1	26	1.0240161	1.0981287	1-0325903	1.0374083	1.0425903	1.0481453	34
4	27	1.0240818	1.0282002	1.0326676	1.0374915	1.0426798	1.0482411	33
3	28 29	1-0241476	1.0282717	1.0327451	1.0375750 1.0376585	1.0427694	1.0483370 1.0484330	32
ı	30	1.0242135	1.0284152	1.0325221	1.0377422	1.0429489	1.0485291	31
ı								
Ē	31 32	1.0243456	1.0284871	1.0329781	1.0378260	1.0430388	1.0486253	29
ı	33	1.0244118	1.0285590	1.0330559	1.0379098	1.0431289	1.0487217 1.0488181	28
ı	34	1.0245445	1.0287033	1.0332119	1.0380779	1.0433092	1.0489146	26
ĕ	35	1.0246110	1.0287755	1 0332901	1.0381621	1.0433995	1.0490113	25
ı	36							1.0
1	37	1.0246776	1.0288479	1.0333683	1.0382463	1.0434900 1.0435805	1.0491080 1.0492049	24
В	38	1.0247442	1.0289929	1.0334467	1.0384152	1.0436712	1.0493019	23
1	39	1.0248779	1.0290655	1.0336037	1.0384998	1.0437619	1.0493989	21
ij	40	1.0249448	1.0291383	1.0336823	1.0385844	1.0438528	1.0494961	20
	41		1.0292111			1.0439437	1.0495934	
9	42	1.0250119	1.0292111	1.0337611	1·0386692 1·0387541	1.0440348	1.0496908	19
	43	1.0250750	1.0293571	1.0338399 1.0339188	1.0388391	1.0441259	1.0197883	18
	44	1.0252136	1.0294302	1.0339979	1.0389242	1.0442172	1.0498859	16
í	45	1.0252811	1.0295034	1.0340770	1.0390094	1.0143086	1.0499836	15
3)	46	3.0053400	1.0005700			7-0411007	1.0500815	
	47	1.0253486	1·0295768 1·0296502	1.0341563	1·0390947 1·0391800	1.0444001	1.0501794	14
	48	1.0254839	1.0297237	1·0342356 1·0343151	1.0392655	1.0445833	1.0502774	12
	49	1.0255518	1.0297973	1.0343131	1.0393511	1.0446751	1.0503756	111
	50	1.0256197	1.0298711	1.0344743	1.0394368	1.0447670	1.0504738	10
	51	1.0256877	1.0299449		1.0395226	1.0448590	1.0505722	9
	52	1.0256877	1.0300188	1.0345540 1.0346338	1.0395226	1.0449511	1.0506706	8
	53	1.0258240	1.0300928	1.0347138	1.0396945	1.0450433	1.0507692	7
	54	1.0258923	1.0301669	1.0347938	1.0397806	1.0451357	1.0508679	6
	55	1.0259607	1.0302411	1.0348740	1.0398669	1.0452281	1.0509667	5
	56	1.0260292	1.0303154	1.0349542	1.0399532	1.0453206	1.0510656	4
	57	1.0260978	1.0303898	1.0350346	1.0400396	1.0454132	1-0511646	3
	58	1.0261665	1.0304643	1.0351150	1-0401261	1.0455060	1.0512637	2
	60	1.0262352	1.0305389	1:0351955	1.0402127	1.0455988	1.0513629	1
	00	1-0263041	1.0306136	1.0352762	1.0402994	1.0456918	1.0514622	0
	1	77°	76°	75°	74°	73°	72°	1

S				

1			DECZ	INIS.			3
,	18°	19°	20°	21°	22°	23°	
0	1.0514622	1.0576207	1.0641778	1-0711450	1.0785347	1-0863604	60
1	1.0515617	1.0577267	1.0642905	1.0712647	1.0786616	1.0864946	59
2	1.0516612	1.0578329	1.0644033	1.0713844	1.0787885	1.0866289	58
3	1.0517608	1.0579390	1-0645163	1.0715013	1.0789156	1.0867631	57
4	1.0518606	1.0580453	1.0646294	1.0716244	1-0790427	1.0868979	56
5	1.0519605	1.0581517	1.0647425	1.0717445	1.0791700	1.0870326	55
6	1.0520604	1.0582583	1.0648558	1.0718647	1.0792975	1.0871675	54
7	1.0521605	1.0583649	1.0649693	1.0719851	1.0794250	1.0873021	53
8	1.0522607	1.0584717	1.0650828	1.0721056	1.0795527	1.0874375	52
9	1.0523610	1 0585786	1.0651964	1.0722262	1.0796805	1.0875727	51
10	1.0524614	1.0586855	1.0653102	1.0723469	1.0798084	1.0877080	50
11	1.0525619	1.0587926	1-0654240	1.0724678	1.0799364	1.0878435	49
12	1.0526625	1.0588999	1.0655380	1.0725887	1.0800646	1.0879791	48
13	1.0527633	1.0590073	1.0656521	1.0727098	1.0801928	1.0881148	47
14	1.0528641	1.0591146	1.0657663	1.0728310	1.0803212	1.0882506	46
15	1:0529651	1.0592221	1.0658807	1.0729523	1.0804497	1.0883866	45
	1.0530661	1.0593298	1.0659951	1.0730737	1.0805784	1.0885226	44
16	1.0531673	1.0594376	1.0661097	1.0730737	1.0807071	1.0886589	43
17	1.0532686	1.0595454	1.0662243	1.0733370	1 0808360	1 0887953	42
18	1.0532689	1.0596534	1.0663391	1.0734388	1.0809650	1.0859317	41
19 20	1.0534714	1.0597615	1.0664540	1.0735607	1.0810942	1.0890682	40
1							
21	1.0535730	1-0598697	1.0665690	1.0736827	1.0812234	1.0892050	39
22	1.0536747	1.0599781	1.0666842	1.0738048	1.0813528	1.0893418	38
23	1.0537765	1.0600865	1.0667994	1.0739271	1.0814823	1.0894788	37
24	1.0538785	1.0601951	1.0669148 1.0670302	1.0740495	1.0816119	1·0896159 1·0897531	36
25	1.0539805	1.0603037		1-0741720			35
26	1.0540826	1 060 1125	1.0671458	1.0712946	1.0818715	1-0898901	34
27	1.0541849	1.0605214	1.0672615	1.0744173	1.0820015	1.0900279	33
28	1.0542873	1.0606304	1.0673774	1.0745402	1.0821316	1.0901655	32
29	1.0543897	1.0607395	1.0674933	1.0746631	1.0822618	1.0903032	31
30	1.0544923	1-0608487	1.0676094	1.0747862	1.0823922	1.0904411	30
31	1.0545950	1.0609580	1.0677255	1.0749095	1.0825227	1.0905791	29
32	1.0546978	1.0610675	1.0678418	1.0750328	1.0826533	1 0907172	28
33	1.0548007	1.0611770	1.0679582	1.0751562	1.0827840	1.0908554	27
34	1.9549037	1.0612867	1.0680747	1.0752798	1.0829149	1.0909938	26
35	1 0550068	1.0613965	1.0081914	1.0754035	1.0830458	1-0911323	25
36	1.0551101	1-0615061	1.0683081	1.0755273	1.0831769	1.0912709	21
37	1.0552134	1.0616164	1.0684250	1.0756512	1.0933081	1.0914097	23
38	1.0553169	1.0617265	1.0685420	1.0757753	1.0834395	1.0915485	23
39	1.0554204	1.0618367	1.0686591	1.0758995	1-0835709	1 0916876	21
40	1.0555241	1.0619471	1.0697763	1.0760237	1.0837025	1.0918267	20
41	1.0556279	1.0620575	1.0688936	1-0761481	1-0838349	1-0019659	19
42	1.0557318	1.0621681	1.0690110	1.0762727	1.0839661	1.0921053	18
43	1.0558358	1.0622788	1.0691286	1.0763973	1.0840980	1.0922418	17
44	1.0559399	1-0623896	1.0692463	1.0765221	1.0842301	1.0923845	16
45	1.0560441	1.0625005	1.0693641	1.0766470	1 0843623	1.0925243	15
46	1.0561485	1.0626115	1-0694820	1.0767720	1.0844947	1.0926642	14
47	1.0562529	1.0627227	1.0696000	1.0768971	1.0846271	1.0928042	13
48	1.0563575	1.0628339	1.0697182	1.0770224	1.0847597	1.0929444	12
49	1.0564621	1.0629453	1.0698364	1 0771477	1.0848924	1.0930846	111
50	1.0565669	1-0630568	1.0699548	1.0772732	1.0850252	1.0932251	10
1	1.0566718	1.0631684	1.0700733	1.0773988	1.0851582	1.0933656	100
51	1.0567768	1.0632801	1.0701733	1.0773988	1.0851582	1.0935063	9
52	1.0568819	1.0633919	1.0703105	1.0776504	1.0854245	1.0936471	8 7
53 54	1.0569871	1.0635038	1.0704295	1.0777764	1.0855578	1.0937880	6
55	1.0570924	1.0636158	1.0705484	1.0779025	1.0856912	1.0939291	5
1	Residence of the second					1.0940702	1 8
56	1.0571978	1.0637280	1.0706675	1.0780287	1-0858248	1.0940702	4
57	1-0573034	1.0638493	1.0707867	1.0781550	1.0859585 1.0860924	1.0943110	3
58	1.0574090	1.0639527 1.0640652	1.0709060 1.0710254	1.0782815	1.0860924	1.0943330	2
59	1.0576207	1.0641778	1.0710254	1.0784080	1.0863203	1.0946363	0
00							1
1	71°	70	- 69°	68°	67°	66	1
1	71°	70°	- 69°	68°	67°	66°	1

SECANTS.										
	24°	25°	26°	27°	28°	29°	1,			
0	1.0946363	1.1033779	1.1126019	1.1223263	1.1325701	1.1433541	60			
1	1-0947781	1.1035277	1.1127599	1.1224927	1.1327453	1.1435385	59			
2	1.0949201	1.1036773	1.1129179	1.1226592	1.1329207	1.1437231	58			
3	1.0950622	1.1038275	1.1130761	1-1228259	1.1330962	1.1439078	57			
4	1.0952011	1.1039777	1.1132345	1.1229928	1.1332719	1.1440927	56			
5	1.0953467	1.1041279	1.1133929	1.1231598	1.1334478	1.1442778	55			
6	1.0954892	1.1042783	1.1135516	1.1233269	1.1336238	1.1444630	54			
7	1-0956318	1.1044289	1'1137103	1.1231942	1.1337999	1.1446484	53			
8	1 0957746	1.1045795	1.1138692	1.1236616	1.1339762	1.1448339	52			
9	1.0959174	1.1047303	1.1140283	1.1238292	1.1341527	1.1450196	51			
1.0	1.0960604	1.1048813	1.1141874	1.1239969	1.1343293	1.1452055	50			
11	1.0962036	1.1050324	1.1143167	1.1211618	1.1345060	1.1453915	49			
12	1 0963468	1.1051836	1.1145062	1-12#3328	1.1346829	1.1455776	48			
13	1.0964902	1.1053349	1.1146658	1.1245010	1.1348500	1.1457639	47			
14	1.0966337	1.1054864	1.1148255	1.1246693	1 1350372	1.1459504	46			
15	1.0967774	1.1056380	1.1149854	1.1218377	1.1352146	1.1461371	45			
16	1.0969212	1.1057898	1.1151454	1.1250063	1-1353921	1.1463238	44			
17	1.0970651	1.1059417	1.1153056	1.1251750	1.1355697	1.1465108	43			
18	1.0972091	1.1060937	1.1154659	1.1253439	1.1357476	1.1466979	42			
19	1.0973533	1.1062453	1.1156263	1.1255130	1.1359255	1.1468852	41			
20	1.0974976	1.1063981	1.1157869	1.1256821	1.1361036	1.1470726	40			
	1.0976420	1-1065506	1.1159476	1.1258514	1.1362819	1.1472602	39			
21	1.0977866	1.1067031	1.1161084	1.1238314	1.1364603	1.1474479	38			
22 23	1.0979313	1.1068558	1.1162694	1.1261905	1.1366389	1.1476358	37			
24	1.0980761	1.1070087	1.1164306	1.1263603	1.1368176	1.1478239	36			
25	1 0982211	1.1071616	1.1165919	1.1265302	1.1369965	1.1480121	35			
	1.0983662	1.1073147	1.1167533			1.1482005	34			
26	1.0985114	1.1074680	1.116/553	1-1267003	1.1371755		33			
27	1-0986568	1.1076214	1.1170766	1·1268705 1·1270408	1.1373547	1.1483890	32			
28 29	1.0988023	1.1077749	1.1172381	1.1272113	1.1377135	1.1487665	31			
80	1.0989479	1.1079285	1.1174004	1.1273819	1.1378932	1.1489555	30			
185	1.0990036	1.1080823					29			
31	1.0992395	1.1082363	1.1175625	1.1275527	1.1380730	1.1491447	23			
32	1.0993855	1.1083903	1.1177248	1.1277237	1.1382529	1.1493340	27			
33	1.0995317	1.1085445	1.1180198	1.1278948	1.1384330	1.1497132	26			
34	1.0996779	1.1086989	1.1182124	1.1282374	1.1387937	1 1499030	25			
35	1.0998243						24			
36	1.0999709	1.1088533	1.1183753	1.1284089	1.1389742	1.1500930	23			
37	1.1001175	1.1090079	1.1185393	1.1295806	1.1391550	1.1502831	93			
38	1.1002644	1.1093176	1.1187014	1.1287524	1.1393358	1.1504734	21			
39	1-1004113	1.1094726	1.1190281	1.1289244	1.1395169	1.1508544	20			
40							19			
41	1·1005584 1·1007056	1.1096277	1.1191916	1.1292687	1.1398794	1.1510452	18			
42	1.1008529	1-1097830	1.1193553	1.1294412	1.1400608	1.1512361	17			
43	1.1010004	1.1099385	1.1195191	1.1296137	1.1102425	1.1514272	16			
44	1.1011480	1.1100940	1·1196831 1·1198472	1·1297864 1·1299593	1.1404243	1.1516185	15			
45										
46	1.1012957	1-1104056	1.1200115	1.1301323	1.1407883	1.1520015	14			
47	1.1014436	1.1105616	1.1201759	1.1303055	1.1409706	1.1521932	13			
48	1·1015916 1·1017397	1.1107177	1.1203405	1.1304788	1.1411530	1.1523851	111			
49	1.1018879	1.11108740	1.1205051	1.1306522	1.1413356	1·1525772 1·1527694	10			
50			1.1206700	1.1308258	1.1415183		1000			
51	1.1020363	1.1111869	1.1208350	1.1309996	1.1417012	1.1529618	9			
52	1.1021849	1.1113436	1.1210001	1.1311735	1.1418842	1.1531543	8 7			
53	1.1023335	1.1115004	1.1211653	1.1313475	1.1:20674	1.1533470	6			
54	1.1024823	1.1116573	1.1213308	1.1315217	1.1422507	1·1535399 1·1537329	5			
55	SE 32 19 27 19 19			1.1316961			100			
56	1.1027803	1.1119716	1.1216620	1.1318706	1 1426179	1.1539261	4			
57	1.1029295	1.1121290	1.1218278	1.1320452	1.1428017	1.1541195	8			
58	1.1030789	1.1122865	1.1219938	1.1322200	1.1429857	1.1543130	1			
59	1.1032283	1.1124442	1.1221600	1.1323950	1.1431698	1.1545067	0			
-60				1.1325701	1.1433541		,			
1	65°	64°	63°	62°	61°	60°	18			
1										

1	30°	31°	32°	33°	34°	050	
		The state of the s		1		35°	6
0	14547005	1.1666334	1.1791784	1.1923633	1.2062179	1.2207746	5
1	1.1518945	1.1668374	1.1793928	1.1925886	1.2064547	1.2210233	5
2	1.1550887	1.1670416	1.1796074	1.1928142	1.2069288	1.2212723	5
3	1·1552830 1·1554775	1:1672459	1.1798222	1·1930399 1·1932658	1.2071662	1.2215215	1 8
5	1.1556722	1.1674504	1·1800372 1·1802523	1.1934918	1-2074037	1·2217708 1·2220204	1
- 1							
6	1·1558670 1·1560620	1·1678599 1·1680649	1·1804676 1·1806831	1·1937181 1·1939446	1.2076415	1.2222702	
8	1.1562572	1.1682701	1.1808988	1.1941712	1.2081175	1.2227703	
9	1.1564525	1.1684755	1.18111146	1.1943980	1.2083559	1.2230207	1
0	1.1566480	1.1686810	1.1813307	1.1946251	1.2085944	1.2232713	
,	1.1568436	1.1688867	1.1815469	1.1948523	1.2088331		1
2	1.1570394	1.1690926	1.1817633	1.1950796	1.2090720	1·2235222 1·2237732	1
3	1.1572354	1.1692986	1.1819798	1.1953072	1.2093112	1.2240244	1
4	1.1574315	1.1695048	1.1821966	1.1955350	1.2095505	1.2242758	1
5	1.1576278	1.1697112	1.1824135	1.1957629	1.2097900	1-2245274	1
6	1.1578243	1.1699178	1.1826306	1.1959911	1.2100297	1.2247793	1
7	1.1580209	1.1701245	1.1828479	1.1962194	1.2102696	1.2247793	1
8	1.1582177	1.1703314	1.1830654	1.1964479	1.2105097	1.2252836	1
9	1.1584146	1.1705385	1.1835830	1.1966767	1.2107500	1.2255361	
0	1.1586118	1.1707457	1.1835008	1.1969056	1.2109905	1.2257887	1
1	1.1588091	1.1709531	1.1837188	1.1971346	1.2112312	1.2260416	1
2	1.1590065	1.1711607	1.1839370	1.1973639	1.2114721	1.2262947	1
3	1.1592041	1.1713685	1.1841554	1.1975934	1-2117132	1.2265480	1
4	1-1591019	1-1715764	1.1843739	1.1978230	1.2119545	1.2268015	1
5	1.1595999	1.1717845	1.1845927	1.1980529	1.2121960	1.2270552	13
6	1.1597980	1.1719928	1.1848116	1.1982829	1.2124377		
7	1.1599963	1.1722013	1.1850307	1.1985131	1-2126795	1.2273091	1
8	1.1601947	1.1724099	1.1852500	1.1987435	1.2129216	1·2275633 1·2278176	
9	1.1603933	1.1726187	1.1854694	1.1989741	1.2131639	1.2280723	
0	1.1605921	1.1728277	1.1856890	1.1992049	1.2134064	1.2283269	
1	1.1607911	1.1730368	1.1859089	1-1994359	1.2136191	1.2285819	
2	1.1609902	1:1732462	1.1861289	1.1996671	1.2138920	1-2258371	
3	1.1611894	1.1734557	1.1863490	1.1998985	1.2141351	1.2290924	1
4	1.1613889	1.1736653	1.1865694	1.2001300	1.2143784	1.2293480	15
5	1.1615885	1.1738752	1.1867900	1.2003618	1-2146218	1.2296039	
6	1.1617883	1.1740852	1.1870107	1.2005937	1.2148655	1.2298599	
7	1.1619882	1.1742954	1.1872316	1.2008258	1.2151094	1.2301161	1
8	1.1621883	1.1745058	1.1874527	1.2010582	1.2153535	1.2303725	1
19	1.1623886	1.1747163	1.1876740	1.2012907	1.2155978	1.2306292	
0	1.1625891	1.1749270	1.1878954	1.2015234	F2158423	1.2308861	1
1	1.1627897	1.1751379	1.1881171	1.2017563	1.2160870	1.2311432	1
2	1.1629905	1.1753490	1.1883389	1.2019894	1.2163319	1 2314004	1
3	1.1631914	1.1755603	1.1885609	1.2022226	1.2165770	1.2316579	
4	1.1633925	1.1757717	1.1892831	1.2024561	1.2168223	1.2319156	
5	1.1635938	1.1759833	1.1890055	1 2026898	1.2170673	1.2321736	1
6	1.1637953	1.1761951	1.1892280	1.2029236	1-2173135	1.2324317	
7	1.1639969	1.1764070	1.1894508	1-2031577	1.2175594	1.2324317	
8	1.1641987	1.1766191	1.1896737	1.2033919	1.2178055	1.2329486	1
19	1:1644007	1.1768314	1.1898968	1.2036264	1.2180518	1.2332074	
50	1.1646028	1.1770439	1.1901201	1.2038610	1.2182983	1.2334664	
1	1.1648051	1 1772566	1.1903436	1.2040958	1-2185450	1.2337256	
2	1.1650076	1.1774694	1.1905673	1.2043308	1-2187919	1.2337250	1
3	1.1652102	1.1776824	1.1907911	1.2045660	1.2190390	1.2342446	1
54	1.1654130	1.1778956	1.1910152	1.2048014	1.2192864	1.2345044	
55	1.1656160	1.1781089	1.1912394	1.2050370	1.2195339	1.2347645	1
56	1.1658191	1.1783225	1.1914638	1.2052728	1.2197816	1.2350248	1
57	1.1660224	1.1785362	1.1916884	1.2055088	1.2200296	1.2350248	-
58	1.1662259	1.1787501	1.1919132	1-2057450	1.2202777	1.2355459	
59	1.1664296	1.1789642	1.1051321	1.2059814	1-2205260	1-2358069	1
60	1.1666334	1.1791784	1.1923633	1.2062179	1.2207746	1.2360680	1
,	59°	58°	57°	56°	55°	TO COLD TO	1
	all the same of th			00	00	54°	

			SECA	M15.			
,	36°	37°	38°	39°	40°	41°	
100	1.2360680	1.2521357	1-2690182	1.2367596	1.3054073	1.3250130	60
0	1.2363293	1.2524102	1.2693067	1.2870628	1.3057261	1.3253483	59
1	1.2363909	1.2526850	1-2695955	1.2873663	1.3060451	1 3256837	58
2	1.2368526	1.2529601	1.2698845	1.2876700	1.3063614	1.3260191	57
3 4	1-2371146	1.2532353	1-2701737	1.2879740	1.3066839	1.3263554	56
5	1 2373768	1.2535108	1.2704632	1.2882782	1.3070038	1:3260918	55
100	1-2376393	1.2537865	1-2707529	1.2885827	1.3073239	1:3270284	54
6	1.2379019	1.2540625	1.2710429	1.2888875	1.3076442	1.3273653	53
7	1.2381647	1.2543387	1.2713331	1.2891925	1.3079649	1.3277021	52
8	1.2384278	1.2546151	1.2716235	1.2891977	1.3082858	1.3280399	51
9	1.2386911	1.2548917	1.2719142	1.2898033	1.3086069	1.3283776	50
10	1-2389546	1-2551685	1.2722052	1.2901090	1.3089284	1.3287156	49
11	1.2392183	1.2554456	1.2724963	1-2904150	1.3092501	1.3290539	48
12	1-2394823	1.2557223	1.2727877	1.2907213	1.3095720	1.3293925	47
13	1.2397464	1.2560005	1.2730794	1.2910278	1.3098943	1.3297314	46
14	1-2400108	1.2562782	1.2733712	1-2913346	1.3102168	1.3300706	45
15	1 2402754	1.2565562	1.2736634	1.2016416	1.3105396	1.3304100	44
16	1-2405403	1 .2568315	1.2739557	1.2919489	1.3108626	1.3307497	43
17	1.2108053	1.2571129	1.2712484	1.2922564	1.3111860	1.3310897	42
18	1-2410704	1.2573916	1.2745412	1-2925642	1.3115095	1.3314301	41
19	1 2413359	1.2576705	1.2718313	1-2928723	1.3118334	1.3317707	40
20	1-2416016	1.2579497	1.2751276	1.2931806	1.3121575	1-3321115	39
21	1 2118675	1-2582291	1.2751213	1.2934892	1.3124820	1.3324527	38
22	1.2421336	1.2585087	1.2757151	1.2937980	1.3128066	1.3327942	37
23	1.2423999	1.2587885	1.2760091	1-2941071	1.3131316	1.8331359	36
24	1-2426665	1.2590686	1.2763034	1-2944164	1.3134568	1.3331779	35
25	The state of the s						
26	1.2429333	1-2593489	1.2765980	1.2947260	1.3137823	1.3338203	84
27	1.2432003	1.2596294	1.2768928	1.2950359	1.3141081	1.3341629	33
28	1.2434675	1·2599102 1·2601912	1.2771878	1·2953160 1·2956564	1.3147604	1.3348489	31
29	1-2410026	1:2604724	1.2777787	1 2959670	1.3150870	1.3351924	30
30							1
1100	1.2442704	1.2607539	1.2780744	1-2962779	1.3154139	1.3355362	29
31	1.2415385	1.2610356	1.2783705	1.2965890	1.3157410	1.3358802	28
32	1.2448069	1.2613175	1.2786667	1-2969004	1.3160684	1.3362246	27
34	1.2450754	1.2615997	1.2789632	1-2972121	1.3163961	1.3365692	25
35	1-2453449	1.2618820	1-2792600	1.2975240	1.3167210	1.3369141	
1100	1.2456131	1.2621647	1.2795570	1.2978362	1.3170523	1.3372594	24
36	1.2458823	1.2624175	1.2798543	1.2981487	1.3173808	1.8376049	23
37	1.2461518	1 2627306	1.2801518	1.2984614	1.3177096	1.3379507	22
38	1-2464214	1.2630140	1.2801495	1.2987743	1.3180386	1 6382968	21
39	1-2466913	1-2632975	1.2807475	1.2990876	1.3183680	1.3386432	20
40	1.2469614	1.2635813	1.2810457	1:2991011	1.3186976	1.3389898	19
41	1.2472317	1.2635653	1.2813442	1-2997148	1.3190274	1.3393368	18
42	1-2475022	1.2611496	1.2816130	. 1.3000288	1.3193576	1.3396841	17
43	1 2477730	1 2644311	1.2819419	1.30G3431	1.3196881	1.3400316	16
1 44	1-2480440	1.2047188	1.2822412	1.3006576	1.3200183	1.3403795	15
45	1.2483152	1.2650038	1.2625407	1.3009724	1.3203498	1.8407276	14
46	1-2485866	1-2652890	1.2828401	1.3012875	1.3206810	1.3410761	13
47	1.2488583	1.2655745	1.2831404	1.3016028	1.3210126	1.3414248	12
48	1-2491302	1.2658601	1-2831406	1.3019184	1.3213444	1.3417738	11
49	1 2494023	1.2661460	1.2837411	1.3022343	1.3216705	1.3421232	10
50	1.2496746	1.2661323	1-2840418	1 3025504	1.3220089	1 34 24 728	9
51	1.2499471	1-2667186	1.2843423	1.3028667	1.3223416	1.3428227	8
52	1.2502199	1.2670052	1.2846140	1 3031834	1.3226745	1 3431729	7
53	1.2504929	1 2672921	1.2849455	1.3035003	1.3230078	1.3435234	6
54	1.2507661	1.2675792	1.2852472	1.3038175	1.3233413	1.3438742	5
55	1.2510396	1.2678665	1.2855492	1.3041349	1.3236750	1.3442253	4
56		1-2681541	1.2858514	1.3044526	1.3240091	1-8445767	3
57		1.2681419	1.2861539	1.3047706	1.3213135	1.3149284	2
58		1.2687299	1.2864566	1.3050888	1.3246781	1.3452804	1
59		1-2690182	1-2867596	1.8054073	1.8250120	1.8456327	0
		100					
60	53°	52°	51°	50°	49°	48°	1

			RECA	NTS.			
,	42°	43°	44°	45°	46°	47°	,
0	1.3456327	1.3673275	1.3901636	1.4142136	1.4395565	1.4662792	60
1	1.3459853	1.3676985	1.3905543	1.4146251	1.4399904	1-4667368	59
2	1.3463382	1.3680699	1.3909453	1.4150370	1.4404216	1.4671948	58
3	1.3466914	1.3684416	1.3913366	1.4154493	1.4408592	1.4676532	56
5	1·3470449 1·3473987	1·3688136 1·3691859	1·3917283 1·3921203	1·4158619 1·4162749	1.4412941	1·4681120 1·4685713	55
6							54
7	1·3477528 1·3481072	1·3695586 1·3699315	1.3925127	1.4166883	1.4421652	1.4690309	53
8	1.3484619	1.3703048	1.3932985	1.4175161	1.4430379	1.4699514	52
9	1.3188168	1.3706784	1.3936918	1.4179306	1.4134748	1.4704123	51
10	1.3491721	1.3710523	1.3940856	1.4183454	1.4439120	1.4708736	50
11	1.3495277	1.3714266	1.3914796	1.4187605	1.4443497	1.4713354	49
12	1.3498836	1.3718011	1.3948740	1.4191761	1.4447878	1.4717975	48
13	1.3502398	1.3721760	1.3952688	1.4195920	1.4452262	1.4722600	47
14	1·3505963 1·3509531	1·3725512 1·3729268	1·3956639 1·3960593	1.4.200083	1.4456651	1.4727230	45
	The second second		A . The state of t				44
16 17	1.3513102	1.3733026	1.3964551	1.4208418	1.4465439	1.4736502	43
18	1·3516677 1·3520254	1·3736788 1·3740553	1·3968512 1·3972477	1.4212592	1.4469839	1.4741144	42
19	1.3523834	1.3744321	1.3976445	1.4220950	1.4478651	1.4750440	41
20	1.3527417	1.3748092	1.3980416	1.4225134	1.4483063	1.4755095	40
21	1.3531003	1.3751867	1.3984391	1.4229323	1.4487478	1.4759751	39
22	1.3534593	1.3755645	1.3988369	1.4233514	1.4491898	1.4764417	38
23	1.3538185	1.3759426	1.3992351	1.4237710	1.4496322	1.4769084	37
24	1.3541780	1.3763210	1.3996336	1.4211909	1.4500749	1.4773755	36
25	1.3545379	1.3766998	1.4000325	1.4246112	1.4505181	1.4778431	
26	1.3548980	1.3770789	1.4004317	1.4250319	1.4509616	1.4788111	34
27	1.3552585	1.3774583	1.4008313	1.4254529	1.4514055	1.4787795	33
28 29	1.3556193	1.3778380	1·4012312 1·4016315	1·4258743 1·4262961	1·4518498 1·4522946	1·4792483 1·4797176	31
30	1.3563417	1.3785985	1.4020321	1.4267182	1.4527397	1.4801872	30
31	1.3567034	1.3789792	1.4024330	1.4271407	1.4531852	1.4806573	29
32	1.3570654	1.3793602	1.4028343	1.4275636	1.4536311	1.4811278	28
33	1.3574277	1.3797416	1.4032360	1.4279868	1.4540774	1.4815988	27
34	1.3577903	1.3801233	1.4036380	1.4284105	1.4545241	1.4820702	26
35	1.3581532	1.3805053	1.4040403	1.4288345	1.4549712	1.4825420	25
36	1.3585164	1.3808877	1.4044430	1.4292588	1.4554187	1.4830142	24
37	1.3588800	1.3812704	1.1048461	1.4296836	1.4558666	1.4834868	23
38	1.3592438	1.3816534	1.4052494	1.4301087	1.4563149	1.4839599	22 21
39	1·3596080 1·3599725	1·3820367 1·3824204	1·4056532 1·4060573	1·4305342 1·4309600	1.4567636	1.4844334	20
	The second						19
41	1:3603372	1:3828044	1.4064617	1.4313863	1·4576621 1·4581120	1·4853817 1·4858565	18
43	1.3610677	1.3835734	1.4072717	1.4322399	1.4585623	1.4863317	17
44	1.3614334	1.3839584	1.4076772	1.4326672	1.4590130	1.4868073	16
45	1.3617995	1.3843437	1.4080831	1.4330950	1.4594641	1.4872834	15
46	1.3621658	1.3847294	1.4084893	1.4335231	1.4599156	1-4877599	14
47	1.3625324	1.3851153	1.4088958	1.4339516	1.4603675	1.4882369	13
48	1.3628994	1.3855017	1.4093028	1.4343805	1-4608198	1.4887142	12
49	1.3632667	1.3858883	1·4097100 1·4101177	1.4348097	-1.4612726	1.4891920	11
50	Barren and		- Allendar	1.4352393	1.4617257	1-4896703	10
51	1.3640022	1.3866626	1.4105257	1.4356693	1.4621792	1.4901489	9
52	1.3643704	1.3870503	1.4109340	1.4360997	1·4626331 1·4630875	1:4906280	8 7
54	1.3651078	1.3878266	1.4117517	1.4369616	1.4635422	1·4911076 1·4915876	6
55	1.3654770	1.3882153	1.4121612	1.4373932	1.4639973	1.4920680	5
56	1.3658464	. 1.3886043	1.4125709	1.4378251	1.4644529	1.4925488	4
57	1-3662162	1.3889936	1.4129810	1.4382574	1.4649089	1.4930301	3
58	1.3665863	1.3893832	1.4133915	1.4386900	1.4653652	1.4935118	2
60	1.3669567	1.3897733	1.4138024	1.4391231	1.4658220	1.4939940	0
	1.3673275	1.3901636	1.4142136	1.4395565	1.4662792	1.4944765	
1	47°	46°	4.5°	44°	43°	42°	
			Cosme	CANTS.			,

			DE DE	CANTS.			
,	48°	49°	50°	51°	52°	53°	
0	1.4914765	1.5242531	1.5557238	1.5890157	1.6242692	1.6616401	6
1	1.4949596	1.5247634	1.5562634	1.5895868	1.6248743	1.6622819	5
2	1.4954431	1.5252741	1.5568035	1.5901584	1.6254799	1.6629243	5
3	1.4959270	1'5257854	1.5573441	1.5907306	1.6260861	1.6635673	5
4	1.1964113	1.5262971	1.5578852	1.5913033	1.6266929	1.6642110	5
5	1.4968961	1.5268093	1.5584268	1.5918766	1.6273003	1.6648553	5
6	1.4973813	1.5273219	1.5589689	1.5924504	1.6279083	1.6655002 1.6661458	5 5
8	1.4983531	1.5283487	1.5600546	1.5935996	1.6291261	1.6667920	5
9	1.4988397	1.5288627	1.5605982	1.5941751	1.6297359	1.6674389	5
10	1.4993267	1.5293773	1.5611424	1.5947511	1.6303462	1.6680864	5
11	1-4998141	1.5298923	1.5616871	1.5953276	1.6309572	1.6687345	4
12	1.5003020	1.5304078	1.5622322	1.5959048	1:6315688	1.6693833	4
13	1.5007903	1.5309238	1.5627779	1.5964824	1.6321809	1.6700328	4
14	1.5012791	1.5314403	1.5633241	1.5970606	1.6327937	1.6706828	40
15	1.5017683	1.5319572	2 0000,00	1.5976394	1.6334070	1.6713336	4
16	1.5022580	1.5324746	1.5644181	1:5982187	1.6340210	1.6719850	44
17	1.5027481	1.5329925	1.5649658	1·5987986 1·5993790	1.6346355 1.6352507	1.6726370 1.6732897	43
18	1.5032387	1.5340297	1.5660628	1.5993790	1.6352507	1.6732897	41
20	1.5042211	1.5345491	1.5666121	1.6005416	1.6364828	1.6745970	40
21	1.5047131	1.5350689	1.5671619	1.6011237	1.6370997	1.6752517	39
22	1.5052054	1.5355892	1.5677123	1.6017064	1.6377173	1.6759070	38
23	1.5056982	1.5361100	1.5682631	1.6022896	1.6383355	1.6765629	37
24	1.5061915	1.5366313	1.5688145	1.6028734	1.6389542	1.6772195	36
25	1.5066852	1.5371530	1.5693664	1.6034577	1.6395736	1.6778768	35
26	1.5071793	1.5376752	1.5699188	1.6040426	1.6401936	1.6785347	34
27	1.5076739	1.5381980	1.5704717	1.6046281	1.6408142	1.6791933	33
28	1.5081690	1.5387212	1.5710252	1.6052142	1.6414354	1.6798525	32
29	1.5086645	1.5392449 1.5397690	1.5715792	1.6058008 1.6063879	1.6420572 1.6426796	1.6805124	31
31	1.5096569	1.5402937	1.5726887	1.6069757	1-6433097	1.6818342	29
32	1.5101538	1.5408189	1.5732443	1.6075640	1.6439263	1.6824961	28
33	1.5106511	1.5413445	1.5738004	1.6081528	1.6445506	1.6831586	27
34	1.5111489	1.5418706	1.5743570	1.6087423	1.6451754	1.6838219	26
35	1.5116472	1.5423973	1.5749141	1.6093323	1.6458009	1.6844857	25
36	1.5121459	1.5429244	1.5751718	1.6099228	1.6464270	1.6851503	24
37	1.5126450	1.5434520	1.5760300	1.6105140	1.6470537	1.6858155	23
38	1.5131446	1.5439801	1.5765887	1.6111057	1.6476811	1.6864814	22
10	1.5136447	1.5445087	1.5771479	1.6122908	1.6483090	1·6871479 1·6878151	21 20
11	1.5146462	1.5455673	1.5782680	1.6128843	1.6 19 5668	1.6884830	19
2	1.5151477	1.5460974	1.5788289	1.6134788	1.6501966	1.6891516	18
3	1.5156496	1.5466280	1.5793902	1.6140728	1.6508270	1.6898208	17
4	1.5161520	1.5471590	1.5799521	1.6146680	1.6514581	1.6904907	16
5	1.5166548	1.5476906	1.5305146	1.6152637	1.6520898	1.6911613	15
6	1.5171581	1.5482226	1.5810776	1.6158600	1.6527221	1.6918326	14
17	1.5176619	1.5487552	1.5816411	1.6164569	1.6533550	1 6925045	13
8	1.5181661	1.5492882	1.5822051	1.6170544	1.6539885	1-6931771	12
9	1.5186708	1.5498218 1.5503558	1·5827697 1·5833348	1·6176524 1·6182510	1.6546227	1.6938504 1.6945244	11 10
0		1.5508904	1.5839005	1.6188502	1.6558929	1.6951990	
1	1:5196815	1.5514254	1.5844667	1.6194500	1.6565290	1.6958744	8
3	1.5206942	1.5519610	1.5850334	1.6200504	1.6571657	1.6965504	7
1	1.5212012	1.5524970	1.5856007	1.6206513	1.6578030	1.6972271	6
5	1.5217087	1.5530335	1.5861685	1.6212528	1.6584409	1.6979044	5
66	1.5222166	1.5535706	1.5867369	1.6218549	1.6590795	1.6985825	4
57	1.5227250	1.5541081	1.5873058	1.6224576	1.6597187	1.6992612	3
8	1.5232339	1.5546462	1·5878752 1·5884452	1.6230609	1.6603586 1.6609990	1.6999407	2
9	1.5237433 1.5242531	1.5551848 1.5557238	1.5890157	1.6236648	1.6616401	1·7006208 1·7013016	0
,	STATE OF THE PARTY OF	40°	39°	38°	37°	36°	1
	41°	20	03	00	01	00	1

302

			SEC.		-		1 -
'	54°	55°	56°	57°	58°	59°	1
0	1.7013016	1.7434468	1.7882916	1.8360785	1.8870799	1.9116040	60
1	1.7019831	1.7441715	1.7890633	1.8369013	1.8879589	1.9425445	59
2	1.7026653	1.7448969	1.7898357	1.8377251	1-8888388	1.9434861	58
3	1.7033482	1.7456230	1.7906090	1.8385498	1.8897197	1.9444288	57
4	1.7040318	1.7463499	1.7913831	1.8393753	1.8906016	1.9453725	56
5	1.7047160	1.7470776	1.7921580	1.8402018	1-8914845	1 9463173	
6	1.7054010	1.7478060	1.7929337	1.8410292	1.8923684	1.9472632	54
7	1.7060867	1.7485352	1.7937102	1.8418574	1.8932532	1.9482102	53
8	1.7067730	1.7492651	1.7944876	1.8426866	1.8941391	1 9491583	52
9	1.7074601	1.7499958	1.7952658	1.8435166	1.8950259	1.9501075	51
10	1.7081478	1.7507273	1.7960449	1.8443476	1.8959138	1.9510577	50
11	1.7088362	1.7514595	1.7968247	1.8451795	1.8968026	1-9520091	49
12	1.7095254	1.7521924	1.7976054	1.8460123	1.8976924	1-9529615	48
13	1.7102152	1.7529262	1.7983869	1.8468460	1.8985832	1.9539150	47
14	1.7109058	1.7536607	1.7991693	1.8476806	1.8994750	1-9548697	46
15	1.7115970	1.7513959	1.7999524	1-8485161	1.9003678	1.9558254	45
16	1-7122890	1.7551320	1.8007365	1.8493525	1-9012616	1.9567822	44
17	1.7129817	1.7558687	1.8015213	1.8501898	1.9021564	1.9577402	43
18	1.7136750	1.7566063	1.8023070	1.8510281	1.9030522	1.9586992	43
19	1.7143691	1.7573446	1.8030935	1.8518672	1.9030491	1-9596593	41
20	1.7150639	1.7580837	1.8038809	1.8527073	1.9018469	1.9606206	40
21	1.7157594	1.7588236	1.8046691	1.8535483	1.9057457	1.9615829	39
22	1.7164556	1.7595642	1.8054582	1.8543903	1.9066456	1.9625464	38
23	1.7171525	1.7603057	1.8062481	1 8552331	1.9075464	1.9635110	37
24	1.7178501	1.7610478	1.8070388	1.8560769	1.9081483	1.9644767	36
25	1.7185484	1.7617908	1.8078304	1.8569216	1.9093512	1.9654435	35
26	1.7192475	1.7625345	1.8086228	1.8577672			34
27	1.7199472	1.7632791	1.8094161	1.8586138	1.9102551 1.9111600	1.9664114 1.9673805	33
28	1.7206477	1.7640244	1.8102102	1.8594612	1-9120659	1.9683507	32
29	1.7213489	1.7647704	1.8110052	1.8603097	1.9129729	1.9693220	31
30	1.7220508	1.7655173	1.8118010	1.8611590	1.9138809	1.9702944	30
31		2000000	-				29
32	1.7227534	1.7662649	1.8125977	1 8620093	1.9147899	1.9712680	28
33	1·7234568 1·7241609	1.7677625	1.8133953	1.8628605 1.8637126	1-9156999	1.9722427	27
34	1.7248657	1.7685125	1.8149929	1.8645657	1.9166110 1.9175230	1-9732185 1-9741954	26
35	1.7255712	1.7692633	1.8157930	1.8654197	1.9184362	1.9751735	25
						Sanata Sana	1 1
36	1.7262774	1.7700149	1.8165940	1.8662747	1.9193503	1.9761527	24
38	1.7269844	1.7707672	1.8173958	1.8671306	1.9202655	1.9771331	23
39	1.7276921 1.7284005	1.7715204	1.8181985	1.8679875	1-9211817	1.9781146	21
40	1.7291096	1.7730290	1.8190021	1.8688453	1.9220990	1.9790972	20
			1.8198065	1.8699040	1.9230173	1-9800810	
41	1.7298195	1.7737815	1.8206118	1.8705637	1.9239366	1.9810659	19
42	1.7305301	1.7745409	1.8214179	1.8714244	1.9248570	1.9820520	18
43	1.7312414	1.7752980	1.8222249	1.8722859	1.9257784	1.9830393	17
45	1.7319535	1.7760559	1.8230328	1.8731485	1.9267009	1.9840276	16
	1.7326663	1.7768146	1.8238416	1.8740120	1.9276244	1.9850172	13:30
46	1.7333798	1.7775741	1.8246513	1.8748764	1.9285400	1.9860080	14
47	1.7340941	1.7783344	1.8254617	1.8757419	1.9294746	1.9869997	13
48	1.7348091	1.7790955	1.8362731	1.8766082	1.9304013	1.9879927	12
49	1.7355248	1.7798574	1.8270854	1.8774755	1.9313290	1.9889869	11
50	1.7362413	1.7806201	1.8278985	1.8783438	1.9322578	1.9899822	10
51	1.7369585	1.7813836	1.8287125	1.8792131	1-9331876	1.9909787	9
52	1.7376764	1.7821479	1.8295274	1.8800833	1.9341185	1.9919764	8
53	1.7383951	1.7829131	1.8303432	1.8809545	1.9350505	1.9929752	7
54	1.7391145	1.7836790	1.8311599	1 8818266	1.9359835	1.9939753	6
55	1.7398347	1.7844457	1.8319774	1.8826998	1.9369176	1.9949764	5
56	1.7405556	1.7852133	1.8327959	1.8835738	1.9378527	1.9959783	4
57	1.7412773	1.7859817	1:8336152	1.8844489	1.9387889	1.9969823	3
58	1.7419997	1.7867508	1.8344354	1.8853249	1-9397262	1.9979870	2
59	1.7427229	1.7875208	1.8352565	1.8862019	1.9406646	1-9989929	1
60	1.7431468	1.7882916	1.8360785	1.8870799	1-9416040	2.0000000	0
1	35°	34°) 33°	32°	31°	30°	1

,	1	60°	61°	62°	63°	64°	65°	1
		2.0000000	2.0626653	2:1300545	2.2026893	2-2811720	2:3662016	60
0		2.0010083	2.0637484	2.1312205	2.2039476	2.2825335	2.3676787	59
1		2.0020177	2.0648328	2.1323880	2.2052075	2.2838967	2.3691578	58
2		2.0030283	2.0659186	2.1335570	2.2064691	2.2852613	2.3706390	57
3	в	2.0040402	2.0670056	2.1347274	2.2077323	2.2866286	2.3721222	56
5		2 0050533	2.0680940	2.1358993	2.2089972	2.2879974	2.3736075	55
		2.0060674	2.0691836	2.1370726	2.2102637	2.2893679	2-3750949	54
6		2.0070828	2.0702746	2.1382475	2.2115318	2.2907403	2:3765843	53
		2.0080994	2.0713670	2.1394238	2.2128016	2.2921145	2:3780758	53
8		2.0091172	2.0724606	2.1406015	2-2140730	2.2934906	2.3795694	51
0		2.0101362	2.0735556	2.1417808	2.2153460	2.2948685	2.3810650	50
		2.0111564	2.0746519	2.1429615	2.2166208	2.2962483	2.3825627	49
1		2.0121779	2.0757496	2.1441438	2.2178971	2.2976299	2:3840625	48
2		2.0132005	20768486	2.1453275	2.2191752	2.2990134	2.3855645	47
3		2.0142243	2.0779489	2.1465127	2.2204548	2.3003988	2.3870685	46
5		2.0152494	2.0790506	2.1476993	2.2217362	2.3017860	2:3885746	43
1		2.0162756	2.0801536	2.1488875	9-9930192	2:3031751	2:3900828	44
6		2.0173031	2.0812580	2.1500772	2.2243039	2:3045660	2:3915931	4:
7		2.0183318	2.0823637	2.1512684	2.2243039	2.3043000	2.3931055	45
8		2.0193618	2.0834708	2.1524611	2.2253903	2.3073536	2:3946201	41
9		2.0203929	2.0845792	2.1536553	2.2281681	2.3087501	2:3961367	-4
)								3
		2.0214253	2.0856890	2.1548510	2-2294595	2.3101486	2.3976555	3
2		2.0224589	2.0868002	2.1560482	2.2307526	2-3115490	2.3991764	3
3		2.0234937	2.0879127	2.1572469	2.2320474	2.3129513	2.4006995	3
1		2·0245297 2·0255670	2·0890265 2·0901418	2·1584471 2·1596489	2-2333438	2·3143554 2·3157615	2·4022247 2·4037520	3
5					2.2346420			3
6		2.0266056	2.0912584	2.1608522	2.2359419	2.3171695	2.4052815	3
7		2.0276453	2.0923764	2.1620570	2.2372435	2.3185794	2.4068132	3
3		2.0286863	2.0934957	2.1632633	2.2385468	2.3199912	2.4083469	3
9		2·0297286 2·0307720	2·0946164 2·0957385	2·1644712 2·1656806	2-2398517	2·3214049 2·3228205	2·4098829 2·4114210	3
0					2-2411585			2
1		2.0318168	2.0968620	2.1668915	2.2424669	2.3242381	2.4129613	2
2		2.0328628	2.0979869	2.1681040	2-2437770	2.3256575	2.4145038	2
3		2.0339100	2.0991131	2.1693180	2-2450889	2.3270790	2.4160484	9
4		2.0349585	2·1002408 2·1013698	2·1705335 2·1717506	2-2464025	2·3285023 2·3299276	2·4175952 2·4191442	2
5		2.0360082		T-Separate -	2-2477178			9
3		2.0370592	2-1025002	2.1729693	2.2490348	2.3313548	2.4206954	1 9
7	3	2.0381114	2.1036320	2.1741895	2.2503536	2.3327840	2.4222488	105
8		2.0391649	2.1047652	2.1754113	2-2516741	2.3342152	2.4238044	1
9		2.0402197	2.1058998	2.1766346	2 2529964	2.3356482	2.4253622	1 9
0		2.0412757	2.1070359	2.1778595	2.2513204	2.3370833	2.4269222	
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2	100	2.0433916	2.1093121	2.1803139	2.2569736	2.3399593	2.4300489	
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4	m.	2.0455126	2.1115940	2.1827746	2.2596339	2.3428432	2.4331844	
5	46	2.0465750	2-1127371	2.1840074	2.2609667	2.3442881	2.4347555	
6		2.0476386	2.1138815	2-1852417	2-2623012	2:3457349	2-4363289	
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8		2.0497698	2.1161748	2.1877150	2.2649756	2.3486347	2.4394823	
9	16	2.0508373	2.1173235	2.1889541	2.2663155	2.3500875	2.4410624	
	16.	2.0519061	2.1184737	2.1901947	2.2676571	2:3515424	2.4426448	
80	63	2-0529762	2-1196253	2.1914370	2.2690005	2.3529992	2.4442294	
1		2.0510476	2.1207783	2.1926808	2.2703457	2.3544581	2.4458163	
2 3	E.	2.0551203	2.1219328	2.1939262	2.2716927	2.3559189	2.4474054	1
6	N.	2.0561942	2.1230887	2.1951733	2.2730415	2:3573818	2.4489968	
5		2.0572695	2.1242460	2.1964219	2.2743921	2.3588467	2.4505905	
6		2.0583460	2.1254048	2.1976721	2-2757445	2:3603136	2.4521865	1
7		2.0594239	2.1265651	2.1989240	2.2770987	2:3617826	2.4537848	1
8	1	2.0605031	2.1277267	2.2001775	2.2784546	2.3632535	2.4553853	
9	1	2.0615836	2.1288899	2.2014326	2-2798124	2.3647265	2.4569882	
0	-	2.0626653	2.1300545	2-2026893	2.2311720	23662016	2.4585933	
		29°	28°	27°		25°	24°	- 1

		rs.

							78
'	66°	67°	68°	69°	70°	71°	
0	2.4585933	2.5593047	2.6694672	2.7904281	2.9238044	3.0715535	6
1	2.4602008	2.5610599	2 6713906	2.7925144	2.9261431	3.0741507	5
2	2 4618106	2.5628176	2.6733171	2.7946641	2-9291858	8.0767525	5
3	2.4634227	2.5645781	2.6752465	2.7967873	2.9308326	3.0793590	5
5	2.4630371	2.5663412	2.6771790	2.7989140	2.9331833	3.0819703	E
25.7	2.4666538	2.5681069	2.6791145	2-8010441	Deliner of the same	3.0815860	3
6	2.4682729	2.5698752	2.6810530	2.8031777	2.9378968	3.0872066	5
7	2.4698943	2.5716162	2.6829945	2.8053148	2.9402597	3.0898319	5
8	2.4715181	2.5734199	2.6849391	2.8074554	2.9126265	3.0924620	0
9	2.4731442	2.5751963	2.6868867	2.8095995	2.9119975	3.095):67	5
10	2.1717726	2.5769753	2.6888371	2.8117471	2.9473725	3.0977363	5
11	2.4764034	9-5787570	2.6907912	2.8138982	2-9497516	3.1003805	4
12	2-1780366	2.5805114	2.6927480	2.8160529	2.9521348	3-1030296	4
13	2.4796721	2.5823284	2.6947079	2.8182111	2.9545221	3.1056835	4
14	2-4813100	2.5841182	2:6966709	2.8203729	2.9569135	3.1093155	4
15	2.4829503	2.5859107	2.6986370	2.8225382	2 959 3090	3.1110037	4
16	2 184 5929	2-5877058	2.7006061	2.8247071	2-9617087	3.1136740	4
17	2 4862380	2.5895037	2.7005061	2.8268796	2.9611125	3.1163172	4
18	2.4878854	2.5913043	2.7045538	2.8290556	2.9665205	3.1190252	4
19	2.4895352	2.5931077	2.7065323	2.8312353	2.9689327	3.1217081	4
20	2.4911874	2.5949137	2.7085139	2.8334185	2:9713490	3.1243959	4
21				Constitution of	SA THE REAL PROPERTY.		
22	2-4928421	2.5967225	2.7104987	2.8356054	2.9737695	3.1270886	3
23	2-1911991	2.5985341	2.7124866	2.8377958	2-9761942	3.1297862	3
24	2.4961586	2.6003484	2.7144777	2.8399899	2.9786231	3.1321887	3
25	2.4978204	2.6021654	2.7164719	2.8421877	2.9810563	3.1351962	3
100	2.4994848	2.6039852	2.7184693	2.8443891	2.9834936	3.1379086	3
26	2.5011515	2 6058078	2.7204698	2.8465941	2.9859352	3.1406259	3
27	2.5028207	2.6076332	2.7224735	2.8488028	2-9883811	3.1433483	3
28	2.5044923	2.6094613	2.7244804	2.8510152	2.9908312	3.1460756	3:
29	2.5061663	2.6112922	2.7261905	2.8532312	2.9932856	3-1485079	3
30	2.5078428	2.6131259	2.7285038	2.8554510	2.9957443	3.1515153 .	30
31	2.5095218	2.6149624	2.7305203	0.0570744	2.9982073	3-1542877	25
32	2.5112032	2.6168018	2.7325400	2.8576744	3.0006746	3.1570351	20
33	2.5128871	2.6186439	2.7345630	2.8599015	3.0031462	3.1597876	2
34	2.5145735	2 6204888	2.7365892	2·8621324 2·8643670	- 3.0056221	3.1625452	26
35	2.5162624	2.6223366	2.7386186	2.8666053	3.0081021	3.1653078	2:
36	0.5100500				2.0105030	A STATE OF THE PARTY OF THE PAR	1
37	2.5179537	2.6211872	2.7406512	2.8688474	3.0105870	3.1680756	24
38	2·5196475 2·5213438	2.6260406	2.7426871	2.8710932	3.0130760 3.0155694	3.1708484	23
39	2.5230426	2·6278969 2·6297560	2.7447263	2.8733428	3.0180672	3-1736264	22
40	2.5217440	2.5316180	2.7467687	2.8755961	3.0205693	3·1764095 3·1791978	21
41	STEP STEP STEP STEP STEP STEP STEP STEP		2.7488144	2.8778532	The state of the s	9 1131310	20
42	2.5264478	2.6334828	2.7508634	2.8801142	3.0230759	3.1819913	19
43	2.5281541	2.6353506	2.7529157	2.8523789	3.0255868	3.1847899	18
44	2-5298630	2.6372211	2.7549712	2.8846174	3.0281023	3-1875937	17
45	2.5315744	2.6390946	2.7570301	2.8869198	3.0306221	3.1904028	16
	2.5332883	2-6409710	2.7590923	2.8891960	3.0331464	3.1932170	15
46	2.5350048	2.6428502	2.7611578	2.8914760	3.0356752	3.1960365	14
47	2.5367238	2.6447323	2.7632267	2.8937598	3.0382084	3-1988613	13
48	2.5381153	2.6466174	2.7652988	2.8960475	3.0107463	3.2016913	12
50	2.5401694	2.6485054	2.7673744	2.8983391	3.0432884	3-2045266	11
lon	2.5418961	2.6503962	2.7694532	2.9006346	3.0458352	3-2073673	10
51	2.5436253	2.6522901	2.7715355	2.9029339	3.0483864	3.2102132	9
52	2.5453571	2.6541868	2.7736211	2.9029339	3.0509123	3.2139644	8
53	2.5470915	2.6560865	2.7757100	2.9052372	3.0535026	3.2159210	7
54	2.5483284	2.6579891	2.7778024	2.9098553	3.0560675	3.2187830	6
55	2.5505680	2.6598947	2.7798982	2.9121703	3.0586370	3.2216503	5
56	2.5523101	2.6618033		THE REAL PROPERTY.	3.0612111		
57	2.223101		2.7819973	2.9144892		3-2215230	4
58	2.5558022	2·6637148 2·6656292	2.7840999	2.9168121	3·0637898 3·0663731	3.2274011	3
59	2.5575521	2.6675467	2·7862059 2·7883153	2-9191389	3 0089610	3.2302346	2
60	2.5593047	2.6694672	2.7901281	2.9214697	3 0715535	3.5331136	0
1	ATRICA - N			2.9238044		SCHOOL STATE OF	0
	23°	22°	21°	20°	19°	18°	

•	72°	73°	74°	75°	76°	77°	
0	3-2360680	3-4203036	3.6279553	3.8637033	4.1335655	4-4454115	6
1	3.2389678	3.4235611	3.6316395	3-8679025	4.1383939	4.4510198	5
2	3.2418732	3-4268251	3.6353316	3.8721112	4.1432339	4.4566428	1 5
3	3-24-178-10	3.4300956	3.6390315	3.8763293	4.1480856	4.4622803	5
4	3-2477003	3.4333727	3.6427392	3.8805570	4.1529491	4.4679324	5
5	3.2506222	3.4366563	3.6164548	3.8847943	4.1578243	4.4735993	5
	9 2000222	9 200000	9 0101010	9 0071979	2 1010220		100
6	3.2535496	3.4399465	3.6501783	3-8890411	4.1627114	4.4792810	5
7	3.2564825	3.4432433	3-6539097	3.8932976	4.1676102	4-4819775	5
8	3-2594211	3.4465467	3.6576491	3.8975637	4.1725210	4.4906889	1
9	3.2623652	3.4498568	3.6613961	3.9018395	4.1774138	4.4964152	1
10							1
	3.2653149	3.4531735	3.6651518	3.9061250	4.1823785	4.5021565	
11	3.2682702	3.4564969	3.6689151	3.9104203	4.1873252	4.5079129	1 4
12	3.2712311	3.4598269	3.6726865	3.9147254	4.1922810	4.5136814	1
13	3.2741977	3.4631637	3.6761660	3.9190403	4.1972549	4.5194711	1
14	3.2771700	3.4665073			4.2022380	4.5252730	1
15			3.6802536	3.9233651			11110
10	3.2801479	3.4698576	3.6810193	3.9276997	4.2072333	4.5310903	1
16	3.2831316	3.4732146	3.6878532	3.9320143	4.2122408	4.5369229	1
17	3.2861209	3.4765785	3.6916652	3.9363988	4.2172606	4.5427709	
18							
19	3.2891160	3-1799192	3.6951854	3.9407633	4-2222928	4.5186311	1
	3.2921168	3-4833267	3.6993139	3.9451379	4.2273373	4.5515134.	
0	3.2951234	3.4867110	3.7031506	3-9195221	4.2323943	4.2601080	1
1	3-2981357	3.4901023	3.7069956	3-9539171	4.2374637	4.5663183	
9							
	3.3011539	3.4935004	3.7108489	3.9583219	4-2125457	4.5722444	
23	3.3041778	3-4969055	3.7147105	3.9627369	4.2476402	4.5781862	
4	3.3072076	3.5003175	3.7185805	3.9671621	4.2527474	4.5841439	1
5	3.3102433	3.5037365	3-7224589	3.9715975	4-2578671	4.5901174	1
6	3-3139847	4.5091005	3.7263157	9,0900191	4.0000000	4.5003000	1
	00101011	3.5071625		3.9760431	4.2629996	4.5961070	
7	3.3163320	3.5105954	3.7302109	3.9804991	4.2681449	4 6021126	1
8	3.3193853	3.5140354	3.7341446	3.9819651	4.2733029	4.6081343	1
19	3.3224444	3.5174824	3.7380568	3.9894:21	4-2784733	4.6141722	1 3
10	3.3255095	3-5209365	3.7419775	3-9939292	4-2836576	4.6202263	
1	3-3285805	3.5243977	3.7459063	3-9984267	4.2888513	4.6262967	1
2	3.3316575	3.5278660	3.7498447	4.0029317	4.2940640	4.6323835	1
3	3.3347405	3.5313414	3.7537911	4.0074533	4.2992867	4.6384867	1 5
4	3.3378294	3-5348240	3.7577462	4.0119823	4.3045225	4.6146061	1 9
5	3-3409214	3.5383138	3.7617100	4.0165219	4-3097715	4.6507427	1 5
		ALTERNATION CO.		2 0100210	7 0001110	Z 0001221	1
6	3-3440254	3.5418107	3.7656821	4.0210723	4.3150336	4.6568956	1 9
7	3-3171321	3.5453149	3.7696636	4.0256332	4.3203090	4.6630652	1 5
8	3.3502455	3.5488263	3.7736535	4.0302048	4.3255977	4.6092516	
9	3.3533617	3.5523450	3.7776522	4.0347872	4.3308996		
o l						4.6754518	1 9
"	3-3564900	3.5558710	3.7816596	4-0393804	4.3362150	4.6816748	1 3
1	3:3596214	3.5591042	3.7856760	4.0439844	4:3415438	4-6879119	1
2	3.3627589	3-5629448	3.7897011	4.0485992	4.3468861	4.6941660	li
3	3.3659026	3.5661928	3.7937352	4.0032249	4.3522419		
	3.3690524		3.7977782	4.0578615	4.3576113	4.7004372	1
5		3.5700481				4.7067256	1
'	3-3722084	3.5736108	3.8018301	4.0625091	4.3629943	4.7130313	1
3	3.3753707	3-5771810	3-8058911	4.0671677	4.3683910	4.7193549	1
	3.3785391	3.5807586	3.8099610	4.0718374	4.3738015		
						4.7256945	1
-	3.3817138	3.5813137	3-8140399	4.0765181	4-3792257	4.7320521	1
	3.3848948	3.5879362	3.8181280	4.0812100	4.3846638	4.7381277	1
	3.3880820	3.5915363	3.8222251	4.0859160	4.3901158	4.7448206	1
	3.3912755	3-5951439	3.8263313	4.0906273	4:3955817		1
	0 00					4.7512313	1
	3.3911754	3.5987590	3.8304467	4.0953526	4.4010616	4.7576596	1
	3.3976816	3.6023818	3.8345713	4.1000893	4.4065556	4.7641058	1
	3.4008941	3.6060121	3.8387052	4.1048374	4.4120637	4.7705699	
	3.1011130	3.6096501	3.8428482	4.1095967	4.4175859	4.7770519	1
						AND RESIDENCE OF THE PARTY OF T	1
	3.4073382	3.6132957	3.8470006	4.1143675	4-4231224	4.7835520	
	3-4105699	3.6169490	3.8511622	4.1191498	4.4286731	4.7900703	
	3.4138080	3.6206101	3.8553332	4-1:239435	4.4312382	4.7966066	
	3-4170526	3 6242758	3-8595135	4.1287487	4.4398176	4.8031613	
	3.4203036	3-6279553	3.8637033	4.1335655	4-4454115	4.8097343	1
1						2 0031010	1
	17°	16°	15°	14°	13°	12°	1

			SEC.	ANTS.			
,	78°	79°	80°	81°	82°	83°	1,
0	4.8097343	5-2408431	5-7587705	6.3924532	7.1852965	8.2055090	60
1	4.8163258	5.2186979	5.7682867	6.4042154	7.2001996	8-2249952	59
2	4.8229357	5-2565768	5.7778350	6.4160216	7-2151653	8-2445748	58
3	4.8295643	5.2614798	5.7874153	6.4278719	7.2301940	8.2642485	57
4	4.8362114	5-2724070	5-7970280	6.4397666	7-2452859	8.2840171	56
5	4.8428774	5.2803587	5.8066733	6.4517059	7.2604417	8.3038812	55
6	4.8495621	5.2883347	5.8163510	6.4636901	7-2756616	8-3238415	54
7	4.8562657	5.2963354	5.8260617	6.4757195	7.2909460	8.3438986	53
8	4.8629883	5.3043608	5.8358053	6.4877944	7.3062954	8.3640534	52
9	4.8697299	5.3124109	5.8455820	6.4999148	7.3217102	8.3813065	51
10	4.8764907	5.3204860	5.8553921	6.5120812	7-3371909	8-4046586	50
11	4.8832707	5.3285861	5.8652356	6.5242938	7.3527377	8.4251105	49
12	4.8900700	5.3367114	5.8751128	6.5365528	7.3683512	8.4456629	48
13	4 8968886	5.3448620	5.8850238	6.5488586	7.3840318	8.4663165	47
14	4.9037267	5.3530379	5-8949688	6.2612113	7.3997798	8.4870721	46
15	4.9105844	5.3612393	5-9049479	6.5736112	7.4155959	8.5079301	45
16	4.9174616	5.3694664	5.9149614	6.5860587	7.4314803	8.5288923	44
17	4 9243586	5-3777192	5.9250095	6.5985540	7-4474335	8-5499584	43
18	4.9312754	5.3859979	5.9350922	6.6110973	7.4631560	8.5711295	42
19 20	4.9382120	5.3943026	5.9452098	6.6236890	7-4795482	8.5924065	41
1	4.9451687	5.4026333	5-9553625	6.6363293	7-4957106	8.6137901	40
21	4.9521453	5.4109903	5.9655504	6.6190184	7.5119437	8.6352812	39
22	4.9591421	5.4193737	5.9757737	6.6617568	7.5282478	8.6568805	38
23	4.9661591	5.4277835	5.9860326	6.6745446	7.5416236	8.6785889	37
24 25	4.9731964	5-4362199	5-9963274	6.6873822	7.5610713	8.7001071	36
	4.9802541	5.4446831	6.0066581	6.7002699	7.5775916	8.7223361	35
26	4 9873323	5.4531731	6.0170250	6.7132079	7.5941849	8.7443766	34
27	4.9944311	5.4616901	6.0274282	6.7261965	7.6108516	8-7665295	33
28	5.0015505	5.4702342	6.0378680	6.7392360	7.6275923	8.7887957	32
30	5.0086907	5.4788056	6.0483445	6.7523268	7.6444075	8-8111761	31
1.55	5.0158517	5-4874043	6.0588580	6.7654691	7.6612976	8.8336715	30
31	5.0230337	5.4960305	6.0694085	6.7786632	7.6782631	8.8562828	29
32	5.0302367	5.5046843	6.0799964	6.7919095	7-6953047	8 8790109	28
34	5.0374607	5.5133659	6-0906219	6.8052082	7.7124227	8.9018567	27
35	5·0447060 5·0519726	5·5220754 5·5308129	6·1012850 6·1119861	6·8185597 6·8319642	7.7296176 7.7468901	8-9248211	.26
	A Company of the last			Charles J. M.	And in case of the	8.9479051	25
36	5 0592606	5.5395786	6.1227253	6.8454222	7.7642406	8.9711095	24
38	5.0665701	5.5483726	6.1335028	6.8589338	7.7816697	8-9944354	23
39	5.0739012	5.5571951	6.1443189	6.8721995	7-7991778	9.0178837	22
40	5.0812539 5.0886284	5.5660460 5.5749258	6·1551736 6·1660674	6·8861195 6·8997942	7·8167656 - 7·8344335	9.0414553	21
					- 1.9944999	9.0651512	20
41	5.0960248	5.5838343	6.1770003	6.9135239	7-8521821	9-0889725	19
42	5.1034431	5.5927719	6-1879725	6.9273089	7-8700120	9.1129200	18
44	5.1108835	5.6017386	6.1989843	6.9411496	7.8879238	9-1369949	17
45	5·1183461 5·1258309	5·6107345 5·6197599	6·2100359 6·2211275	6-9550464	7.9059179	9.1611980	16
1				6.9689991	7.9239950	9.1855305	15
46	5.1333381	5.6288148	6.2322594	6.9830092	7-9421556	9.2099934	14
48	5.1408677	5.6378995	6.2434316	6.9970760	7-9604003	9.2345877	13
49	5-1484199	5.6470140	6.2546446	7.0112001	7.9787298	9.2593145	12
50	5·1559948 5·1636924	5.6551584 5.6653331	6·2658984 6·2771933	7·0253820 7·0396220	7.9971445	9-2841749	11
51	SECOND NOTES				8.0156450	9-3091699	10
59	5.1712128	5.6745380	6.2885295	7.0539205	8.0342321	9.3313006	9
53	5.1788563	5.6837734	6.2999073	7.0682777	8.0529062	9.3595682	8
54	5·1865228 5·19±2125	5·6930393 5·7023360	6:3113269 6:3227884	7-0826941 7-0971700	8.0716681	9.3849738	7
55	5.2019254	5.7116636	6.3342923	7.1117059	8.0905182 8.1094573	9·4105184 9·4362033	6
56						STATE OF THE PARTY	5
57	5.2096618	5.7210223	6-3458386	7.1263019	8-1284860	9-4620296	4
58	5·2174216 5·2252050	5.7304121	6.3574276	7:1409587	8-1476048	9.4879984	3
69	5.2330121	5·7398333 5·7492861	6·3690595 6·3807347	7·1556764 7·1704556	8·1668145 8·1861157	9·5141110 9·5403686	2
60	5-2408431	5.7587705	6.3924532	7.1852965	8.2055090	9.5103086	1 0
1							1.
0.00	11°	10°	- 8°	8°	7°	6°	1
1		4.00			100	34.8	1

			SEC	ANTS.			
,	84°	85°	86°	_ 87°	88°	89°	
0	9.5667722	11-473713	14:335587	19-107323	28-653708	57-298688	60
1	9.5933233	11.511990	14.395471	19:213970	28.894398	58-269755	59
2	9.6200229	11.550523	14-455859	19:321816	29 139169	59-274308	58
3	9-6468724	11-589316	14.516757	19.430882	29.388124	60-314110	57
4	9-6738730	11.628372	14.578172	19-541187	29.641373	61.391050	56
5	9.7010260	11-667693	14.640109	19-652754	29-899026	62 507153	55
3/4	and total distribution	121000	THE PERSON NAMED IN				
6	9-7283327	11.707283	14.702576	19.765604	30.161201	63.664595	54
7	9.7557944	11-747141	14-765580	19.879758	30.428017	64 865716	53
8	9.7834124	11-787274	14-829128	19-995241	30-699598	66.113036	52
9	9-8111880	11.827683	14.893226	20.112075	30.976074	67-409272	51
10	9.8391227	11.868370	14.957882	20.230284	31.257577	68.757360	50
11	9.8672176	11-909340	15-023103	20-349893	31-544246	70-160474	49
12	9.8954744	11-950595	15-088896	20.470926	31-836225	71-622052	48
13	9.9238943	11-992137	15-155270	20-593409	32-133663	73-145827	47
14	9-9524787°	12.033970	15-222231	20:717368	- 32-436713	74-735856	46
15	9.9812291	12.076098	15.289788	20.842830	32-745537	76-396554	45
16	10.010147	12-118523	35,359040	00.000001	0.0.000000		
17	10.039234		15:357949	20 969824	33-060300	78-132742	44
		12:161246	15-426721	21.098376	33-381176	79-949684	43
18	10.068491	12-204274	15-496114	21.228515	33.708345	81 853150	43
19 20	10·097920 10·127522	12·247608 12·291252	15.566135	21:360273	34.041994	83-849170	41
20	10-12/022	12.291232	15-636793	21.493676	34-382316	85-945609	40
21	10.157300	12-335210	15.708096	21.628759	34.729515	88-149244	39
22	10.187254	12.379484	15.780054	21.765553	25.083800	90.468863	38
23	10.217386	12-424078	15.852676	21-904090	35-445391	92-913869	37
24	10-247697	12.468995	-15-925971	22.044403	35-814517	95-494711	36
25	10-278190	12.514240	15-999948	22 1865 28	36-191414	98-223033	35
26	10.308866	12-559815	16-074617	22:330499	36-576332	101-11185	34
	10.339726	12.605724	16.149987				
27	10.370772	12.651971	16.226069	22·476353 22·624126	36·969528 37·371273	104·17574 107·43114	33
29	10-402007	12.698560	16:302873	22:773857	37-781849		31
30	10.433431	12.745495	16:380408	22-773837	38-201550	110-89656 114-59301	30
Vo	10 300201	• 12	10 300 100	22 920000	99.701990	114.03901	
81	10.465046	12.792779	16-458686	23.079351	38-630683	118-54440	29
32	10.496854	12.840416	16.537717	23-235196	39-069571	122.77803	28
23	10.528857	12.888410	16.617512	23-393161	39-518549	127-32526	27
34	10.561057	12.936765	16-698082	23.553291	39-977969	132-22229	26
85	10.593455	12.985486	16-779439	23.715630	40-448201	137-51108	25
36	10-626054	13-034576	16-861594	23-880224	40-929630	143-24061	24
37	10.658854	13.084040	16.944559	24 .047121	41.422660	149-46837	23
38	10 691859	13-133882	17.028346	24-216370	41.927717	156.26228	29
39	10.725070	13:184106	17.112966	24.388020	42 445245	163.70325	21
40	10.758488	13-234717	17-198434	24.562123	42-975713	171.88831	20
20							
41	10.792117	13:285719	17-284761	24.738731	43.519612	180 93496	19
42	10-825957	13-337116	17.371960	24-917900	44 077458	190-98680	18
43	10.860011	13.388914	17.460046	25.099685	44.619795	203-22123	17
44	10.894281	13.441118	17.549030	25.284144	45-237195	214-85995	16
45	10-928768	13-493731	17-638928	25.471337	45-840260	229.18385	15
46	10.963476	13-546758	17-729753	25-661324	46:459625	245-55402	14
47	10-998406	13-600205	17-821520	25.854169	47-095961	264-44269	13
48	11.033560	13-654077	17-914243	26.049937	47-749974	286-17948	12
49	11.068940	13.708379	18.007937	26-248694	48-422411	312-52297	111
50	11-104549	13.763115	18-102619	26.450510	49.114062	343-77516	10
	The state of the s						10 316
51	11-140389	13.818291	18-198303	26.655455	49.825762	381-97230	9
52	11-176462	13-873913	18-295005	26.863603	50-558396	429.71873	8
53	11-212770	13-929985	18-392742	27-075030	51.312902	491 10702	7
54	11-249316	13-986514	18-491530	27-289814	52-090272	572-95809	6
55	11.286101	14-043504	18-591387	27.508035	52.891564	687-54960	5
56	11.323129	14-100963	18-692330	27-729777	53-717896	859-43689	4
57	11.360402	14.158894	18-794377	27-955125	54-570464	1145-9157	3
58	11.397922	14.217304	18-897545	28.184168	55-450534	1718-8735	2
59	11-435692	14-276200	19.001854	28-416997	56.359462	3437-7468	1
60	11.473713	14.335587	19.107323	28-653708	57-298688	Infinite.	0
	AND			00	40	0°	1
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	1	Tang	Cotang	Tang	Cotang	Tang	Cotang	Tang	Cotang	1
	012345678910	.00000 .00029 .00058 .00087 .00116 .00145 .00175 .00204 .00233 .00262 .00291	Infinite, 3437.75 1718.87 1145.92 859.436 687.549 572.957 491.106 429.718 381.971 343.774	.01746 .01775 .01804 .01833 .01862 .01891 .01920 .01949 .01978 .02007 .02036	57.2900 56.3506 55.4415 54.5613 53.7086 52.8821 52.0807 51.3032 50.5485 49.8157 49.1039	.03492 .03521 .03550 .03579 .03609 .03638 .03667 .03696 .03725 .03754	28. 6363 28. 3994 28. 1664 27. 9372 27. 7117 27. 4899 27. 2715 27. 0566 26. 8450 26. 6367 26. 4316	05241 05270 05299 05328 05357 05387 05416 05445 05474 05503 05533	19.0811 18.9755 18.8711 18.7678 18.6656 18.5645 18.4645 18.3655 18.2677 18.1708 18.0750	60 59 58 57 56 55 54 53 52 51
	11 12 13 14 15 16 17 18 19 20	.00820 .00349 .00378 .00407 .00436 .00465 .00495 .00534 .00553 .00582	312.521 286.478 264.441 245.552 229.182 214.858 202.219 190.984 180.932 171.885	.02066 .02095 .02124 .02153 .02182 .02211 .02240 .02269 .02298 .02328	48.4121 47.7395 47.0853 46.4489 45.8294 45.2261 44.6386 44.0661 43.5081 42.9641	.03812 .03842 .03871 .03900 .03929 .03958 .03987 .04016 .04046 .04075	26.2296 26.0307 25.8348 25.6418 25.4517 25.2644 25.0798 24.8978 24.7185 24.5418	.05562 .05591 .05620 .05649 .05678 .05708 .05737 .05766 .05795 .05824	17.9802 17.8863 17.7934 17.7015 17.6106 17.5205 17.4314 17.3432 17.2558 17.1693	49 48 47 46 45 44 43 42 41 40
	21 22 23 24 25 26 27 28 29 30	.00611 .00640 .00669 .00698 .00727 .00756 .00785 .00815 .00844 .00873	163,700 156,259 149,465 143,237 137,507 132,219 127,321 122,774 118,540 114,589	.02357 .02386 .02415 .02444 .02473 .02502 .02531 .02560 .02589 .02619	42,4835 41,9158 41,4106 40,9174 40,4358 39,9655 39,5059 39,0568 38,6177 38,1885	.04104 .04133 .04162 .04191 .04220 .04250 .04279 .04308 .04337 .04366	24.3675 24.1957 24.0263 23.8593 23.6945 23.5321 23.3718 23.2137 23.0577 22.9038	.05854 .05883 .05912 .05941 .05970 .05999 .06029 .06058 .06087 .06116	17.0837 16.9990 16.9150 16.8319 16.7496 16.6681 16.5874 16.5075 16.4283 16.3499	39 38 37 36 35 34 33 32 31 30
	31 32 33 34 35 36 37 38 39 40	.00902 .00931 .00960 .00989 .01018 .01047 .01076 .01105 .01135	110.892 107.426 104.171 101.107 98.2179 95.4895 92.9085 90.4633 88.1436 85.9398	.02648 .02677 .02706 .02735 .02764 .02793 .02822 .02851 .02881 .02910	37.7686 37.3579 36.9560 36.5627 36.1776 35.8006 35.4313 35.0695 34.7151 34.3678	.04395 .04424 .04454 .04483 .04512 .04541 .04570 .04599 .04628 .04658	22.7519 22.6020 22.4541 22.3081 22.1640 22.0217 21.8813 21.7426 21.6056 21.4704	.06145 .06175 .06204 .06233 .06262 .06291 .06321 .06350 .06379	16.2722 16.1952 16.1190 16.0485 15.9687 15.8945 15.8211 15.7483 15.6762 15.6048	29 28 27 26 25 24 23 22 21 20
	41 42 43 44 45 46 47 48 49 50	.01193 .01222 .01251 .01280 .01309 .01308 .01367 .01396 .01425 .01455	83.8435 81.8470 79.9434 78.1263 76.3900 74.7292 73.1390 71.6151 70.1533 68.7501	.02939 .02968 .02997 .03026 .03055 .03084 .03114 .03143 .03172 .03201	34.0273 33.6935 33.3662 33.0452 32.7303 32.4213 32.1181 31.8205 31.5284 31.2416	.04687 .04716 .04745 .04774 .04803 .04833 .04862 .04891 .04920 .04949	21.3369 21.2049 21.0747 20.9460 20.8188 20.6032 20.5691 20.4465 20.3253 26.2056	.06437 .06467 .06496 .06525 .06554 .06584 .06613 .06642 .06671	15.5340 15.4638 15.3943 15.3254 15.2571 15.1893 15.1222 15.0557 14.9898 14.9244	19 18 17 16 15 14 13 12 11 10
	51 52 53 54 55 56 57 58 59 60	.01484 .01513 .01542 .01571 .01600 .01629 .01658 .01687 .01716 .01746	67, 4019 66, 1055 64, 8580 63, 6567 62, 4992 61, 3829 60, 3058 59, 2659 58, 2612 57, 2900	.03230 .03259 .03288 .03317 .03346 .03376 .03405 .03434 .03463 .03492	30.9599 30.6833 30.4116 30.1446 29.8823 29.6245 29.3711 29.1220 28.8771 28.6363	.04978 .05007 .05037 .05066 .05095 .05124 .05153 .05182 .05212 .05241	20.0872 19.9702 19.8546 19.7403 19.6273 19.5156 19.4051 19.2959 19.1879 19.0811	.06730 .06759 .06788 .06817 .06847 .06876 .06905 .06934 .06963 .06993	14.8596 14.7954 14.7317 14.6685 14.6059 14.5438 14.4823 14.4212 14.3607 14.3007	9876543210
	,	Cotang	Tang 90	Cotang	Tang 8°	Cotang	Tang	Cotang	Tang	,
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		10		-TANGE		3°		70	
1	Tang	Cotang	Tang	Cotang	Tang	Cotang	Tang	Cotang	1
0	.06993	14.3007	.08749	11.4301	.10510	9.51436	.12278	8,14435	60
1	.07022	14.2411	.08778	11.3919	.10540	9.48781	.12308	8.12481	59
	.07051	14,1821	.08807	11.3540	.10569	9.46141	.12338	8.10536	58
3	.07080	14.1235	.08837	11.3163	.10599	9.43515	.12367	8.08600	57
4	.07110	14.0655	.08866	11.2789	.10628	9.40904	.12397	8.06674	56
5 6	.07139	14.0079	.08895	11.2417	.10657	9.38307	.12426	8.04756	55
7	.07168	13.9507 13.8940	.08925	11.2048 11.1681	.10687	9.35724 9.33155	.12456	8.02848 8.00948	54 53
8	.07227	13.8378	.08983	11.1316	.10746	9.30599	12515	7.99058	52
. 9	.07256	13.7821	.09013	11.0954	.10775	9,28058	.12544	7.97176	51
10	.07285	13.7267	.09042	11.0594	.10805	9.25530	.12574	7.95302	50
11	.07314	13,6719	.09071	11.0237	.10834	9,23016	.12603	7.93438	49
12	.07344	13.6174	.09101	10.9882	.10863	9.20516	.12633	7.91582	48
13	.07373	13.5634	.09130	10.9529	.10893	9.18028	.12662	7.89734	47
14 15	.07402	13.5098 13.4566	.09159	10.9178 10.8829	.10922	9.15554 9.13093	.12692	7.87895 7.86064	46 45
16	.07461	13.4039	.09169	10.8483	.10932	9.13093	.12751	7.84242	44
17	.07490	13.3515	.09247	10.8139	.11011	9.08211	.12781	7.82428	43
118	.07519	13.2996	.09277	10.7797	.11040	9.05789	.12810	7.80622	42
19	.07548	13.2480	.09277 .09306	10.7797 10.7457	.11070	9.03379	.12840	7.78825	41
20	.07578	13.1969	.09335	10.7119	.11099	9,00983	.12869	7.77035	40
21	.07607	13.1461	.09365	10.6783	.11128	8.98598	.12899	7.75254	39
22	.07636	13.0958	.09394	10.6450	.11158	8.96227	.12929	7.73480	38
23 24	.07665	13.0458	.09423	10.6118	.11187	8.93867	.12958	7.71715	37
25	.07695	12.9962 12.9469	.09453	10.5789	.11217	8.91520 8.89185	.12988	7.69957	36
26	.07753	12.8981	.09511	10.5136	.11276	8.86862	.13047	7.66466	34
27	.07782	12,8496	.09541	10.4813	.11305	8.84551	.13076	7.64732	33
28	.07812	12.8014	.09570	10.4491	.11335	8.82252	.13106	7.63005	32
29	.07841	12.7536	.09600	10.4172	.11364	8.79964	.13136	7.61287	31
30	.07870	12.7062	.09629	10.3854	.11394	8.77689	.13165	7.59575	30
31	.07899	12.6591	.09658	10.3538	.11423	8.75425	.13195	7.57872	29
32	.07929	12.6124	.09688	10.3224	.11452	8.73172 8.70931	.13224	7.56176	28
33	.07958	12.5660	.09717	10.2913 10.2602	.11482	8.70931	.13254	7.54487 7.52806	27 26
35	.08017	12.5199	.09746	10.2294	.11541	8.66482	.13313	7.51132	25
36	.08046	12.4288	.09805	10.1988	.11570	8.64275	.13343	7.49465	24
37	.08075	12.3838	.09834	10.1683	.11600	8.62078	.13372	7.47806	23
38		12.3390	.09864	10.1381	.11629	8.59893	.13402	7.46154	22
39		12.2946	.09893	10.1080	.11()	8.57718 8.55555	.13432	7.44509 7.42871	21 20
40	CERTITION	12.2505	.09923		.11688	The second			Part .
41	.08192	12.2067	.09952	10.0483	.11718	8.53402	.13491	7.41240 7.39616	19
42		12.1632	.09981	10.0187	.11747	8.51259 8.49128	.13521	7.37999	17
44		12.1201 12.0772	.10011	9.98931	.11806	8,47007	13580	7.36389	16
45		12.0346	.10040	9.93101	.11836	8.44896	.13609	7.34786	15
46	.08339	11.9923	.10099	9.90211	.11865	8.42795	.13639	7.33190	14
47	.08368	11.9504	.10128	9.87338	.11895	8.40705	.13669	7.31600	13
48		11.9087	.10158	9.84482	.11924	8.38625 8.36555	.13698	7.30018	12
49 50		11.8673	.10187	9.81641 9.78817	.11954	8.34496	.13758	7.26873	10
1000	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	DISTRICT STATE		DESCRIPTION OF	ACCUSATION AND ADDRESS OF THE PARTY OF THE P		.13787	7.25310	9
51	.08485	11.7853	.10246	8.76009 9.73217	.12013	8.32446	.13817	7.23754	8
53		11.7448 11.7045	.10305	9.70441	12072	8.28376	.13846	7.22204	87654
54	.08573	11.6645	.10334	9.67680	.12101	8.26355	.13876	7.20661	6
55	.08602	11.6248	.10363	9.64935	,12131	8.24345	.13906	7.19125	5
56	.08632	11.5853	.10393	9.62205	.12160	8.22344 8.20352	.13935	7.17594 7.16071	3
57	.08661	11.5461 11.5072	.10422	9.59490 9.56791	.12190	8.20352	.13995	7.14553	2
59	.08720	11.4685	.10432	9.54106	.12249	8.16398	14024	7.13042	1 0
60		11.4301	.10510	9.51436	.12278	8.14435	.14054	7.11537	0
-	Cotang	Tang	Cotang	Tang	Cotang	Tang	Cotang	Tang	1,
1	-	35°		40	g	33°	9	2°	1
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		IABLI		11110211		COTANG			
1,		8° -		9°	1	10°	1	1°	1,
	Tang	Cotang		Cotang	Tang	Cotang	Tang	Cotang	_
1 2 3	.14084	7.11537 7.10038 7.08546 7.07059	.15838 .15868 .15898 .15928	6.31375 6.30189 6.29007 6.27829	.17633 .17663 .17693 .17723	5.67128 5.66165 5.65205 5.64248	.19438 .19468 .19498 .19529	5.14455 5.13658 5.12862 5.12069	60 59 58 57
4 5 6 7 8,9	.14173 .14202 .14232 .14262	7.05579 7.04105 7.02637 6.91174	.15958 .15988 .16017 .16047	6.26655 6.25486 6.24321 6.23160	.17753 .17783 .17813 .17843	5.63295 5.62344 5.61397 5.60452	.19559 .19589 .19619 .19649	5.11279 5.10490 5.09704 5.08921	56 55 54 53
8 9 10	.14291 .14321 .14351	6.99718 6.98268 6.96823	.16077 .16107 .16137	6.22003 6.20851 6.19703	.17873 .17903 .17933	5.59511 5.58573 5.57638	.19680 .19710 .19740	5.08139 5.07360 5.06584	52 51 50
11 12 13 14 15 16 17 18 19	.14381 .14410 .14440 .14470 .14499 .14529 .14559 .14588 .14618	6.95385 6.93952 6.92525 6.91104 6.89688 6.88278 6.86874 6.85475 6.84082	.16167 .16196 .16226 .16256 .16286 .16316 .16346 .16376 .16405	6.18559 6.17419 6.16283 6.15151 6.14023 6.12899 6.11779 6.10664 6.09552	.17963 .17998 .18023 .18053 .18083 .18113 .18143 .18173 .18203	5.56706 5.55777 5.54851 5.53927 5.53007 5.52090 5.51176 5.50264 5.49356	.19770 .19801 .19831 .19861 .19891 .19921 .19952 .19982 .20012	5.05809 5.05037 5.04267 5.03499 5.02734 5.01971 5.01210 5.00451 4.99695	49 48 47 46 45 44 43 42 41
20 21 22 23 24 25 26 27 28 29 30	.14648 .14678 .14707 .14737 .14767 .14796 .14826 .14856 .14886 .14915 .14945	6.82694 6.81312 6.79936 6.78564 6.77199 6.75838 6.74483 6.73133 6.71789 6.70450 6.69116	.16435 .16465 .16495 .16525 .16555 .16585 .16645 .16674 .16704 .16734	6.08444 6.07340 6.06240 6.05143 6.04051 6.02962 6.01878 6.00797 5.99720 5.98646 5.97576	.18233 .18263 .18293 .18323 .18353 .18384 .18414 .18444 .18474 .18504 .18534	5.48451 5.47548 5.46648 5.45751 5.44857 5.43076 5.42192 5.41309 5.40429 5.39552	.20042 .26373 .20103 .20133 .20164 .20194 .20254 .20254 .20285 .20315 .20345	4.98940 4.98188 4.97438 4.96690 4.95945 4.95201 4.9460 4.93721 4.92984 4.92249 4.91516	40 39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	.14975 .15005 .15034 .15064 .15094 .15124 .15153 .15183 .15213 .15243	6.67787 6.66463 6.65144 6.63831 6.62523 6.61219 6.59921 6.58627 6.57339 6.56055	.16764 .16794 .16824 .16854 .16884 .16914 .16944 .17004 .17003	5.96510 5.95448 5.94390 5.93335 5.92283 5.91236 5.90191 5.89151 5.88114 5.87080	.18564 .18594 .18624 .18654 .18684 .18714 .18745 .18775 .18805 .18835	5.38677 5.37805 5.36936 5.36070 5.35206 5.34345 5.33487 5.32631 5.31778 5.30928	.20376 .20406 .20436 .20436 .20497 .20527 .20527 .20588 .20618 .20648	4.90785 4.90056 4.89330 4.88605 4.87162 4.86444 4.85727 4.85013 4.84300	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	.15272 .15302 .15332 .15362 .15391 .15421 .15451 .15481 .15511 .15540	6.547777 6.53508 6.52234 6.50970 6.49710 6.48456 6.47206 6.45961 6.44720 6.43484	.17063 :17093 .17123 .17153 .17153 .17213 .17213 .17243 .17273 .17303 .17333	5.86051 5.85024 5.84001 5.82982 5.81966 5.80953 5.79944 5.78938 5.77936 5.76937	.18865 .18895 .18925 .18925 .18986 .19016 .19046 .19076 .19106 .19136	5.30080 5.29235 5.28393 5.27553 5.26715 5.25880 5.25048 5.24218 5.23391 6.22566	.20679 .20709 .20739 .20770 .20800 .20830 .20861 .20891 .20921 .20952	4.83590 4.82582 4.82175 4.81471 4.80769 4.80068 4.79370 4.78673 4.77978 4.77286	19 18 17 16 15 14 13 12 11 10
51 52 53 54 55 56 57 58 59 60	.15570 .15600 .15630 .15660 .15689 .15719 .15749 .15779 .15809 .15838	6.42253 6.41026 6.39804 6.38587 6.37374 6.36165 6.34961 6.32566 6.31375	.17363 .17393 .17423 .17453 .17483 .17513 .17543 .17573 .17603 .17633	5,75941 5,74949 5,73960 5,72974 5,71992 5,71013 5,70037 5,69064 5,68094 5,67128	.19166 .19197 .19227 .19257 .19287 .19317 .19347 .19378 .19408 .19438	5.21744 5.20925 5.20107 5.19298 5.18480 5.17671 5.16863 5.16058 5.15256 5.14455	.20982 .21013 .21043 .21073 .21104 .21134 .21164 .21195 .21225 .21256	4.76595 4.75906 4.75219 4.74534 4.73851 4.73170 4.72490 4.71813 4.71137 4.70463	9876543210
1	Cotang	Tang	Cotang	Tang	Cotang	Tang	Cotang	Tang	,
	81°		8	0°	7	9°	7	8°	

N		2°	1	.3°	1	4°	1	5°	1
1	Tang	Cotang	Tang	Cotang	Tang	Cotang	Tang	Cotang	1
0	.21256 .21286	4.70463 4.69791	.23087 .23117	4.33148 4.32573	.24933 .24964	4.01078 4.00582	.26795 .26826	3.73205 3.72771 3.72338	60 59
3 4	.21316 .21347 .21377	4.69121 4.68452 4.67786	.23148 .23179 .23209	4.32001 4.31430 4.30860	.24995 .25026 .25056	4.00086 3.99592 3.99099	.26857 .26888 .26920	3.72338 3.71907 3.71476	58 57 56
6 7	.21408 .21438 .21469	4.67121 4.66458	.23240 .23271 .23301	4.30291 4.29724 4.29159	.25087 .25118	3.98607 3.98117	.26951 .26982	3.71046 3.70616	55 54
8 9 10	.21499 .21529 .21560	4.65797 4.65138 4.64480 4.63825	.23332 .23363 .23393	4.28595 4.28032 4.27471	.25149 .25180 .25211 .25242	3.97627 3.97139 3.96651 3.96165	.27013 .27044 .27076 .27107	3.70188 3.69761 3.69335 3.68909	52 52 51 50
11 12 13 14 15	.21590 .21621 .21651 .21682 .21712	4.63171 4.62518 4.61868 4.61219 4.60572	.23424 .23455 .23485 .23516 .23547	4.26911 4.26352 4.25795 4.25239 4.24685	.25273 .25304 .25335 .25366 .25397	3.95680 3.95196 3.94713 3.94232 3.93751	.27138 .27169 .27201 .27232 .27263	3.68485 3.68061 3.67638 3.67217 3.66796	49 48 47 46 45
16 17 18 19 20	.21743 .21773 .21804 .21834 .21864	4.59927 4.59283 4.58641 4.58001 4.57863	.23578 .23608 .23639 .23670 .23700	4.24132 4.23580 4.23030 4.22481 4.21933	.25428 .25459 .25490 .25521 .25552	3.93271 3.92793 3.92316 3.91839 3.91364	.27294 .27326 .27357 .27388 .27419	3.66376 3.65957 3.65538 3.65121 3.64705	44 43 42 41 40
21 22 23 24 25 26 27 28 29 30	.21895 .21925 .21956 .21986 .22017 .22047 .22078 .22108 .22139 .22169	4.56726 4.56091 4.55458 4.54826 4.54196 4.53568 4.52941 4.52316 4.51693 4.51071	.23731 .23762 .23793 .23823 .23854 .23855 .23916 .23946 .23977 .24008	4.21387 4.20842 4.20298 4.19756 4.19215 4.18675 4.18137 4.17600 4.17064 4.16530	.25583 .25614 .25645 .25676 .25707 .25738 .25769 .25800 .25831 .25862	3.90890 3.90417 3.89945 3.89474 3.89004 3.88536 3.88068 3.87601 3.87136 3.86671	.27451 .27482 .27513 .27545 .27576 .27607 .27638 .27670 .27701 .27732	3.64289 3.63874 3.63461 3.63048 3.62636 3.62224 3.61814 3.61405 3.60996 3.60588	39 38 37 36 35 34 33 32 31 30
31 32 33 34 35 36 37 38 39 40	.22200 .22231 .22261 .22292 .22322 .22353 .22383 .22414 .22444 .22475	4.50451 4.49832 4.49215 4.48600 4.47986 4.47374 4.46764 4.46155 4.45548 4.44942	.24039 .24069 .24100 .24131 .24162 .24193 .24223 .24223 .24254 .24285 .24316	4.15997 4.15465 4.14934 4.14405 4.13877 4.13350 4.12825 4.12301 4.11778 4.11256	.25893 .25893 .25924 .25955 .25986 .26017 .26048 .26079 .26110 .26141 .26172	3.86208 3.85745 3.85284 3.84824 3.84364 3.83906 3.83449 3.82992 3.82537 3.82083	.27764 .27795 .27826 .27858 .27859 .27921 .27952 .27983 .28015 .28046	3.60181 3.59775 3.59870 3.58966 3.58562 3.58160 3.57758 3.57357 3.56957 3.56557	29 28 27 26 25 24 23 22 21 20
41 42 43 44 45 46 47 48 49 50	.22505 .22536 .22567 .22597 .22628 .22658 .22689 .22719 .22750 .22781	4,44338 4,43735 4,43134 4,42534 4,41340 4,40745 4,40152 4,39560 4,38969	.24347 .24377 .24408 .21439 .24170 .24501 .24532 .24562 .24593 .24624	4.10736 4.10216 4.09699 4.09182 4.08666 4.08152 4.07639 4.07127 4.06616 4.06107	.26208 .26285 .26266 .26297 .26328 .26359 .26390 .26421 .26452 .26483	3,81630 3,81177 3,80726 3,80276 3,79827 3,79827 3,78931 3,78485 3,78040 3,77595	.28077 .28109 .28140 .28172 .28203 .28234 .28266 .28297 .28329 .28360	3.56159 3.55761 3.55364 3.54968 3.54573 3.54179 3.554785 3.53785 3.5393 3.53001 3.52609	19 18 17 16 15 14 13 12 11 10
51 52 53 54 55 56 57 58 59 60	.22811 .22842 .22872 .22903 .22934 .22964 .22995 .23026 .23056 .23087	4.38381 4.37793 4.37207 4.36623 4.36040 4.35459 4.34879 4.34300 4.33723 4.33148	.24655 .24686 .24717 .24747 .24778 .24809 .24840 .24871 .24902 .24933	4.05599 4.05092 4.04586 4.04081 4.03578 4.03076 4.02574 4.02574 4.01576 4.01078	.26515 .26546 .26577 .26608 .26639 .26670 .26701 .26733 .26764 .26795	3.77152 3.76709 3.76268 3.75828 3.75388 3.74950 3.74512 3.74075 3.73640 3.78205	.28391 .28423 .28454 .28486 .28517 .28549 .28580 .28612 .28643 .28675	3.52219 3.51829 3.51441 3.51053 3.50666 3.50279 3.49894 3.49509 3.49125 3.48741	9876543210
-	Cotang	Tang	Cotang	Tang	Cotang	Tang	Cotang	Tang	-
1	7	70	H	6°	8	5°	17	40	1

			TABLE	X11.—1	ANGEN	IS AND	COTANO	ENTS.		
F	,	1	.6°	1	70	1	8°	1	9°	1
	1	Tang	Cotang	Tang	Cotang	Tang	Cotang	Tang	Cotang	1
	0	.28675 .28706	3.48741 3.48359	.30573	3.27085 3.26745	.32492	3.07768 3.07464	.34433	2.90421 2.90147	60 59
	23	.28738	3.47977	.30637	3.26406	.32556	3.07160	.34498	2.89873	58
		.28769	3.47596 3.47216	.30669	3.26067 3.25729	.32588	3.06857 3.06554	.34530	2.89600 2.89327	57 56
	4 5	.28832	3.46837	30732	3.25392	.32653	3.06252	.34596	2.89055	55
	6	.28864	3.46458	.30732	3.25055	.32685	3.05950	.34628	2.88783	54
	8	.28895	3.46080 3.45703	.30796	3.24719 3.24383	.32717	3.05649 3.05349	.34661	2.88511 2.88240	53 52
	9	.28958	3.45327	.30860	3.24049	.32782	3.05049	.34726	2.87970	51
- 1	10	.28990	3.44951	.30891	3.23714	.32814	3.04749	.34758	2 87700	50
	11	.29021	3.44576 3.44202	.30923	3.23381 3.23048	.32846	3.04450 3.04152	.34791	2.87430 2.87161	49
1	13	.29084	3.43829	.30987	3.22715	.32911	3.03854	.34856	2.86892	47
	14	.29116	3.43456 3.43084	.31019	3.22384 3.22053	.32943	3.03556 3.03260	.34889	2.86624 2.86356	46 45
1	16	.29179	3.42713	.31083	3.21722	.33007	3.02963	.34954	2.86089	44
1	17	.29210	3.42343 3.41973	.31115	3.21392 3.21063	.33040	3.02667	.34987	2.85822 2.85555	43
	19	.29274	3.41604	.31178	3.20734	.33104	3.02077	.35052	2.85289	41
	20	.29305	3.41236	.31210	3.20406	.33136	3.01783	.35085	2.85023	40
100	21.	.29337	3.40869 3.40502	.31242	3.20079	.33169	3.01489 3.01196	.35118	2.84758 2.84494	39
6	22	.29400	3,40136	.31306	3.19752 3.19426	.33233	3.00903	.35183	2.84229	37
1 %	24	.29432	3.39771	.31338	3.19100	.33266	3.00611	.35216	2.83965	36
- 9	25	.29463	3.39406 3.39042	.31370	3.18775 3.18451	.33298	3.00319 3.00028	.35248	2.83702 2.83439	35
1 %	27	.29526	3.38679	.31434	3.18127	.33363	2.99738	.35314	2.83176	33
	28	.29558	3.38317 3.37955	.31466	3.17804 3.17481	.33395	2.99447 2.99158	.35346	2.82914 2.82653	32
100	30	.29621	3.37594	.31530	3.17159	.33460	2.98868	.35412	2.82391	30
	31	.29653	3.37234	.31562	3.16838	.33492	2.98580	.35445	2.82130	29
000	32	.29685	3.36875 3.36516	.31594	3.16517 3.16197	.33524	2.98292 2.98004	.35477	2.81870 2.81610	28
16	34	.29748	3.36158	.31658	3.15877	.33589	2.97717	.35543	2.81350	26
	35	.29780 .29811	3.35800 3.35443	.31690 .31722	3.15558 3.15240	.33621	2.97430 2.97144	.35576	2.81091 2.80833	25
1	37	.29843	3.35087	.31754	3.14922	.33686	2.96858	.35641	2.80574	23
	38	.29875	3.34732 3.34377	.31786	3.14605 3.14288	.33718	2.96573 2.96288	.35674	2.80316 2.80059	22 21
	10	.29938	3.34023	.31850	3.13972	.33783	2.96004	.35740	2.79802	20
	11	.29970	3.33670	.31882	3.13656	.33816	2.95721	.35772	2.79545	19
	12	.30001	3.33317 3.32965	.31914	3.13341 3.13027	.33848	2.95437 2.95155	.35805	2.79289 2.79033	18 17
14	14	.30065	3.32614	.31978	3.12713	.33913	2.94872	.35871	2.78778	16
	15	.30097	3.32264 3.31914	.32010	3.12400 3.12087.	.33945	2.94591 2.94309	.35904	2.78523 2.78269	15 14
4	17	.30160	3.31565	.32074	3.11775	.34010	2.94028	.35969	2.78014	13
	18	.30192	3.31216 3.30868	.32106	3.11464 3.11153	.34043	2.93748 2.93468	.36002	2.77761 2.77507	12 11
	50	.30255	3.30521	.32171	3.10842	.34108	2.93189	.36068	2.77254	10
	51	.30287	3.30174	.32203	3,10532	.34140	2.92910	.36101	2.77002	9
1	53	.30319	3.29829 3.29483	.32235	3.10223 3.09914	.34173	2.92632 2.92354	.36134	2.76750 2.76498	8
1	54	*.30382	3.29139	.32299	3.09606	.34238	2.92076	.36199	2.76247	6 5
	55	.30414	3.28795 3.28452	.32331	3.09298 3.08991	.34270	2.91799 2.91523	.36232	2.75996 2.75746	5 4
1	57	.30478	3.28109	.32396	3.08685	.34335	2.91246	.36298	2.75496	3
	58	.30509	3.27767 3.27426	.32428	3.08379 3.08073	.34368	2.90971 2.90696	.36331 .36364	2.75246 2.74997	2
	30	.30573	3.27085	.32492	3.07768	.34433	2.90421	.36397	2.74748	0
	,	Cotang	Tang	Cotang	Tang	Cotang	Tang	Cotang	Tang	,
		7	3°	7	2°	7	1°	7	0°	

			TABLE	. AII.—	ANGEN	IS AND	COLANG	ENIS.		
	,	2	0°	2	1°	2	2°	2	3°	1,
1		Tang	Cotang	Tang	Cotang	Tang	Cotang	Tang	Cotang	
1	0	.36397	2.74748	.38386	2.60509	.40403	2.47509	.42447	2.35585	60
1	1 9	.36430	2.74499 2.74251	.38420	2.60283 2.60057	.40436	2.47302 2.47095	.42482	2.35395 2.35205	59 58
1	3	.36496	2.74004	.38487	2.59831	.40504	2.46888	.42551	2.35015	57
1	123456	.36529	2.73756	.38520	2.59606	.40538	2.46682	.42585	2.34825 2.34636	56
1	6	.36562	2.73509 2.73263	.38553	2.59381 2.59156	.40572	2.46476 2.46270	.42619	2.34447	55
1	7 8	.36628	2.73017	.38620	2.58932	.40640	2.46065	.42688	2.34258	53
1	8 9	.36661	2.72771 2.72526	.38654	2.58708 2.58484	.40674	2.45860 2.45655	.42722 .42757	2.34069 2.33881	52 51
	10	.36694	2.72281	.38721	2.58261	.40741	2.45451	42791	2.33693	50
-	11	.36760	2.72036	.38754	2.58038	.40775	2.45246	.42826	2.33505	49
	12	.36793	2.71792	.38787	2.57815	.40809	2.45043	.42860	2.33317	48
	13	.36826	2.71548	.38821	2.57593	.40843	2.44839	.42894	2.33130	47
	14 15	.36859	2.71305 2.71062	.38854	2.57371 2.57150	.40911	2.44636 2.44433	.42963	2.32943 2.32756	45
	16	.36925	2.70819	.38921	2.56928	.40945	2.44230	.42998	2.32570	44
	17 18	.36958	2.70577 2.70335	.38955	2.56707 2.56487	.40979	2.44027 2.43825	.43032	2.32383 2.32197	43 42
-	19	.36991	2.70094	.39022	2.56266	.41047	2.43623	.43101	2.32012	41
	20	.37057	2.69853	.39055	2.56046	.41081	2.43422	.43136	2.31826	40
	21	.37090	2.69612	.39089	2.55827	.41115	2.43220	.43170	2.31641	39
1	22 23	.37123	2.69371 2.69131	.39122	2.55608 2.55389	.41149	2.43019 2.42819	.43205	2.31456 2.31271	38
	24	.37157	2.68892	39190	2.55170	.41217	2.42618	.43274	2.31086	36
	25	.37223	2.68653	.39223	2.54952	.41251 .41285	2.42418	.43308	2.30902	35
	26 27	.37256 .37289	2.68414 2.68175	.39257	2.54734 2.54516	.41285	2.42218 2.42019	.43343	2.30718 2.30534	34
	28	.37322	2 67937	.39324	2.54299	.41353	2.41819	.43412	2.30351	32
	29	.37355	2.67700	.39357	2.54082	.41387	2.41620	.43447	2.30167 2.29984	31
	30	.37388	2.67462	.39391	2.53865	.41421	2.41421	1 3 3 3 3 4 1 1 1	14 10000000	29
1	31	.37422	2.67225 2.66989	.39425	2.53648 2.53432	.41455	2.41223 2.41025	.43516	2.29801 2.29619	28
	33	.37488	2.66752	.39492	2.53217	.41524	2.40827	.43585	2.29437	27
	34	.37521	2.66516	.39526	2.53001	.41558	2.40629 2.40432	.43620	2.29254 2.29073	26 25
	35 36	.37554	2.66281 2.66046	.39559	2.52786 2.52571	.41592	2.40432	.43689	2.28891	24
	37	.37621	2.65811	.39626	2.52357	.41660	2.40038	.43724	2.28710	23
1	38	.37654	2.65576	.39660	2.52142 2.51929	.41694 .41728	2.39841 2.39645	.43758	2.28528 2.28348	21
	40	.37687	2.65342 2.65109	.39694	2.51715	.41763	2.39419	.43828	2.28167	20
	41	.37754	2.64875	.39761	2.51502	.41797	2.39253	.43862	2.27987	19
	42	.37787	2.64642	.39795	2.51289	.41831	2.39058	.43897	2.27806	18
-	43	.37820	2.64410	.39829	2.51076 2.50864	.41865 41899	2.38863 2.38668	.43932	2.27626 2.27447	17
	45	.37853	2.64177 2.63945	.39896	2,50652	.41933	2.38473	.44001	2.27267	15
	46	.37920	2.63714	.39930	2.50440	.41968	2.38279	.44036	2.27088 2.26909	14
1	47	.37953	2.63483 2.63252	.39963	2.50229 2.50018	.42002	2.38084 2.37891	.44071	2.26730	12
	49	.38020	2.63021	.40031	2.49807	.42070	2.37697	.44140	2.26552	11
	50	.38053	2.62791	.40065	2.49597	.42105	2.37504	.44175	2.26374	10
1	51	.38086	2.62561	.40098	2.49386	.42139	2.37311	.44210	2.26196 2.26018	9
	52 53	.38120	2.62332 2.62103	.40132	2.49177 2.48967	.42173	2.37118 2.36925	.44279	2.25840	8 7
	54	.38186	2.61874	.40200	2.48758	.42242	2.36733	.44314	2.25663	6
	55	.38220	2.61646	.40234	2.48758 2.48549	.42276	2.36541 2.36349	.44349	2.25486 2.25309	5
	56 57	.38253	2.61418 2.61190	.40267	2 48340 2.48132	.42310	2.36158	.44418	2.25132	3 2 1
	58	.38320	2.60963	.40335	2.47924	.42379	2.35967	.44453	2.24956	2
	59	.38353	2.60736	.40369	2.47716 2.47509	.42413	2.35776 2.35585	.44488	2.24780 2.24604	0
-	60	.38386	2.60509 Tang	.40403 Cotang	Tang	Cotang	Tang	Cotang	Tang	-
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-		6	90	6	80	6	70	6	6°	

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'	Tang	Cotang	Tang	Cotang	Tang	Cotang	Tang	Cotang	1
0	.44523	2.24604	.46631	2.14451	.48773	2.05030	.50953	1.96261	60
1	.44558	2.21428	.46666	2.14288	.48809	2.04879	.50989	1.96120	59
1 2 3	.44593	2.24252	.46702	2.14125	.48845	2.04728 2.04577	.51026	1.95979 1.95838	58
4	.44627 .44662	2.24077 2.23902	.46737	2.13963 2.13801	.48917	2.04377	.51003	1.95698	56
5	.44697	2.23727	46808	2.13639	48953	2.04276	.51136	1.95557	55
6	.44732	2.23553	.46843	2.13477	.48989	2.04125	.51173	1.95417	54
789	.44767	2.23378	.46879	2.13316	.49026	2.03975	.51209	1.95277	53
8	.44802	2.23204	.46914	2.13154	.49062	2.03825	.51246	1.95137	52
	.44837	2.23030	.46950	2.12993	.49098	2.03675	.51283	1.94997	51
10	.44872	2.22857	.46985	2.12832	.49134	2.03526	.51319	1.94858	50
11	.44907	2.22683	.47021	2.12671	.49170	2.03376	.51356	1.94718	49
12	.44942	2.22510	.47056	2.12511	.49206	2.03227	.51393	1.94579	48
13 14	.44977	2.22337 2.22164	.47092	2.12350 2.12190	.49242	2.03078 2.02929	.51430	1.94440 1.94301	47
15	.45013	2.21992	.47163	2.12030	.49315	2.02780	.51503	1.94162	45
16	.45082	2.21819	.47199	2,11871	.49351	2.02631	.51540	1.94023	44
17	.45117	2.21647	.47234	2.11711	.49387	2.02483	.51577	1.93885	43
18	.45152	2.21475	.47270	2.11552	.49423	2.02335	.51614	1.93746	42
19	.45187	2.21304	.47305	2.11392	.49459	2.02187	.51651	1.93608	41
20	.45222	2.21132	.47341	2.11233	.49495	2.02039	.51688	1.93470	40
21	.45257	2.20961	.47377 .47412	2.11075	.49532	2.01891	.51724	1.93332	39
22	.45292	2.20790	.47412	2.10916	.49568	2.01743	.51761	1.93195	38
23 24	.45327	2.20619	.47448	2.10758	.49604	2.01596	.51798	1.93057 1.92920	37
25	.45362	2.20449 2.20278	.47483	2.10600 2.10442	.49640	2.01449 2.01302	.51872	1.92920	35
26	.45432	2.20108	.47555	2.10284	.49713	2.01155	.51909	1.92645	34
27	.45467	2.19938	.47590	2.10126	.49749	2.01008	.51946	1.92508	33
28	.45502	2.19769	.47626	2.09969	.49786	2.00862	.51983	1.92371	32
29	.45538	2.19599	.47662	2.09811	.49822	2.00715	.52020	1.92235	31
30	.45573	2.19430	.47698	2.09654	.49858	2.00569	.52057	1.92098	30
31	.45608	2.19261	.47733	2.09498	.49894	2.00423	.52094	1.91962	29
32	.45643	2.19092	.47769	2.09341	.49931	2.00277	.52131	1.91826	28
33	.45678	2.18923	.47805	2.09184	.49967	2.00131	.52168	1.91690	27
34 35	.45713	2.18755	.47840	2.09028 2.08872	.50004	1.99986	.52205	1.91554	26 25
36	.45748	2.18587 2.18419	.47912	2.08716	.50040	1.99841 1.99695	.52279	1.91418 1.91282	24
37	.45819	2.18251	47948	2.08560	.50113	1.99550	.52316	1.91147	23
38	.45854	2.18084	.47984	2.08405	.50149	1.99406	.52353	1.91012	22
39	.45889	2.17916	.48019	2.08250	.50185	1.99261	.52390	1.90876	21
40	.45924	2.17749	.48055	2.08094	.50222	1.99116	.52427	1.90741	20
41	.45960	2.17582	.48091	2.07939	.50258	1.98972	.52464	1.90607	19
42	.45995	2.17416	.48127	2.07785	.50295	1.98828	.52501	1.90472	18
43	.46030	2.17249 2.17083	.48163	2.07630	.50331	1.98684	.52538	1.90337	17
44 45	.46065	2.17083	.48198	2.07476 2.07321	.50368	1.98540	.52575	1.90203	16
46	.46101 .46136	2.16917 2.16751	.48270	2.07167	.50404	1.98396 1.98253	.52650	1.89935	14
47	.46171	2.16585	.48306	2.07014	.50477	1.98110	.52687	1.89801	13
48	.46206	2.16420	.48342	2.06860	.50514	1.97966	.52724	1.89667	12
49	.46242	2.16255	.48378	2.06706	.50550	1.97823	.52761	1.89533	11
50	.46277	2.16090	.48414	2.06553	.50587	1.97681	.52798	1.89400	10
51	.46312	2.15925	.48450	2.06400	.50623	1.97538	.52836	1.89266	9
52	.46348	2.15760	.48486	2.06247	.50660	1.97395	.52873	1.89133	8 7 6
53	.46383	2.15596	.48521	2.06094	.50696	1.97253	.52910	1.89000	1
54 55	.46418	2.15432	.48557	2.05942 2.05790	.50733	1.97111	.52947	1.88867	0
56	.46454	2.15268 2.15104	.48629	2.05637	.50806	1.96969 1.96827	.52985	1.88602	5 4 9
57	.46525	2.14940	.48665	2.05485	.50843	1.96685	53059	1.88469	0.0
58	.46560	2.14777	.48701	2.05333	.50879	1.96544	.53096	1.88337	1
59	.46595	2.14614	.48701 .48737	2.05182	.50916	1.96402	.53134	1.88205	1
60	.46631	2.14451	.48773	2.05030	.50953	1.96261	.53171	1.88073	(
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	'	Tang	Cotang	Tang	Cotang	Tang	Cotang	Tang	Cotang	1
-	0	.53171	1.88073	,55431	1.80405	.57735	1.73205	.60086	1.66428	60
	1	.53208	1.87941	.55469	1.80281	.57774	1.73089	.60126	1.66318	59
	2 3	.53246	1.87809	.55507	1.80158	.57813	1.73089 1.72973	.60165	1.66209	58
	3	.53283	1.87677	.55545	1.80034	.57851	1.72857	.60205	1.66099	57
	4	.53320	1.87546	.55583	1.79911	.57890	1.72741	.60245	1.65990	56
	5	.53358	1.87415	.55621	1.79788	.57929	1.72625	.60284	1.65881	55
	6 7	.53395	1.87283	.55659	1.79665	.57968	1.72509	.60324	1.65772	54
1	8	.53470	1.87021	.55736	1.79542	.58046	1.72278	.60403	1.65663	53
1	9	.53507	1.86891	.55774	1.79296	.58085	1.72163	.60443	1.65445	51
	10	.53545	1.86760	.55812	1.79174	.58124	1.72047	.60483	1.65337	50
-	11	.53582	1.86630	.55850	1.79051	.58162	1.71932	.60522	1.65228	49
	12	.53620	1.86499	.55888		.58201	1.71817	.60562	1.65120	48
	13	.53657	1.86369	.55926	1.78929 1.78807	.58240	1.71702	.60602	1.65011	47
	14	.53694	1.86239	.55964	1.78685	.58279	1.71588	.60642	1.64903	46
	15	.53732	1.86109	.56003	1.78563	.58318	1.71473	.60681	1.64795	45
	16	.53769	1.85979	.56041	1.78441	.58357	1.71358	.60721	1.64687	44
	17	.53807	1.85850	.56079	1.78319	.58396	1.71244	.60761	1.64579	43
	18	.53844	1.85720	.56117	1.78198	.58435	1.71129	.60801	1.64471	42
	19 20	.53882	1.85591 1.85462	.56156	1.78077	.58474	1.71015	.60841	1.64363	41 40
		The state of the s	Tana and		The state of the last		The State of the later of the	Charles of	-5 Black 5 "	1
-	21	.53957	1.85333	.56232	1.77834	.58552	1.70787	.60921	1,64148	39
	22 23	.53995	1.85204	.56270	1.77713	.58591	1.70673	.60960	1.64041	38
1	24	.54032	1.85075	.56347	1.77592 1.77471	.58631	1.70560 1.70446	.61000	1.63934 1.63826	36
	25	.54107	1.84818	.56385	1 77351	.58709	1.70332	.61080	1.63719	35
	26	.54145	1.84689	.56424	1.77230	.58748	1.70219	.61120	1.63612	34
1	27	.54183	1.84561	.56462	1.77110	.58787	1.70106	.61160	1.63505	33
1	28	.54220	1.84433	.56501	1.77110 1.76990	.58826	1.69992	.61200	1.63398	32
	29	.54258	1.84305	.56539	1.76869	.58865	1.69879	.61240	1.63292	31
	30	.54296	1.84177	.56577	1.76749	.58905	1.69766	.61280	1.63185	30
	31	.54333	1.84049	.56616	1.76629	.58944	1.69653	.61320	1.63079	29
1	32	.54371	1.83922	.56654	1.76510	.58983	1.69541	.61360	1.62972	28
	33	.54409	1.83794	.56693	1.76390	.59022	1.69428	.61400	1.62866	27
	34	.54446	1.83667	.56731	1.76271	.59061	1.69316	.61440	1.62760	26 25
	35 36	.54484	1.83540 1.83413	.56808	1.76151 1.76032	.59101	1.69091	.61480	1.62654	24
	37	.54560	1.83286	.56846	1.75913	.59179	1.68979	.61561	1.62442	23
	38	.54597	1.83159	.56885	1.75794	.59218	1.68866	.61601	1.62336	22
1	39	.54635	1.83033	.56923	1.75675	.59258	1.68754	.61641	1.62230	21
	40	.54673	1.82906	.56962	1.75556	.59297	1.68643	.61681	1.62125	20
1	41	.54711	1.82780	.57000	1.75437	,59336	1,68531	.61721	1.62019	19
	42	.54748	1.82654	.57039	1.75319	.59376	1.68419	.61761	1.61914	18
	43	.54786	1.82528	.57078	1.75200	.59415	1.68308	.61801	1.61808	17
	44	.54824	1.82402	.57116	1.75082	.59454	1.68196	.61842	1.61703	16
	45	.54862	1.82276	.57155	1.74964	.59494	1.68085	.61882	1.61598	15
	46	.54900	1.82150	.57193	1.74846	.59533	1.67974	.61922	1.61493	14
-	47	.54938	1.82025	.57232	1.74728 1.74610	.59573	1.67752	.62003	1.61383	12
	48	.55013	1.81774	.57309	1.74492	.59651	1.67641	62043	1.61179	111
	50	.55051	1.81649	.57348	1.74375	.59691	1.67530	.62083	1.61074	10
	51	.55089	1.81524	.57386	1.74257	.59730	1.67419	.62124	1.60970	9
	52	.55127	1.81399	.57425	1.74140	.59770	1.67309	62164	1.60865	8
	53	.55165	1.81274	.57464	1.74022	.59809	1.67198	.62204	1.60761	7
	54	.55203	1.81150	.57503	1.73905	.59849	1.67088	.62245	1.60657	6
	55	.55241	1.81025	.57541	1.73788	.59888	1.66978	.62285	1.60553	5
	56	.55279	1.80901	.57580	1.73671	.59928	1.66867	.62325	1.60449	4
	57 58	.55317	1.80777	.57619	1.73555 1.73438	.59967	1.66757	.62366	1.60345 1.60241	0
-	59	.55355	1.80653 1.80529	.57657	1.73321	.60046	1.66538	.62446	1.60137	3 2 1
	60	.55431	1.80405	.57735	1.73205	.60086	1.66428	.62487	1.60033	Ô
1	-	Cotang	Tang	Cotang	Tang	Cotang	Tang	Cotang	Tang	-
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1 62527 1.59930 64982 1.58791 67793 1.48163 2 63568 1.59836 650624 1.58791 67736 1.48070 4 62649 1.59517 65165 1.53595 67620 1.47885 5 62689 1.59517 65148 1.53407 67663 1.47797 6 62730 1.59414 65189 1.53409 67705 1.47792 6 62730 1.59413 65281 1.53400 67705 1.477699 7 62770 1.59311 65281 1.53400 67705 1.47699 8 62811 1.59208 65272 1.53205 67790 1.47514 9 62852 1.59105 65381 1.5307 67832 1.47422 10 62892 1.59002 65355 1.53010 67857 1.47303 11 62963 1.58907 65387 1.52813 67917 1.47238 12 62973 1.58955 65480 1.52719 68002 1.47053 13 63014 1.58695 65480 1.52719 68002 1.47053 14 63055 1.58490 65563 1.52622 68045 1.46902 15 63035 1.58490 65563 1.52525 68045 1.46902 16 63136 1.58388 65604 1.52332 68173 1.46686 18 63217 1.58184 65688 1.52235 68173 1.46503 19 63258 1.57781 66881 1.52139 68351 1.46503 20 63299 1.57781 66896 1.51743 68301 1.46713 21 63340 1.57787 66881 1.51502 68361 1.46903 22 63380 1.57775 65598 1.51652 68361 1.46933 23 63421 1.57575 65598 1.51652 68614 1.45305 24 63463 1.57775 66586 1.51502 68614 1.45305 25 63503 1.57474 66003 1.51502 68614 1.45305 26 63544 1.57372 66021 1.51466 68557 1.45294 27 63584 1.57676 66696 1.51502 68651 1.45955 28 63666 1.57069 66187 1.5104 68288 1.44530 29 63366 1.57069 66189 1.51084 68288 1.44530 20 63366 1.55666 66656 1.50228 69114 1.44688 21 63340 1.55666 66656 1.50228 69114 1.44688 22 63380 1.57775 66968 1.51502 68651 1.45395 23 63665 1.57069 66189 1.51084 68281 1.45390 24 64865 1.55666 66666 1.50228 69114 1.44688 25 64638 1.55666 66666 1.50228	Tang	Cotang	'
2	.70021	1.42815	$\overline{60}$
3	.70064	1.42726	59
4 62649 1.59620 65106 1.53595 67620 1.47785 5 63989 1.59517 65148 1.53407 6763 1.47709 6 62730 1.59414 65189 1.53400 67705 1.47699 7 62770 1.59105 65272 1.53205 67790 1.47649 9 62852 1.59005 65374 1.53107 67832 1.47422 10 62892 1.59002 65355 1.53010 67875 1.47232 12 62973 1.58790 65397 1.52913 67917 1.47238 12 62973 1.58695 65480 1.52719 68002 1.47033 14 63055 1.58593 65521 1.52622 68045 1.46862 15 63035 1.58184 65664 1.52429 6813 1.46787 16 63136 1.58388 65644 1.52332 68173 1.46868 16 <	.70107 .70151	1.42638 1.42550	58 57
5 62989 1.59517 65148 1.53497 67663 1.47792 6 62730 1.59414 65189 1.53400 67765 1.47697 7 62770 1.59311 65281 1.53205 67748 1.47607 8 62871 1.59005 65344 1.53107 67832 1.47422 10 62892 1.59002 65355 1.53010 67875 1.47230 11 629373 1.58695 65397 1.52913 67917 1.47238 12 62973 1.58797 65438 1.52719 6802 1.47033 14 63055 1.58593 65521 1.52622 68045 1.47053 14 63055 1.58490 65563 1.52525 68988 1.48705 15 63305 1.58489 655641 1.52429 68130 1.46778 18 63217 1.58184 656881 1.52235 68988 1.46825 19	.70194	1.42462	56
6 62730 1.59414 65189 1.53400 67705 1.47699 7 62770 1.5931 65281 1.53030 67738 1.47607 8 62811 1.59208 65273 1.53205 67790 1.47514 9 62852 1.59002 65355 1.53010 67832 1.47238 11 62963 1.58900 65397 1.52913 67917 1.47238 12 62973 1.58797 66438 1.52816 67960 1.47146 13 68014 1.58695 65480 1.52719 68002 1.47033 14 63055 1.58490 65563 1.52622 68045 1.46778 15 63055 1.58490 65563 1.52525 68045 1.46778 16 63136 1.58388 65604 1.52429 68130 1.46778 17 63175 1.58588 65604 1.52429 68130 1.46783 19	.70238	1.42374	55
8 62811 1.59208 65872 1.53205 67790 1.47514 1 629852 1.50105 65814 1.53010 67875 1.47320 1 68892 1.59002 65855 1.53010 67875 1.47320 1 68892 1.59002 65855 1.53010 67875 1.47320 1 68902 1.59002 65855 1.53010 67875 1.47320 1 68902 1.59029 65897 1.59213 67917 1.47238 1 63014 1.58695 65480 1.52719 68002 1.47053 1 4 63055 1.88593 65521 1.52022 60945 1.46902 1 65631 1.52022 60945 1.46902 1 65631 1.52022 60945 1.46902 1 65631 1.52022 60945 1.46902 1 663136 1.68388 65604 1.52429 68130 1.46778 1 663177 1.58286 65646 1.52323 68137 1.46678 1 63217 1.58184 65688 1.52235 68908 1.46570 1 69525 1 65898 1 65729 1.52139 68258 1.46503 1 65729 1.52139 68258 1.46503 1 65771 1.52043 68301 1.46411 1 65838 1 65771 1.52043 68301 1.46411 1 65838 1 65771 1.52043 68301 1.46411 1 65778 1 65854 1.51946 68343 1.46290 1 63306 1.57778 65854 1.51946 68343 1.46290 1 63306 1.57778 65854 1.51850 68396 1.46232 1 63306 1.57778 65854 1.51850 68396 1.46232 1 63303 1.57778 65854 1.51850 68396 1.46232 1 63303 1.57778 65854 1.51850 68396 1.46232 1 63303 1.57778 65854 1.51850 68396 1.46232 1 63303 1.57778 65854 1.51850 68396 1.46232 1 63303 1.57778 65854 1.51850 68396 1.46232 1 63303 1.57778 65854 1.51850 68396 1.46232 1 63303 1.57778 65854 1.51850 68396 1.46232 1 63303 1.57778 66854 1.51850 68396 1.46323 1 63303 1.57774 66003 1.51638 68371 1.46016 1 63303 1 63304 1.57779 66003 1.51608 68577 1.43864 1 63303 1 63304 1 63772 1 66003 1.51466 68577 1 68577 1 68657 1 68577 1 68577 1 68577 1 68657 1 68577 1 685	.70281	1.42286	54
9	.70325	1.42198	53
10	.70368 .70412	1.42110 1.42022	52 51
11 .62953 1.58900 .65397 1.52913 .67917 1.47238 12 .62978 1.58797 .6438 1.52816 .67960 1.47146 13 .63014 1.58695 .65480 1.52719 .68002 1.47033 14 .63055 1.58490 .65563 1.52525 .68081 1.46962 15 .63051 1.58388 .65604 1.52322 .68081 1.46778 16 .63136 1.58388 .65604 1.52329 .68133 1.46778 17 .63177 1.58286 .66646 1.52332 .68173 1.46686 19 .63251 1.58083 .65729 1.52139 .68258 1.46503 20 .63291 1.57778 .65813 1.51946 .68341 1.46503 22 .63380 1.57778 .65864 1.51850 .68341 1.46229 23 .63421 1.57675 .65866 1.51754 .68349 1.46187	.70455	1.41934	50
12 62973 1.58797 65438 1.52371 67900 1.47146 13 63014 1.58905 65480 1.52719 68002 1.47053 14 63055 1.58490 65563 1.52525 68088 1.46870 16 63136 1.68388 65604 1.52429 68130 1.46783 17 63177 1.58286 65646 1.52323 68173 1.46686 18 63217 1.58184 65688 1.52235 68215 1.46505 19 63258 1.58083 65729 1.52139 68258 1.46503 20 63299 1.57981 66771 1.32043 68301 1.46471 21 63340 1.57879 65813 1.51364 68301 1.46411 22 63380 1.57778 65854 1.51850 68386 1.40229 23 63421 1.57676 65896 1.51724 68429 1.40187 24 63462 1.57575 65938 1.51768 68311 1.40416 25 63303 1.57474 63980 1.51562 68514 1.40305 25 63364 1.57372 66021 1.51562 68642 1.40229 27 63384 1.57372 66021 1.51562 68642 1.4573 28 63625 1.57179 66105 1.51275 68642 1.4573 29 63666 1.57069 66147 1.51179 68605 1.45502 20 63666 1.57069 66189 1.51084 68728 1.45501 31 63748 1.56868 66230 1.50983 68871 1.45408 32 63789 1.56667 66324 1.50072 68900 1.4573 33 63850 1.56667 66324 1.50072 68985 1.45802 34 63871 1.56566 66636 1.50072 68990 1.45139 35 63912 1.56466 66398 1.5007 68942 1.45049 35 63912 1.56666 66656 1.50023 68942 1.44508 38 64035 1.56666 66666 1.50228 69071 1.44788 44 64240 1.55666 66666 1.50228 69071 1.44788 45 64199 1.55766 66666 1.50238 6900 1.44308 44 64240 1.55666 66666 1.50238 69117 1.44398 45 64191 1.55766 66666 1.50238 69116 1.44906 46 64303 1.55368 66600 1.49755 69329 1.44239 45 64392 1.55467 66668 1.50038 69000 1.44308 45 64446 1.55269 66690 1.49755 69329 1.44239 45 64368 1.54576 66669 1.4984 69245 1.44508 45 64464 1.55266 66698 1.4909	.70499	1.41847	49
13 .63014 1.58695 .65490 1.52719 .68022 1.47053 14 .63055 1.55893 .65521 1.52622 .68045 1.46962 16 .63136 1.58389 .65563 1.52525 .68088 1.46870 17 .63177 1.58286 .66646 1.52323 .68130 1.46778 18 .63217 1.58184 .65688 1.52235 .68215 1.46595 19 .63258 1.55688 .65729 1.52139 .68258 1.46595 20 .63299 1.57981 .65771 1.52043 .68301 1.46411 21 .63340 1.57676 .65864 1.51850 .68348 1.46429 22 .63380 1.57778 .65854 1.51850 .68361 1.46325 23 .63462 1.57575 .65398 1.51658 .68314 1.45355 24 .63662 1.57774 .66023 1.51526 .68514 1.45355 <td>.70542</td> <td>1.41759</td> <td>48</td>	.70542	1.41759	48
15	.70586	1.41672	47
16 .63136 1.58388 .65604 1.52322 .68173 1.46678 17 .63177 1.58886 .65646 1.52332 .68173 1.46686 18 .63217 1.58184 .65688 1.52235 .68251 1.46503 19 .63258 1.58083 .66729 1.52139 .68258 1.46503 20 .63299 1.57981 .65771 1.52043 .68301 1.46411 21 .63340 1.57879 .65813 1.51860 .68386 1.46229 22 .63380 1.57778 .65894 1.51754 .68420 1.46137 24 .63462 1.57575 .65938 1.51658 .68471 1.46046 25 .63503 1.57474 .65980 1.51562 .68514 1.45952 26 .63544 1.57271 .66021 1.51466 .68537 1.45952 27 .63662 1.57079 .66105 1.51275 .68642 1.45592 <td>.70629</td> <td>1.41584</td> <td>46</td>	.70629	1.41584	46
17 .63177 1.58286 .65646 1.52323 .68173 1.46868 19 .63217 1.58184 .65688 1.52325 .68215 1.46503 20 .63258 1.58083 .65729 1.52139 .68258 1.46503 20 .63399 1.57870 .65813 1.51946 .68343 1.46229 22 .63380 1.57778 .65854 1.51754 .68328 1.46229 23 .63421 1.57676 .65896 1.51754 .68429 1.440229 24 .63462 1.57575 .65938 1.51658 .68311 1.40045 25 .63504 1.57774 .65986 1.51562 .68514 1.43955 26 .63544 1.57372 .66021 1.51562 .68514 1.43955 27 .63584 1.57372 .66021 1.51466 .68537 1.45682 29 .63666 1.5709 .66147 1.51179 .68620 1.45682 <td>.70673</td> <td>1.41497</td> <td>45 44</td>	.70673	1.41497	45 44
19 .63217 1.58184 .65688 1.52235 .68215 1.46505 20 .63239 1.57981 .65729 1.52139 .68258 1.46505 20 .63299 1.57781 .65729 1.52139 .68258 1.46211 21 .63340 1.57879 .65813 1.51946 .68343 1.46222 22 .63380 1.57776 .65896 1.51754 .68391 1.40137 24 .63462 1.57575 .65980 1.51562 .68514 1.4046 25 .63503 1.57474 .65980 1.51562 .68514 1.4046 25 .63503 1.57771 .66021 1.51406 .68577 1.45864 27 .63564 1.57271 .66035 1.51370 .68600 1.44773 28 .63625 1.57170 .66105 1.51275 .68621 1.4562 29 .63666 1.57069 .66147 1.51179 .68655 1.45592	.70717 .70760	1.41322	43
19	.70804	1.41235	42
21	.70848	1.41148	41
22 63380 1.57778 65854 1.51850 68986 1.46229 23 63121 1.57676 65896 1.51754 68429 1.46187 24 63421 1.57675 65838 1.51658 68471 1.46046 25 63544 1.57372 66021 1.51562 68514 1.43953 27 63584 1.57771 66063 1.51370 68000 1.45773 23 63625 1.57170 66105 1.51275 68642 1.45582 29 63666 1.55069 66147 1.51084 68728 1.45592 30 63707 1.50969 66189 1.51084 68728 1.45592 31 63748 1.56868 66330 1.50988 68814 1.45320 32 63789 1.56767 66272 1.50983 68814 1.45320 33 63851 1.56667 66356 1.50707 68890 1.45422 34	.70891	1.41061	40
23 63421 1.57676 65896 1.51754 68429 1.46187 24 63402 1.57575 65938 1.51652 68471 1.46046 25 63503 1.57474 65380 1.51652 68514 1.46904 26 63344 1.57372 66021 1.51466 68557 1.43864 27 63854 1.57377 66003 1.51370 68602 1.45763 23 63625 1.57170 66105 1.51275 68642 1.45682 29 63606 1.57099 66147 1.51179 68652 1.45501 31 63788 1.56667 66829 1.5088 68771 1.4540 32 63789 1.56667 66322 1.50903 68814 1.4529 33 63830 1.56466 66398 1.50072 68957 1.4529 34 63931 1.56466 66398 1.50072 68957 1.4529 35	.70935	1.40974	39
24 .63402 1.57575 .65988 1.51658 .68471 1.46046 25 .63503 1.57574 .65980 1.51562 .68514 1.45955 26 .63344 1.57372 .66021 1.51466 .68557 1.43864 27 .63384 1.57271 .66003 1.51370 .68600 1.45773 28 .63625 1.577170 .66105 1.51179 .68685 1.45692 29 .63666 1.57069 .66149 1.51084 .68728 1.45592 30 .63707 1.56968 .66830 1.5088 .68721 1.4540 31 .63748 1.56667 .66220 1.50993 .68814 1.4520 32 .63789 1.56767 .66314 1.50707 .68857 1.45229 33 .63912 1.56566 .66356 1.50707 .68857 1.45229 34 .63871 1.56566 .66356 1.50072 .68942 1.45049	.70979	1.40887	38
25	.71023	1.40800	37
26 .63544 1.57372 .66021 1.51466 .68557 1.45864 27 .63584 1.57371 .66063 1.51370 .68600 1.45773 23 .63625 1.57170 .66105 1.51275 .68602 1.45682 20 .63666 1.57069 .66147 1.51179 .68685 1.45692 30 .63707 1.56069 .66189 1.51084 .68728 1.45693 31 .63748 1.56868 .66230 1.50988 .68771 1.45410 32 .63789 1.56767 .66272 1.50993 .68814 1.45329 31 .63871 1.56566 .66336 1.50707 .68857 1.45490 33 .63871 1.56366 .66356 1.50707 .68907 1.45139 35 .63303 1.56366 .66440 1.5012 .68985 1.44948 37 .63994 1.56265 .66482 1.50472 .69073 1.44788	.71110	1.40627	35
23 .63625 1.57170 .66105 1.51275 .68642 1.45682 20 .63666 1.57069 .66147 1.51179 .68085 1.45592 30 .63707 1.55069 .66189 1.51084 .68728 1.45592 31 .63748 1.56868 .66230 1.50983 .68771 1.45410 32 .63789 1.56767 .68272 1.50893 .68814 1.45320 31 .63871 1.56566 .66336 1.50702 .68900 1.45139 31 .63871 1.56566 .66338 1.50007 .68942 1.45049 35 .63912 1.56466 .66398 1.50007 .68942 1.44594 37 .63934 1.5666 .66482 1.5012 .68985 1.44968 37 .6394 1.56665 .66524 1.5032 .69071 1.44788 38 .64055 1.56665 .66524 1.5032 .69171 1.44588	.71154	1.40540	34
29	.71198	1.40454	33
30 63707 1,56969 66189 1,51084 68728 1,45501 31 63748 1,56967 66272 1,50983 68814 1,45320 32 63789 1,56767 66272 1,50983 68814 1,45320 33 63830 1,56667 66314 1,50797 68857 1,45229 31 63871 1,56566 66336 1,50702 68900 1,45139 32 63912 1,56466 66398 1,50607 68942 1,45049 33 63953 1,56366 66440 1,50512 68985 1,44958 37 63994 1,56265 66482 1,50417 69028 1,44508 38 64035 1,56165 66524 1,50322 69071 1,44778 39 64076 1,56065 66566 1,50228 69114 1,44688 30 64107 1,55666 66680 1,50133 69157 1,44598 41 64158 1,55866 66668 1,50133 69157 1,44598 42 64199 1,55766 66608 1,4494 69243 1,44418 43 64240 1,55666 66734 1,4944 69243 1,44418 44 64281 1,55567 66776 1,49755 69329 1,44239 45 64363 1,55368 66800 1,4956 69316 1,44960 47 64404 1,55269 66902 1,4972 69459 1,43881 49 64487 1,55071 66944 1,4984 69586 1,43891 49 64487 1,55071 66948 1,49284 60565 1,43881 49 64487 1,55071 66948 1,49284 60565 1,43891 50 64528 1,54776 67078 1,49079 69588 1,43614 50 64528 1,54776 67078 1,49090 69588 1,43614 50 64528 1,54776 67078 1,49090 69588 1,43614 50 64528 1,54776 67078 1,49090 69718 1,43614 50 64528 1,54776 67071 1,49077 69631 1,43614 50 64528 1,54776 67071 1,49079 69631 1,43614 50 64528 1,54776 67071 1,49079 69631 1,43614 50 64528 1,5474 67713 1,49090 69718 1,43436 50 64528 1,54475 67230 1,4872 69691 1,43436 50 64528 1,54478 67230 1,4872 69611 1,43436 50 64528 1,54478 67230 1,4872 69611 1,43436 50 64528 1,54478 67230 1,4816 6761 1,43476 50 64724 1,54478 67230 1,4872 69614 1,43246 50 64724 1,54478 67230 1,4872 696	.71242 .71285	1.40367	32
31 .63748 1,56868 .66230 1,50988 .68771 1,45410 32 .63789 1,56767 .66272 1,50993 .68814 1,45320 33 .63880 1,56666 .66374 1,50707 .68857 1,45239 31 .63871 1,56566 .66356 1,50907 .68942 1,45139 35 .63912 1,56366 .66398 1,50907 .68942 1,45049 36 .63933 1,56366 .66440 1,5017 .69028 1,44958 37 .63994 1,56265 .66482 1,50322 .69071 1,4478 39 .64076 1,56065 .66564 1,50322 .69071 1,4478 40 .64117 1,55966 .66660 1,5033 .69200 1,44598 41 .64188 1,55866 .66650 1,50038 .69200 1,44508 42 .64199 1,55766 .60602 1,49944 .69213 1,44498	.71329	1.40281 1.40195	31
\$\frac{3}{3}\$ \$63789 \$1.56767 \$66324 \$1.50797 \$68857 \$1.43529 \$31.63830 \$1.56666 \$66356 \$1.50702 \$68903 \$1.45133 \$35.63912 \$1.56566 \$66356 \$1.50702 \$68903 \$1.45133 \$35.63912 \$1.56466 \$66398 \$1.50007 \$68942 \$1.45049 \$36.63953 \$1.56366 \$66440 \$1.50612 \$68985 \$1.44568 \$37.63994 \$1.56265 \$66440 \$1.50612 \$68985 \$1.44958 \$37.63994 \$1.56265 \$66440 \$1.50612 \$68985 \$1.44958 \$38.64035 \$1.56165 \$66524 \$1.50322 \$69071 \$1.44778 \$39.64076 \$1.56065 \$66524 \$1.50322 \$69071 \$1.44778 \$39.64076 \$1.56065 \$66566 \$1.50228 \$69114 \$1.44698 \$40.64117 \$1.55966 \$66608 \$1.50133 \$69157 \$1.44598 \$42.64199 \$1.55766 \$66603 \$1.49944 \$69243 \$1.44498 \$42.64199 \$1.55766 \$66603 \$1.49944 \$69243 \$1.44498 \$42.64210 \$1.55666 \$66734 \$1.49849 \$69296 \$1.44929 \$4566421 \$1.55567 \$66776 \$1.49755 \$69329 \$1.4429 \$4566421 \$1.55369 \$66903 \$1.49661 \$69372 \$1.44449 \$46441 \$1.55369 \$66903 \$1.49472 \$69416 \$1.49660 \$49464 \$4.55289 \$66903 \$1.49472 \$69459 \$1.43979 \$49.64487 \$1.55071 \$66944 \$1.49874 \$69502 \$1.43881 \$4964487 \$1.55071 \$66946 \$1.49284 \$0.9558 \$1.43703 \$49.64487 \$1.55071 \$66946 \$1.49284 \$0.9558 \$1.43703 \$59.66693 \$1.49949 \$69588 \$1.43703 \$59.66693 \$1.49949 \$69588 \$1.43703 \$59.66693 \$1.49949 \$69588 \$1.43703 \$59.66693 \$1.49949 \$69588 \$1.43703 \$59.66693 \$1.49949 \$69588 \$1.43703 \$59.66693 \$1.49949 \$69588 \$1.43703 \$59.66693 \$1.49949 \$69588 \$1.43703 \$59.66693 \$1.49949 \$69588 \$1.43703 \$59.66693 \$1.49949 \$69588 \$1.43703 \$59.66693 \$1.49472 \$69693 \$1.49472 \$69693 \$1.49472 \$69693 \$1.49472 \$69693 \$1.49472 \$69693 \$1.49472 \$69693 \$1.49472 \$69693 \$1.49472 \$69693 \$1.49472 \$69693 \$1.49472 \$69693 \$1.49472 \$69693 \$1.49472 \$69693 \$1.49472 \$69693 \$1.49472 \$69693 \$1.49472 \$69693 \$1.49472 \$69693	.71373	1.40109	29
33	.71373	1.40109	28
34 .63871 1.56566 .66356 1.50702 .68900 1.45139 35 .63912 1.56466 .66398 1.50007 .68942 1.45049 36 .63953 1.56366 .66440 1.50512 .68985 1.44958 37 .03934 1.56265 .66482 1.50417 .6028 1.444868 38 .64055 1.56665 .66524 1.50322 .69071 1.44758 40 .64117 1.55966 .66608 1.50133 .69157 1.44598 41 .64158 1.55866 .66650 1.50038 .6920 1.44598 42 .64199 1.55766 .66630 1.4944 .69243 1.44418 43 .64240 1.5566 .66630 1.49944 .69243 1.44418 44 .64281 1.5567 .66776 1.4955 .69329 1.44392 45 .64322 1.55467 .66818 1.49661 .69372 1.44414	.71461	1.39936	27
36	.71505	1.39850	26
37 63994 1,56265 66482 1,50417 69028 1,44268 38 64035 1,56165 66524 1,50322 69071 1,44778 39 54076 1,56063 66566 1,50228 69114 1,44788 40 64117 1,55966 66608 1,50133 69157 1,44598 41 64188 1,55866 66650 1,50338 69200 1,44508 42 64199 1,55766 66662 1,49944 69243 1,44408 43 64240 1,55866 66734 1,49849 69286 1,44329 45 64323 1,55467 66776 1,49755 69329 1,44329 46 64323 1,55369 66800 1,49661 69372 1,44149 47 64404 1,55289 66902 1,4956 69416 1,44060 48 64446 1,55170 66941 1,49874 69502 1,48819 50	.71549	1.39764	25
38 64095 1.56165 66524 1.50322 69071 1.44778 39 64076 1.56065 66566 1.50228 69114 1.44688 40 64117 1.55966 66608 1.50133 69157 1.44508 41 64158 1.55866 66608 1.50038 69200 1.44508 42 64199 1.55766 66693 1.49944 69213 1.44418 43 64240 1.55666 66734 1.49849 69286 1.44329 44 .64281 1.55567 66767 1.49755 59329 1.44423 45 .64322 1.55467 66818 1.49961 69372 1.44149 46 .64303 1.55368 66800 1.4956 69416 1.4960 47 .64404 1.55290 66902 1.4972 .69459 1.43881 49 .64487 1.55170 66944 1.49378 .69502 1.43881 50 <td>.71593</td> <td>1.39679</td> <td>24 23</td>	.71593	1.39679	24 23
33 .64076 1.56065 .66566 1.50238 .69114 1.44688 40 .64117 1.55966 .66608 1.50133 .69157 1.44598 41 .64158 1.55666 .66608 1.50038 .69200 1.44598 42 .64199 1.55766 .66693 1.49944 .69243 1.44418 43 .64240 1.55667 .66776 1.49755 .69329 1.44393 44 .64281 1.55567 .66776 1.49755 .69329 1.44419 46 .64303 1.55368 .66800 1.49666 .69416 1.44060 47 .64494 1.55170 .66940 1.4972 .69459 1.43870 48 .64448 1.55170 .66986 1.49247 .69459 1.43870 49 .64487 1.55071 .66986 1.49284 .69545 1.43703 50 .64588 1.54873 .67071 1.49097 .69631 1.43614	.71681	1.39507	22
41 .64158 1.55866 .66650 1.50038 .69200 1.44508 42 .64199 1.55766 .66630 1.49944 .69243 1.44418 43 .64240 1.55566 .66734 1.49849 .69286 1.44329 44 .64281 1.55567 .66776 1.49755 .69329 1.44239 45 .64322 1.55467 .66818 1.49661 .69372 1.444149 46 .64303 1.55368 .66860 1.49566 .69416 1.49606 47 .64404 1.55269 .66902 1.49472 .69459 1.43970 48 .64446 1.55170 .66944 1.49378 .69502 1.4881 49 .64487 1.55071 .66948 1.49828 .69502 1.49881 50 .64528 1.54972 .67028 1.49190 .69588 1.43703 51 .64569 1.54873 .67071 .49097 .69631 1.42614 52 .64610 1.54774 .67113 1.49007 .69631 1.42614 52 .64610 1.54774 .67113 1.49007 .696718 1.43136 53 .64628 1.54575 .67155 1.48909 .69718 1.43136 54 .64693 1.54576 .67197 1.48816 .69761 1.43347 55 .64734 1.54478 .67239 1.48722 .69804 1.43347	.71725	1.39421	21
42 64199 1.55766 66692 1.49944 69243 1.44418 43 64240 1.55666 66734 1.49849 69286 1.44329 44 64281 1.55567 66776 1.49755 69329 1.44329 45 64322 1.55467 66818 1.49661 69372 1.44449 46 64303 1.55388 66860 1.49666 69416 1.44039 47 64404 1.55289 66902 1.49472 69459 1.43970 48 64446 1.55170 66944 1.49874 60502 1.48881 49 64487 1.55071 66986 1.49284 69515 1.43703 50 64588 1.54972 67028 1.49190 69588 1.43703 51 64509 1.54873 67071 1.49097 69631 1.43614 52 64610 1.54774 67113 1.49003 69675 1.4325 53	.71769	1.39336	20
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$.71813	1.39250	19
$\begin{array}{cccccccccccccccccccccccccccccccccccc$.71857	1.39165	18
46	.71901	1.39079	17
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$.71990	1.38909	15
48 .64446 1.55170 .66944 1.49378 .69502 1.43881 49 .64487 1.55071 .66986 1.49284 .93545 1.43792 50 .64528 1.54972 .67028 1.49190 .69588 1.43703 51 .64569 1.54873 .67071 1.49097 .69631 1.43614 52 .64610 1.54774 .67113 1.49003 .69675 1.43525 53 .64652 1.54675 .67185 1.48909 .69718 1.43436 54 .64693 1.54576 .67197 1.48816 .69761 1.43347 55 .64734 1.54478 .67239 1.48722 .69804 1.432347	.72034	1.38824	14
49 .64487 1.55071 .66986 1.49284 .00545 1.43792 50 .64588 1.54972 .67028 1.49190 .69588 1.43703 51 .64569 1.54873 .67071 1.49097 .69631 1.43614 52 .64610 1.54774 .67113 1.49093 .69675 1.43624 53 .64652 1.54675 .67185 1.48909 .69718 1.43436 54 .64693 1.54576 .67197 1.48816 .69761 1.43347 55 .64734 1.54478 .67239 1.48722 .69804 1.43238	.72078	1.38738	13
50 .64528 1.54972 .67028 1.49190 .69588 1.43703 51 .64569 1.54873 .67071 1.49097 .96631 1.43614 52 .64610 1.54774 .67113 1.49003 .9675 1.4365 53 .64652 1.54675 .67185 1.48909 .69718 1.43436 54 .64693 1.54576 .67197 1.48816 .99761 1.43347 55 .64734 1.54478 .67239 1.48722 .99804 1.43234	.72122	1.38653	12
51 .64569 1.54873 .67071 1.49097 .69631 1.43614 52 .64610 1.54774 .67113 1.49003 .69675 1.43525 53 .64625 1.54675 .67155 .148909 .69718 1.43436 54 .64693 1.54576 .67197 1.48816 .69761 1.43347 55 .64734 1.54478 .67239 1.48722 .09804 1.43234	72211	1.38568 1.38484	10
52 .64610 1.54774 .67113 1.49003 .69675 1.43525 53 .64652 1.54675 .67155 1.48909 .69718 1.43436 54 .64693 1.54576 .67197 1.48816 .69761 1.43347 55 .64734 1.54478 .67239 1.48722 .69804 1.43247	.72255	1.38399	9
53 .64652 1.54675 67155 1.48909 69718 1.43436 54 .64698 1.54576 67197 1.48816 69761 1.43347 55 .64734 1.54478 67239 1.48732 69804 1.43258	.72299	1.38314	8
54 .64698 1.54576 .67197 1.48816 .69761 1.43347 55 .64734 1.54478 .67239 1.48722 .69804 1.43258	.72344	1.38229	7
1.10000	.72388	1.38145	8 7 6 5 4 3 2 1
56 .64775 1.54379 .67282 1.48629 .69847 1.43169	.72432	1.38060	5
56 .64775 1.54379 .67282 1.48629 .69847 1.43169 .57 .64817 1.54281 .67324 1.48536 .69891 1.43080	72477	1.37976	4
58 .64858 1.54183 .67366 1.48442 .69934 1.42992	72565	1.37807	2
59 .64899 1.54085 .67409 1.48349 .69977 1.42903	72610	1.37722	1
60 .64941 1.53986 .67451 1.48256 .70021 1.42815	.72654	1.37638	0
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1	3	6°	3	70	3	8°	3	9°	
1	Tang	Cotang	Tang	Cotang	Tang	Cotang	Tang	Cotang	1
(1.37638	.75355	1.32704	.78129	1.27994	.80978	1.23490	60
1 64	.72699	1.37554	.75401	1.32624	.78175	1.27917	.81027	1.23416	59
6	2 .72743 3 .72788	1.37470 1.37386	.75447	1.32544 1.32464	.78222	1.27841 1.27764	.81075 .81123	1.23343	58
4	72832	1.37302	.75538	1.32384	.78316	1.27688	.81171	1.23196	56
1	.72877	1.37218	.75584	1.32304	.78363	1.27611	.81220	1.23123	55
1	.72921	1.37134	.75629	1.32224	.78410	1.27535	.81268	1.23050	54
1 8	72966	1.37050	.75675	1.32144	.78457	1.27458	.81316	1.22977	53
1		1.36967 1.36883	.75721	1.32064 1.31984	.78504	1.27382 1.27306	.81364 .81413	1.22904 1.22831	52 51
10	73100	1.36800	.75812	1.31904	.78598	1.27230	.81461	1.22758	50
11	.73144	1.36716	.75858	1.31825	.78645	1,27153	.81510	1,22685	49
19	.73189	1.36633	.75904	1.31745	.78692	1.27077	.81558	1.22612	48
13	3 .73234	1.36549	.75950	1.31666	.78739	1.27001	.81606	1.22539	47
14	.73278	1.36466	.75996	1.31586	.78786	1,26925	.81655	1.22467	46
15		1.36383 1.36300	.76042	1.31507 1.31427	.78834	1.26849 1.26774	.81703 .81752	1.22394 1.22321	45
17		1.36217	.76134	1.31348	.78928	1.26698	.81800	1.22249	43
18		1.36134	.76180	1.31269	.78975	1.26622	.81849	1.22176	42
19		1.36051	.76226	1.31190	.79022	1.26546	.81898	1.22104	41
20	1	1.35968	.76272	1.31110	.79070	1.26471	.81946	1.22031	40
2:		1.35885	.76318	1.31031	.79117	1.26395	.81995	1.21959	39
25		1.35802	.76364	1.30952	.79164	1.26319	.82044	1.21886	38
2		1.35719 1.35637	.76410 .76456	1.30873 1.30795	.79212 .79259	1.26244	.82092 .82141	1.21814	37
2	73771	1.35554	.76502	1.30716	.79306	1.26093	.82190	1.21670	35
20	73816	1.35472	.76548	1.30637	.79354	1.26018	.82238	1.21598	34
25	7 .73861	1.35389	.76594	1.30558	.79401	1.25943	.82287	1.21526	33
20	3 .73906 .73951	1.35307 1.35224	.76640	1.30480	.79449	1.25867	.82336	1.21454 1.21382	32
30		1.35142	.76733	1.30323	.79496 .79544	1.25792	.82385	1.21382	31 30
3:	1	1.35060	.76779	1,30244	.79591	1.25642	,82483	1,21238	29
39	74086	1.34978	.76825	1.30166	.79639	1.25567	.82531	1.21166	28
3	3 .74131	1.34896	.76871	1.30087	.79686	1.25492	.82580	1.21094	27
3		1.34814	.76918	1.30009	.79734	1.25417	.82629	1.21023	26
3		1.34732	.76964	1.29931	.79781	1.25343	.82678	1.20951	25 24
3		1.34568	.77057	1.29775	.79877	1.25193	82776	1.20879	23
3	3 .74357	1,34487	.77103	1.29696	.79924	1.25118	.82825	1.20736	22
39		1.34405	.77149	1.29618	.79972	1.25044	.82874	1.20665	21
4		1.34323	.77196	1.29541	.80020	1.24969	.82923	1.20593	20
4		1.34242	.77242	1.29463	.80067	1.24895	.82972	1.20522	19
4		1.34160	.77289	1.29385	.80115	1.24820 1.24746	.83022	1.20451 1.20379	18
4		1,34079	.77335 .77382	1.29307	.80163	1.24746	.83071	1.20379	17
4	5 .74674	1.33998 1.33916	.77428	1.29152	.80258	1.24597	.83169	1.20237	15
4	6 .74719	1.33835	.77475	1.29074	.80306	1.24523	.83218	1.20166	14
4	7 .74764	1.33754	.77521	1.28997	.80354	1.24449	.83268	1.20095	13
4		1.33673	.77568	1.28919	.80402	1.24375	.83317	1,20024	12
5		1.33592	.77615	1.28842	.80450	1.24301	.83366 .83415	1.19953	11 10
5		1.33430	.77708	1.28687	.80546	1.24153	.83465	1.19811	9
5	2 .74991	1.33349	.77754	1.28610	.80594	1.24155	.83514	1.19740	8
5	3 .75037	1.33268	.77801	1.28533	.80642	1.24005	.83564	1.19669	8 7 6
5	4 .75082	1.33187	.77848	1.28456	.80690	1.23931	.83613	1.19599	6
5		1.33107	.77895	1.28379	.80738	1.23858	.83662	1.19528	5
5 5	6 .75173 7 .75219	1.33026	.77941	1.28302 1.28225	.80786	1.23784 1.23710	.83712 .83761	1.19457 1.19387	3
5	8 .75264	1.32865	.78035	1.28148	.80882	1.23637	.83811	1.19316	2
5	9 .75310	1.32785	.78082	1.28071	.80930	1.23563	.83860	1.19316 1.19246	2
6	-	1.32704	.78129	1.27994	.80978	1.23490	.83910	1.19175	0
	Cotang	Tang	Cotang	Tang	Cotang	Tang	Cotang	Tang	,
		53°	1	2°	5	1°	5	0°	
1				104	U		U	0	100

	4	0°°	4	1°	1 4	2°	4	3°	1
1	Tang	Cotang	Tang	Cotang	Tang	Cotang	Tang	Cotang	1
0	.83910	1.19175	.86929	1.15037	.90040	1.11061	.93252	1.07237	60
1	.83960	1.19105	.86980	1.14969	.90093	1.10996	.93306	1.07174	59
3	.84009	1.19035	.87031	1.14902	.90146	1.10931	.93360	1.07112	58
3	.84059	1.18964	.87082	1.14834	.90199	1.10867	.93415	1.07049	57
5	.84108	1.18894 1.18824	.87133	1.14767 1.14699	.90251	1.10802 1.10737	.93469	1.06987	56
6	.84208	1.18754	.87236	1.14632	.90357	1.10672	.93578	1.06862	54
7	.84258	1.18684	.87287	1.14565	.90410	1.10607	.93633	1.06800	53
8	.84307	1.18614	.87338	1.14498	.90463	1.10543	.93688	1.06738	52
9	.84357	1.18544	.87389	1.14430	.90516	1.10478	.93742	1.06676	51
10	.84407	1.18474	.87441	1.14363	.90569	1.10414	.93797	1.06613	50
11	.84457	1.18404	.87492	1.14296	.90621	1.10349	.93852	1.06551	49
12	.84507	1.18334	.87543	1.14229	.90674	1.10285	.93906	1.06489	48
13	.84556	1.18264	.87595	1.14162	.90727	1.10220	.93961	1.06427	47
14	.84606	1.18194	.87646	1.14095	.90781	1.10156	.94016	1.06365	46
15	.84656	1.18125	.87698 .87749	1.14028	.90834	1.10091	.94071	1.06303	45
16	.84706 .84756	1.18055 1.17986	.87801	1.13961	.90887	1.10027	.94125	1.06241	44 43
18	.84806	1.17916	.87852	1.13828	.90993	1.09899	.94235	1.06117	42
19	.84856	1.17846	.87904	1.13761	.91046	1.09834	.94290	1.06056	41
20	.84906	1.17777	.87955	1.13694	.91099	1.09770	.94345	1.05994	40
21	.84956	1.17708	.88007	1.13627	.91153	1.09706	.94400	1.05932	39
22	.85006	1.17638	.88059	1.13561	.91206	1.09642	.94455	1.05870	38
23	.85057	1.17569	.88110	1.13494	.91259	1.09578	.94510	1.05809	37
24	.85107	1.17500	.88162	1.13428	.91313	1.09514	.94565	1.05747	36
25	.85157	1.17430	.88214	1.13361	.91366	1.09450	.94620	1.05685	35
26 27	.85207 .85257	1.17361 1.17292	.88265	1.13295 1.13228	.91419	1.09386 1.09322	.94676	1.05624	34
28	.85308	1.17223	.88369	1.13162	.91475	1.09322	.94731	1.05562	32
29	.85358	1.17154	.88421	1.13096	.91580	1.09195	.94841	1.05439	31
30	.85408	1.17085	.88473	1.13029	.91633	1.09131	.94896	1.05378	30
31	.85458	1.17016	.88524	1.12963	.91687	1.09067	.94952	1.65317	29
32	.85509	1.16947	.88576	1.12897	.91740	1.09003	.95007	1.05255	28
33	.85559	1.16878	.88628	1.12831	.91794	1.08940	.95062	1.05194	27
34	.85609	1.16809	.88680	1.12765	.91847	1.08876	.95118	1.05133	26
35	.85660	1.16741	.88732	1.12699	.91901	1.08813	.95173	1.05072	25
36	.85710	1.16672	.88784	1.12633	.91955	1.08749	.95229	1.05010	24
38	.85761	1.16603	.88888	1.12567	.92008	1.08686	.95284	1.04949 1.04888	23
39	.85862	1.16466	.88940	1.12435	.92116	1.08559	.95395	1.04827	21
40	.85912	1.16398	.88992	1.12369	.92170	1.08496	.95451	1.04766	20
41	.85963	1.16329	.89045	1,12303	,92224	1.08432	.95506	1.04705	19
42	.86014	1.16261	.89097	1.12238	.92277	1.08369	.95562	1.04644	
43	.86064	1.16192	.89149	1.12172	.92331	1.08306	.95618	1.04583	18 17
44	.86115	1.16124	.89201	1.12106	.92385	1.08243	.95673	1.04522	16
45	.86166	1.16056	.89253	1.12041	.92439	1.08179	.95729	1.04461	15
46	.86216	1.15987	.89306	1.11975	.92493	1.08116	.95785	1.04401	14
47	.86267 .86318	1.15919 1.15851	.89358	1.11909	.92547	1.08053	.95841	1.04340	13
49	.86368	1.15783	.89463	1.11844	.92601	1.07990	.95897	1.04279	12
50		1.15715	.89515	1.11713	.92709	1.07864	.96008	1.64158	10
51	.86470	1.15647	.89567	1.11648	.92763	1.07801	.96064	1.04097	9
52		1.15579	.89620	1.11582	.92817	1.07738	.96120	1.04097	8
53		1.15511	.89672	1.11517	.92872	1.07676	.96176	1.03976	7
54	.86623	1.15443	.89725	1.11452	.92926	1.07613	.96232	1.03915	6
55		1.15375	.89777	1.11387	.92980	1.07550	.96288	1.03855	5
56		1.15308	89830	1.11321	.93034	1.07487	.96344	1.03794	4
57 58		1.15240 1.15172	.89883	1.11256	.93088	1.07425	.96400	1.03734	3 2
59		1.15104	.89988	1.11126	.93197	1.07362	.96457	1.03674	1
60		1.15037	.90040	1.11061	.93252	1.07237	.96569	1.03553	0
-	Cotang	Tang	Cotang	Tang	Cotang	Tang	Cotang	Tang	1
1	-	-	-						1
-	4	49°		49° 48°		4	170	4	1

TABLE XII.-TANGENTS AND COTANGENTS.

1	4	4 °	,	,	4	4°	1,	1,	4	4 °	1,
	Tang	Cotang			Tang	Cotang	6		Tang	Cotang	10
0	.96569	1.03553	60	20	.97700	1.02355	40	40	.98843	1.01170	20
1	.96625	1.03493	59	21	.97756	1.02295	39	41	.98901	1.01112	19
2	.96681	1.03433	58	22	.97813	1.02236	38	42	.98958	1.01053	18
3	.96738	1.03372	57	23	.97870	1.02176	37	43	.99016	1.00994	17
4	.96794	1.03312	56	24	.97927	1.02117	36	44	.99073	1.00935	16
5	.96850	1.03252	55	25	.97984	1.02057	35	45	.99131	1.00876	15
6	.96907	1.03192	54	26	.98041	1.01998	34	46	.99189	1.00818	14
7	.96963	1.03132	53	27	.98098	1.01939	33	47	.99247	1.00759	13
8	.97020	1.03072	52	28	.98155	1.01879	32	48	.99304	1.00701	12
9	.97076	1.03012	51	29	.98213	1.01820	31	49	.99362	1.00642	11
10	.97133	1.02952	50	30	.98270	1.01761	30	50	.99420	1.00583	10
11	.97189	1.02892	49	31	.98327	1.01702	29	51	.99478	1.00525	9
12	.97246	1.02832	48	32	.98384	1.01642	28	52	.99536	1.00467	8
13	.97302	1.02772	47	33	.98441	1.01583	27	53	.99594	1.00408	8
14	.97359	1.02713	46	34	.98499	1.01524	26	54	.99652	1.00350	6 5
15	.97416	1.02653	45	35	.98556	1.01465	25	55	.99710	1.00291	5
16	.97472	1.02593	44	36	.98613	1.01406	24	56	.99768	1.00233	
17	.97529	1.02533	43	37	.98671	1.01347	23	57	.99826	1.00175	3 2
18	.97586	1.02474	42	38	.98728	1.01288	22	58	.99884	1.00116	
19	.97643	1.02414	41	39	.98786	1.01229	21	59	,99942	1.00058	1
20	.97700	1.02355	40	40	.98843	1.01170	20	60	1.00000	1.00000	0
-,	Cotang	Tang	,	,	Cotang	Tang	,	,	Cotang	Tang	,
	45°		900	0	4	5°			4	5°	

TABLE XIII.—VERSINES AND EXSECANTS.

	,	0	ė	1	l°	2	20	8	3°	,
		Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	
	0	.00000	.00000	.00015	.00015	.00061	.00061	.00137	.00137	0
9	1	.00000	.00000	.00016	.00016	.00062	.00062	.00139	00139	1
ı	3	.00000	.00000	.00016	.00016	.00063	.00063	.00140	.00140	2 3
	4	.00000	.00000	.00017	.00017	.00064	.00065	.00143	.00142	.4
3	5	.00000	.00000	.00018	.00018	.00066	.00066	.00145	.00145	5
	6	.00000	.00000	.00018	.00018	.00067	.00067	.00146	.00147	6
-	8	.00000	.00000	.00019	.00019	.00068	.00068	.00148	.00148	5 6 7 8
1	8 9	.00000	.00000	.00020	.00020	.00069	.00069	.00150 .00151	.00150	8 9
	10	.00000	.00000	.00020	.00021	.00071	.00070	.00153	.00151	10
	11	.00001	.00001	.00021	.00021	.00073	.00073	.00154	.00155	11
	12	.00001	,00001	.00022	.00022	.00074	.00074	.00156	.00156	12
1	13	.00001	.00001	.00023	.00023	.00075	.00075	.00158	.00158	13
	14	.00001	.00001	.00023	.00023	.00076	.00076	.00159	.00159	14
	15	.00001	.00001	.00024	.00024	.00077	.00077	.00161	.00161	15
	16 17	.00001	.00001	.00024	.00024	.00078	.00078	.00162	.00163	16
	18	.00001	.00001	.00026	.00026	.00081	.00081	.00166	.00166	18
	19	.00002	.00002	.00026	.00026	.00082	.00082	.00168	.00168	19
	20	.00002	.00002	.00027	.00027	.00083	.00083	.00169	.00169	20
-	21	.00002	.00002	.00028	.00028	.00084	.00084	.00171	.00171	21
	22	.00002	.00002	.00028	.00028	.00085	.00085	.00173	.00173	22
	23	.00002	.00002	.00029	.00029	.00087	.00087	.00174	.00175	23
	24 25	.00002	.00002	.00030	.00030	.00088	.00088	.00176	.00176	24 25
	26	.00003	.00003	.00031	.00031	.00090	.00090	.00179	.00180	26
	27	.00003	.00003	.00032	.00032	.00091	.00091	.00181	.00182	27
	28	.00003	.00003	.00033	.00033	.00093	.00093	.00183	.00183	28
	29	.00004	.00004	.00034	.00034	.00094	.00094	.00185	.00185	29
1				16 0000	1 1 1 1 1 1			The Country	.00187	
	31 32	.00004	.00004	.00035	.00035	.00096	.00097	.00188	.00189	31
	33	.00004	.00005	.00037	.00037	.00098	.00098	.00190	.00190	32
	34	.00005	.00005	.00037	.00037	.00100	.00100	.00194	.00194	34
	35	.00005	.00005	.00038	.00038	.00102	.00102	.00196	.00196	35
1	36	.00005	.00005	.00039	.00039	.00103	-,00103	.00197	.00198	36
ı	37	.00006	.00006	.00040	.00040	.00104	.00104	.00199	.00200	37 38
H	39	.00006	.00006	.00041	.00041	.00107	.00107	.00201	.00201	39
	40	.00007	.00007	.00042	.00042	.00108	.00108	.00205	.00205	40
	41	.00007	.00007	.00043	.00043	.00110	.00110	.00207	.00207	41
	42	.00007	.00007	.00044	.00044	.00111	.00111	.00208	.00209	42
1	43	.00008	.00008	.00045	.00045	.00112	.00113	.00210	.00211	43
	44 45	.00008	.00008	.00046	.00046	.00114	.00114	.00212	.00213	44
Н	46	.00009	.00009	.00048	.00048	.00117	.00117	.00214	.00213	45 46
	47	.00009	.00009	.00048	.00048	.00118	:00118	.00218	.00218	47
ı	48	.00010	.00010	.00049	.00049	.00119	.00120	.00220	.00220	48
	49 50	.00010	.00010	.00050	.00050	.00121	.00121	.00222	.00222	49
					.00051	.00122	.00122	.00224	.00224	50
	51 52	.00011	.00011	.00052	.00052	.00124	.00124	.00226	.00226	51
	53	.00011	.00011	.00054	.00053	.00125	.00125	.00228	.00228	52 53
1	54	.00012	.00012	.00055	.00055	.00128	.00128	.00232	.00232	54
	55	.00013	.00013	.00056	.00056	.00130	.00130	.00234	.00234	55
	56 57	.00013	.00013	.00057	.00057	.00131	.00131	.00236	.00236	56
	58	.00014	.00014	.00058	.00058	.00133	.00133	.00238	.00238	57
	59	.00015	.00015	.00060	.00060	.00134	.00136	.00240	.00242	59
	60	.00015	.00015	.00061	.00061	.00137	.00137	.00244	.00244	60

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	,	4	Į°		je	(3°	77	10	,
		Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	
1	0	.00244	.00244	.00381	.00382	.00548	.00551	.00745	.00751	0
	1	.00246	.00246	.00383	.00385	.00551	.00554	.00749	.00755	1
	2 3	.00248	.00248	.00386	.00387	.00554	.00557	.00752	.00758	2
	1	.00250 $.00252$.00250	.00388	.00390	.00557	.00560	.00756	.00762	1
13	4 5 6 7	.00254	.00254	.00393	.00395	.00563	.00566	.00763	.00769	2 3 4 5 6 7
	6	.00256	.00257	.00396	.00397	.00566	.00569	.00767	.00773	6
	7	.00258	.00259	.00398	.00400	.00569	.00573	.00770	.00776	7
100	8 9	.00260	.00261	.00401	.00403	.00572	.00576	.00774	.00780	8 9
1	10	.00264	.00265	.00404	.00405	.00579	.00579	.00781	.00784	10
	11	.00266	.00267	.00409	.00411	.00582	.00585	.00785	.00791	11
	2	.00269	.00269	.00403	.00411	.00585	.00588	.00789	.00795	12
1	13	.00271	.00271	.00414	.00416	.00588	.00592	.00792	.00799	13
1	14	.00273	.00274	.00417	.00419	.00591	.00595	.00796	.00802	14
	15	.00275	.00276	.00420	.00421	.00594	00598	.00800	.00806	15
	16	.00277	.00278	.00422	.00424	.00598	.00601	.00803	.00810	16 17
	18	.00279	.00282	.00425	.00427	.00601	.00604	.00807	.00813	18
	19	.00284	.00284	.00430	.00432	.00607	.00611	.00814	.00821	19
	20	.00286	.00287	.00433	.00435	.00610	.00614	.00818	.00825	20
1 5	21	.00288	.00289	.00436	.00438	.00614	.00617	.00822	.00828	21
1 %	22	.00290	.00291	.00438	.00440	.00617	.00621	.00825	.00832	22
	23	.00293	.00293	.00441	.00443	.00620	.00624	.00829	.00836	23
	24	.00295	.00296	.00444	.00446	.00623	.00627	.00833	.00840	24 25
1 6	25	.00297 $.00299$.00298	.00447	.00449	.00626	.00630	.00837	.00844	26
	27	.00301	.00302	.00452	.00451	.00633	.00637	.00844	.00851	27
1 %	28	.00304	.00305	.00455	.00457	.00636	.00640	.00848	.00855	28
1 %	29	.00306	.00307	.00458	.00460	.00640	.00644	.00852	.00859	29
1	30	.00308	.00309	.00460	.00463	.00643	.00647	.00856	.00863	30
	31	.00311	.00312	.00463	.00465	.00646	.00650	.00859	.00867	31
100	32	.00313	.00314	.00466	.00468	.00649	.00654	.00863	.00871	32
	34	.00315	.00316	.00469	.00471	.00653	.00657	.00871	.00878	34
	35	.00320	.00318	.00474	.00477	.00659	.00664	.00875	.00882	35
1 8	36	.00322	.00323	.00477	.00480	.00663	.00667	.00878	.00886	36
1 8	37	.00324	.00326	.00480	.00482	.00666	.00671	.00882	.00890	37
	38	.00327	.00328	.00483	.00485	.00669	.00674	.00886	.00894	38
	10	.00329	.00330	.00486	.00488	.00673	.00677	.00890	.00902	40
1	11	.00334	.00335	.00493	.00494	.00680	.00684	.00898	.00906	41
	12	.00334	.00337	.00492	.00494	,00683	.00688	.00902	.00910	42
	13	.00339	.00340	.00497	.00500	.00686	.00691	.00906	.00914	43
4	14	.00341	.00342	.00500	.00503	.00690	.00695	.00909	.00918	44
	15	.00343	.00345	.00503	.00506	.00693	.00698	.00913	.00922	45
	16	.00346	.00347	.00506	.00509	.00697	.00701	.00917	.00926	46
	18	.00348	.00350	.00509	.00512	.00700	.00705	.00921	.00930	48
	19	.00353	.00354	.00512	.00518	.00707	.00712	.00929	.00938	49
	50	.00356	.00357	.00518	.00521	.00710	.00715	.00933	.00942	50
	51	.00358	.00359	.00521	.00521	.00714	.00719	.00937	.00946	51
1	52	.00361	.00362	.00524	.00527	.00717	.00722	.00941	.00950	52
	53	.00363	.00364	.00527	.00530	.00721	.00726	.00945	.00954	53 54
	54 55	.00365	.00367	.00530	.00533	.00724	.00730	.00949	.00958	55
	56	.00370	.00372	.00536	.00539	.00731	.00737	.00957	.00966	56
1	57	.00373	.00374	.00539	.00542	.00735	.00740	.00961	.00970	57
	58	.00375	.00377	.00542	.00545	.00738	.00744	.00965	.00975	58
	59	.00378	.00379	.00545	.00548	.00742	.00747	.00969	.00979	59 60
L	60 l	.00381	1 .00382	.00548	.00551	.00745	.00751	61600.	1 .00903	00

TABLE XIII,-VERSINES AND EXSECANTS.

7										
	,	8	30	9)0	1	0°	1:	1°	,
-		Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	
	0	.00973	.00983	.01231	.01247	.01519	.01543	.01837	.01872	0
	1	.00977	.00987	.01236	.01251	.01524	.01548	.01843	.01877	0
1	2	.00981	.00991	.01240	.01256	.01529	.01553	.01848	.01883	2 3
	3	.00985	.00995	.01245	.01261	.01534	.01558	.01854	.01889	3
1	4	.00989	.00999	.01249	.01265	.01540	.01564	.01860	.01895	4
	5	.00994	.01004	.01254	.01270	.01545	.01569	.01865	.01901	5
	0	.00998	.01008	01209	01270	.01550	.01574	.01871	.01906	0
	2345678	.01002	.01016	.01259 .01263 .01268	.01270 .01275 .01279 .01284	.01560	.01579 .01585	.01882	.01918	5 6 7 8
	9	.01010	.01020	.01272	.01289	.01565	.01590	.01888	.01924	9
	10	.01014	.01024	.01277	.01294	.01570	.01595	.01893	.01930	10
	11	.01018	.01029	.01282	.01298	.01575	.01601	.01899	.01936	11
	13	.01022	.01033	.01286	.01303	.01580	.01606	.01904	.01941	12
	13	.01027	.01037	.01291	.01308	.01586	.01611	.01910	.01947	13
1	14	.01031	.01041	.01296	.01313	.01591	.01616	.01916	.01953	14
1	15 16	.01035	.01046	.01300	.01318	.01596	.01622	.01921	.01959	15 16
	17	.01043	.01054	.01310	.01327	.01606	.01633	.01933	.01903	17
	18	.01047	.01059	.01314	.01332	.01612	.01638	.01939	.01977	18
3	19	.01052	.01063	.01319	.01337	.01617	.01643	.01944	.01983	19
	20	.01056	.01067	.01324	.01342	.01622	.01649	.01950	.01989	20
	21	.01060	.01071	.01329	.01346	.01627	.01654	.01956	.01995	21
	22	.01064	.01076	.01333	.01351	.01632	.01659	.01961	.02001	22
	23	.01069	.01080	.01338	.01356	.01638	.01665	.01967	.02007	23
	24 25	.01073	.01084	.01343	.01361	.01643	.01670	.01973	.02013	24
	25	.01081	.01093	.01352	.01366	.01653	.01676	.01979	.02019	25 26
	27	.01086	.01097	.01357	.01376	.01659	.01687	.01990	.02031	27
	28	.01090	.01102	.01362	.01381	.01664	.01692	.01996	.02037	28
	29	.01094	.01106	.01367	.01386	.01669	.01698	.02002	.02043	29
	30	.01098	.01111	.01371	.01391	.01675	.01703	.02008	.02049	30
	31	.01103	.01115	.01376	.01395	.01680	.01709	.02013	.02055	31
	32	.01107	.01119	.01381	.01400	.01685	.01714	.02019	.02061	32
	33	.01111	.01124	.01386	.01405	.01690	.01720 .01725 .01731	.02025	.02067	33
	35	.01120	.01133	.01396	.01410	.01696	01725	.02031	.02073	34 35
	36	.01124	.01137	.01400	.01420	.01706	01736	.02042	.02085	36
	37	.01129	.01142	.01405	.01425	.01706 .01712	.01736 .01742	.02048	.02091	37
	38	.01133	.01146	.01410	.01430	.01717	.01747	.02054	.02097	38
	39	.01137	.01151	.01415	.01435	.01723	.01753	.02060	.02103	39
	40	.01142	.01155	.01420	.01440	.01728	.01758	.02066	.02110	40
	41	.01146	.01160	.01425	.01445	.01733	.01764	.02072	.02116	41
	42 43	.01151	.01164	.01430	.01450	.01739	.01769	.02078	.02122	42
	44	.01159	.01173	.01435	.01455	.01744	.01775	.02084	.02128	43
	45	.01164	.01178	.01444	.01466	.01755	.01786	.02095	.02140	45
	46	.01168	.01182	.01449	.01471	.01760	01792	.02101	.02146	46
	47	.01173	.01187	.01454	.01476	.01766	.01798	.02107	.02153	47
	48	.01177	.01191	.01459	.01481	.01771	.01803	.02113	.02159	48
	49 50	.01182	.01196	.01464	.01486	.01777	.01809	.02119	.02165	49
	-		1	.01469	-01491	.01782	.01815	.02125	.02171	50
	51 52	.01191	.01205	.01474	.01496	.01788	.01820	.02131	.02178	51 52
	53	.01200	.01214	.01484	.01506	.01799	.01832	.02143	.02184	53
	54	.01204	.01219 .01223	.01489	.01512	.01804	.01837	.02149	.02196	54
	55	.01209	.01223	.01494	.01517	.01810	.01843	.02155	.02203	55
	56	.01213	.01228	.01499	.01522	.01815	.01849	.02161	.02209	56
	57 58	.01218	.01233	.01504	.01527	.01821	.01854	.02167	.02215	57
	59	.01222	.01237	.01509	.01532	.01826	.01860	.02173	.02221	58
	60	.01231	.01247	.01514	.01537	.01837	.01866	.02179	.02234	59 60
	-			,	.01010	.01001	01010			, 00

ı												
	,	1	2°	1	3°	1	4°	1	5°	,		
-		Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.			
1	0	.02185	.02234	.02563	.02630	.02970	.03061	.03407	.03528	0		
	1	.02191	.02240	.02570	.02637	.02977	.03069	.03415	.03536	1		
1	2 3	.02197	.02247	.02576	.02644	.02985	.03076	.03422	.03544	2 3		
	3	.02203	.02253	.02583	.02651	.02992	.03084	.03430	.03552	3		
ı	4	.02210	.02259	.02589	.02658	.02999	.03091	.03438	.03560	4		
8	0	.02216	.02266	.02596	.02665	.03006	.03099	.03445	.03568	5		
	77	.02222	.02272	.02602	.02672	.03013	.03106	.03453	.03576	6		
	4 5 6 7 8	.02234	.02285	.02616	.02686	.03027	.03121	.03468	.03584	5 6 7 8		
	9	.02240	.02291	.02622	.02693	.03034	.03129	.03476	.03601	9		
3	10	.02246	.02298	.02629	.02700	.03041	.03137	.03483	.03609	10		
	11	.02252	.02304	.02635	.02707	.03048	.03144	.03491	.03617			
	12	.02258	.02311	.02642	.02714	.03055	.03152	.03498	.03625	11 12		
1	13	.02265	.02317	.02649	02721	.03063	.03159	.03506	.03633	13		
	14	.02271	.02323	.02655	.02728	.03070	.03167	.03514	.03642	14		
	15	.02277	.02330	.02662	.02728 .02735	.03077	.03175	.03521	.03650	15		
	16	.02283	.02336	.02669	:02742	.03084	.03182	.03529	.03658	16		
	17	.02289	.02343	.02675	.02749	.03091	.03190	.03537	.03666	17		
	18 19	.02295	.02349	.02682	.02756	.03098	.03198	.03544	.03674	18		
	20	.02308	.02362	.02696	.02770	.03100	.03213	.03552	.03683	19 20		
		W75 1 1 1 1 1 1	100,000	The State of the S		100		THE PERSON NAMED IN	252111100			
1	21 22	.02314	.02369	.02702	.02777	.03120	.03221	.03567	.03699	21		
	23	.02327	.02382	.02709	.02784	.03127	.03228	.03575	.03708	22 23		
	24	.02333	.02388	.02722	.02799	.03142	.03244	.03590	03794	24		
1	25	.02339	.02395	02729	.02806	.03149	.03251	.03598	.03724	25		
	26	.02345	.02402	.02736	.02813	.03156	.03251	.03606	.03741	26		
	27	.02352	.02408	.02736 .02743	.02820	.03163	.03267	.03614	.03741 .03749 .03758	27		
	28	.02358	.02415	.02749	.02827	.03171	.03275	.03621	.03758	28		
	29 30	.02364	.02421	.02756	.02834	.03178	.03282	.03629	.03766	29		
		No. of Persons and	(C)/LD((L))	-	1000	113-114-11-11	3 3 3 5 E	.03637	.03774	30		
	31	.02377	.02435	.02770	.02849	.03193	.03298	.03645	.03783	31		
	32 33	.02383	.02441	.02777	.02856	.03200	.03306	.03653	.03791	32		
	34	.02396	.02454	.02790	.02870	.03214	.03313	.03660	.03799	33 34		
	35	.02402	.02461	.02797	.02878	.03222	.03329	.03676	.03816	35		
	36	.02408	.02468	.02804	.02885	.03229	.03337	.03684	.03825	36		
	37	.02415	.02474	.02811	.02892	.03236	.03345	.03692	.03833	37		
	38	.02421	.02481	.02818	.02899	.03244	.03353	.03699	.03842	38		
	39 40	.02427	.02488	.02824	.02907	.03251	.03360	.03707	.03850	39		
		OURSELL AND	.02494	.02831	.02914	.03258	.03368	.03715	.03858	40		
	41	.02440	.02501	.02838	.02921	.03266	.03376	.03723	.03867	41		
	42	.02447	.02508	.02845	.02928	.03273	.03384	.03731	.03875	42		
	43	.02453	.02515	.02852	.02936	.03281	.03392	.03739	.03884	43		
	45	.02466	.02528	.02866	.02950	.03295	.03408	.03754	.03901	45		
	46	.02472	.02535	.02873	.02958	.03303	.03416	.03762	.03909	46		
	47	.02479	.02542	.02880	.02965	.03310	.03424	.03770	.03918	47		
	48	.02485	.02548	.02887	.02972	.03318	.03432	.03778	.03927	48		
	49 50	.02492	.02555	.02894	.02980	.03325	.03439	.03786	.03935	49		
	1000	1.53	17 1000	.02900	.02987	.03333	.03447		.03944	50		
1	51 52	.02504	.02569	.02907	.02994	.03340	.03455	.03802	.03952	51		
1	53	.02517	.02576	.02914	.03002	.03347	.03463	.03810	.03961	52 53		
	54	.02524	.02589	.02928	.03017	.03362	.03479	.03826	.03978	54		
-	55	.02530	.02596	.02935	.03024	.03370	.03487	.03834	.03987	55		
	56	.02537	.02603	.02942	.03032	.03377	.03495	.03842	.03995	56		
1	57	.02543	.02610	.02949	.03039	.03385	.03503	.03850	.04004	57		
	-58 59	.02550	.02617	.02956	.03046	.03392	.03512	.03858	.04013	58		
1	60	.02556	.02624	.02963	.03054	.03400	.03520	.03866	.04021	59		
-	00	. ONOOO	1 .00000	1 .00010	TOOOT	100401	1 00000	1,00014	.03000	00		

	(S) (1) (A)	6°	13	70	1	8°	19	90	
,	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	,
0	.03874	,04030	.04370	.04569	.04894	.05146	.05448	.05762	0
1	.03882	.04039	.04378	.04578	.04903	.05156	.05458	.05773	1
2	.03890	.04047	.04387	.04588	.04912	.05166	.05467	.05783	2
2 3 4 5 6	.03898	.04056	.04395	.04597	.04921	.05176	.05477	.05794	3 4
4	.03906	.04065	.04404	.04606	.04930	.05186	.05486	.05805	4
5	.03914	.04073	.04412	.04625	.04948	.05206	.05505	.05826	5 6 7 8
7	.03930	.04091	.04429	.04635	.04957	.05216	.05515	.05836	7
8	.03938	.04100	.04438	.04644	.04967	.05226	.05524	.05847	8
9	.03946	.04108	.04446	.04653	.04976	.05236	.05534	.05858	9
10	.03954	.04117	.04455	.04663	.04985	.05246	.05543	.05869	10
11	.03963	.04126	.04464	.04672	.04994	.05256	.05553	.05879	11
12	.03971	.04135	.04472	.04682	.05003	.05266	.05562	.05890	12
13	.03979	.04144	.04481	.04691	.05012	.05276	.05572	.05901	13
14	.03987	.04152	.04489	.04700	.05021	.05286	.05582	.05911	14 15
15 16	.04003	.04170	.04507	.04719	.05039	.05307	.05601	.05933	16
17	.04011	.04179	.04515	.04729	.05048	.05317	.05610	.05944	17
18	.04019	.04188	.04524	.04738	.05057	.05327	.05620	.05955	18
19	.04028	.04197	.04533	.04748	.05067	.05337	.05630	.05965	19
20	.04036	.04206	.04541	.04757	.05076	.05347	.05639	.05976	20
21	.04044	.04214	.04550	.04767	.05085	.05357	.05649	.05987	21
22 23	.04052	.04223	.04559	.04776	.05094	.05367	.05658	.05998	22
23	.04060	.04232	.04567	.04786	.05103	.05378	.05668	.06009	23
24 25	.04069	.04241	.04576	.04795	.05112	.05388	.05678	.06020	24 25
26	.04085	.04259	.04593	.04815	.05131	.05408	.05697	.06041	26
27	.04093	.04268	.04602	.04824	.05140	.05418	.05707	.06052	27
28	.04102	.04277	.04611	.04834	.05149	.05429	.05716	.06063	28
29	.04110	.04286	.04620	.04843	.05158	.05439	.05726	.06074	29
30	.04118	.04295	.04628	.04853	.05168	.05449	.05736	.06085	30
31	.04126	.04304	.04637	.04863	.05177	.05460	.05746	.06096	31
32	.04135	.04313	.04646	.04872	.05186	.05470	.05755	.06107	32
33 34	.04143	.04322	.04655	.04882	.05195	.05480	.05765	.06118	33
35	.04159	.04340	.04672	.04901	.05203	.05501	.05785	.06140	35
36	.04168	.04349	.04681	.04911	,05223	.05511	.05794	.06151	36
37	.04176	.04358	.04690	.04920	.05232	.05521	.05804	.06162	37
38	.04184	.04367	.04699	.04930	.05242	.05532	.05814	.06173	38
39	.04193	.04376	.04707	.04940	.05251	.05542	.05824	.06184	39
40	.04201	.04385	.04716	.04950	17.00	.05552	.05833	.06195	40
41	.04209	.04394	.04725	.04959	.05270	.05563	.05843	.06206	41
42 43	.04218	.04403	.04734	.04969	.05279	.05573	.05853	.06217	42 43
44	.04234	.04413	04752	.04919	.05298	.05594	.05873	.06239	44
45	.04243	.04431	.04752 .04760	.04998	.05307	.05604	.05882	.06250	45
46	.04251	.04440	.04769	.05008	.05316	05615	.05892	.06261	46
47	.04260	.04449	.04778 .04787	.05018	.05326	.05625	.05902	.06272	47
48	.04268	.04458	.04787	.05028	.05335	.05636	.05912	.06283	48
50	.04276	.04468	.04796	.05088	.05344	.05646	.05922	.06295	49 50
51	.04293	.04486	.04814	.05057	.05363	.05667	.05942	.06317	51
52	.04293	.04495	04814	.05067	.05373	.05678	.05942	.06328	52
53	.04310	.04504	.04832	.05077	.05382	.05688	.05961	.06339	53
54	.04319	.04514	.04841.	.05087	.05391	.05699	.05971	.06350	54
55	.04327	.04523	.04850	.05097	.05401	.05709	.05981	.06362	55
56	.04336	.04532	.04858	.05107	.05410	.05720	.05991	.06373	56 57
58	.04353	.04541	.04807	.05116	.05429	.05730	.06001	.06395	58
59	.04361	.04560	.04885	.05136	.05439	.05751	.06021	.06407	59
60	.04370	.04569	.04894	.05146	.05448	.05762	.06031	.06418	60

II III	
, 20° 21°	22° 23°
Vers. Exsec. Vers. Exsec. Ve	s. Exsec. Vers. Exsec.
0 .06031 .06418 .06642 .07115 .073	82 .07853 .07950 .08636 0
1 .06041 .06429 .06652 .07126 .07	93 .07866 .07961 .08649 1
2 .06051 .06440 .06663 .07138 .073 3 .06061 .06452 .06673 .07150 .073	03 .07879 .07972 .08663 2 14 .07892 .07984 .08676 3
3 .06061 .06452 .06673 .07150 .07	14 .07892 .07984 .08676 3
4 .06071 .06463 .06684 .07162 .07 5 .06081 .06474 .06694 .07174 .07	25 .07904 .07995 .08690 4 36 .07917 .08006 .08703 5
6 .06091 .06486 .06705 .07186 .07	47 .07930 .08018 .08717 6
7 .06101 .06497 .06715 .07199 .07	58 07943 08029 08730 7
8 .06111 .06508 .06726 .07211 .07	
9 .06121 .06520 .06736 .07223 .07	
10 .06131 .06531 .06747 .07235 .07	
11 .06141 .06542 .06757 .07247 .07	
12 .06151 .06554 .06768 .07259 .07	
13 .06161 .06565 .06778 .07271 .07 14 .06171 .06577 .06789 .07283 .07	
15 .06181 .06588 .06799 .07295 .07	46 .08045 .08121 .08839 15
16 .06191 .06600 .06810 .07307 .07	57 .08058 .08132 .08852 16
17 .06201 .06611 .06820 .07320 .07	
18 .06211 .06622 .06831 .07332 .07	79 .08084 .08155 .08880 18
19 .06221 .06634 .06841 .07344 .07	90 .08097 .08167 .08893 19
20 .06231 .06645 .06852 .07356 .07	
21 .06241 .06657 .06863 .07368 .07	
22 .06252 .06668 .06873 .07380 .07	23 .08135 .08201 .08934 22
23 .06262 .06680 .06884 .07393 .07	
24 .06272 .06691 .06894 .07405 .07 25 .06282 .06703 .06905 .07417 .07	
26 .06292 .06715 .06916 .07429 .07	
27 .06302 .06726 .06926 .07442 .07	79 .08200 .08259 .09003 27
28 .06312 .06738 .06937 .07454 .07	
29 .06323 .06749 .06948 .07466 .07	
30 .06333 .06761 .06958 .07479 .07	
31 .06343 .06773 .06969 .07491 .07	323 .08252 .08306 .09058 31
32 .06353 .06784 .06980 .07503 .07 33 .06363 .06796 .06990 .07516 .07	334 .08265 .08317 .09072 32 45 .08278 .08329 .09086 33
33 .06363 .06796 .06990 .07516 .07 34 .06374 .06807 .07001 .07528 .07	
35 .06384 .06819 .07012 .07540 .07	
36 .06394 .06831 .07022 .07553 .07	379 .08318 .08364 .09127 36
37 .06404 .06843 .07033 .07565 .07	90 .08331 .08375 .09141 37
38 .06415 .06854 .07044 .07578 .07	01 .08344 .08387 .09155 38
39 .06425 .06866 .07055 .07590 .07 40 .06435 .06878 .07065 .07602 .07	13
	The second secon
41 .06445 .06889 .07076 .07615 .07 42 .06456 .06901 .07087 .07627 .07	
43 .06466 .06913 .07098 .07640 .07	
44 .06476 .06925 .07108 .07652 .07	69 .08423 .08457 .09238 44
45 .06486 .06936 .07119 .07665 .07	80 .08436 .08469 .09252 45
46 .06497 .06948 .07130 .07677 .07	91 .08449 .08481 .09266 46
47 .06507 .06960 .07141 .07690 .07	
48 .06517 .06972 .07151 .07702 .07 49 .06528 .06984 .07162 .07715 .07	14 .08476 .08504 .09294 48 25 .08489 .08516 .09308 49
50 .06538 .06995 .07173 .07727 .07	36 .08503 .08528 .09323 .50
51 .06548 .07007 .07184 .07740 .07	48 .08516 .08539 .09337 51
52 .06559 .07019 .07195 .07752 .07	59 .08529 .08551 .09351 52
53 .06569 .07031 .07206 .07765 .07	70 .08542 .08563 .09365 53
54 .06580 .07043 .07216 .07778 .07	81 .08556 .08575 .09579 54
55 .06590 .07055 .07227 .07790 .07 56 .06600 .07067 .07238 .07803 .07	
56 .06600 .07067 .07238 .07803 .07 57 .06611 .07079 .07249 .07816 .07	
58 .06621 .07091 .07260 .07828 .07	27 .08609 .08622 .09435 58
59 .06632 .07103 .07271 .07841 .07	38 .08623 .08634 .09449 59
60 .06642 .07115 .07282 .07853 .07	50 .08636 .08645 .09464 60

TABLE XIII.—VERSINES AND EXSECANTS.

	2	4°	2	5°	2	6°	2	70	
	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	
-	.08645	.09464	.09369	.10338	.10121	.11260	,10899	.12233	0
0 1 2 3	.08657	.09478	.09382	.10353	10133	11976	.10913	.12249	1
2	.08669	.09492	.09394	.10368	10146	.11292	10926	.12266	2
3	.08681	.09506	.09406	.10383	.10146	11308	.10939	.12283	2 3
4	.08693	.09520	.09418	.10398	.10172	.11323	.10952	.12299	4
4 5 6 7	.08705	.09535	.09431	.10413	.10184	.11339	.10965	.12316	4 5 6 7
6	.08717	.09549	.09443	.10428	.10197	.11355	.10979	.12333	6
7	.08728	.09563	.09455	.10443	.10210	.11371	.10992	.12349	7
8	.08740	.09577	.09468	.10458	.10223	.11387	.11005	.12366	8
9	.08752	.09592	.09480	.10473	.10236	.11403	.11019	.12383	9
10	.08764	.09606	.09493	.10488	.10248	.11419	.11032	.12400	10
			THE PERSON NAMED IN		1				1.11
11	.08776	.09620	.09505	.10503	.10261	.11435	.11045	.12416	11
12	.08788	.09635	.09517	.10518	.10274	.11451	.11058	.12433	12
13	.08800	.09649	.09530	.10533	.10287	.11467	.11072	.12450	13
14	.08812	.09663	.09542	.10549	.10300	.11483	.11085	.12467	14
15	.08824	.09678	.09554	.10564	.10313	.11499	.11098	.12484	15
16	.08836	.09692	.09567	.10579	.10326	.11515	.11112	.12501	16
17	.08848	.09707	.09579	.10594	.10338	.11531	.11125	.12518	17
18	.08860	.09721	.09592	.10609	.10351	.11547	.11138	.12534	18
19	.08872	.09133	.09604	.10625	.10364	.11563	.11152	.12551 .12568	19
20	.08884	.09750	.09617	.10040	.10377	.11579	.11100	.12508	20
21	.08896	.09764	.09629	.10655	.10390	.11595	.11178	.12585	21
22	.08908	.09779	.09642	.10670	.10403	.11611	.11192	.12602	22
23	.08920	.09793	.09654	1.10686	.10416	.11627	.11205	.12619	23
24	.08932	.09808	.09666	.10701 .10716	.10429	.11643	.11218	.12636	24
25	.08944	.09822	.09679	.10716	.10442	.11659	.11232	.12653	25
26	.08956	.09837	.09691	.10731	.10455	.11675	.11245	.12670	26
27	.08968	.09851	.09704	.10747	.10468	.11691	.11259	.12687	27
28	.08980	.09866	.09716	.10762	.10481	.11708	.11272	.12704	28
29	.08992	.09880	.09729	.10777	.10494	.11724	.11285	.12721	29
30	.09004	.09895	.09741	.10793	.10507	.11740	.11299	.12738	30
31	.09016	.09909	.09754	.10808	.10520	.11756	.11312	.12755	31
32	.09028	.09924	.09767	.10824	.10533	.11772	.11326	.12772	32
33	.09040	.09939	.09779	.10839	.10546	.11789	.11339	.12789	33
34	.09052	.09953	.09792	.10854	.10559	.11805	,11353	.12807	34
35	.09064	.09968	.09804	.10870	.10572	.11821	.11366	.12824	35
36	.09076	.09982	.09817	.10885	.10585	.11838	.11380	.12841	36
37	.09089	.09997	.09829	.10901	.10598	.11854	.11393	.12858	37
38	.09101	.10012	.09842	.10916	.10611	.11870	.11407	.12875	38
39	.09113	.10026	.09854	.10932	.10624	.11886	.11420	.12892	39
40	.09125	.10041	.09867	.10947	.10637	.11903	.11434	.12910	40
41	.09137	.10055	.09880	.10963	.10650	.11919	,11447	.12927	41
42	.09149	.10071	.09892	10978	.10663	.11936	.11461	19044	42
43	.09161	.10085	.09905	.10978	10676	.11952	.11474	.12944 .12961	43
41	.09174	.10100	.09918	.11009	10689	.11968	.11488	.12979	44
45	.09186	.10115	.09930	.11025	.10689 .10702 .10715 .10728 .10741	.11985	.11501	.12996	45
46	.09198	.10130	.09943	.11041	10715	12001	.11515	.13013	46
47	09910	.10144	.09955	.11056	10728	.12018	.11528	.13031	47
48	.09222	.10159	.09968	.11072	10741	.12034	.11542	.13048	48
49	.09234	.10159 .10174	.09981	.11087	.10755	.12051	.11555	.13065	49
50	.09247	.10189	.09993	.11103	.10768	.12067	.11569	.13083	50
51	.09259	.10204	COMMON A	100000000000000000000000000000000000000	12 - 12 - 12 - 12 - 12 - 12 - 12 - 12 -	TO STATE OF THE PARTY OF THE PA	C. Shares and	13 Dayson C	11
52	.09239	.10204	.10006	.11119	.10781	.12084	.11583	.13100	51
53	.09283	.10218	.10019	.11134	.10794	.12100	.11596	.13117	52
54	.09283	.10233	.10032	.11166	.10807		.11610	.13135	53
55	.09308	.10263	.10057		.10833	.12133	.11623	.13152	54
56	.09320	.10203	.10037	.11181	.10833	.12150	.11637	.13170	55 56
57	.09332	.10278	.10070	.11213	.10847	.12166	.11651	.13187	500
58	.09345	.10308	.10095	.11213	.10860	.12183	.11664	.13205	57 58
59	.09357	.10323	.10108	.11244	.10886	.12216	.11692	.13240	59
60	.09369	.10338	.10121	.11260	.10899	.12233	.11705	.13257	60

					LIS AND	EASEC		11-11-11	
1	2	28°	2	9°	3	0° .	3	1°	
	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	
2 2 2 4 4 5 6 6 7 8 8 9 10 10 10 10 10 10 10 10 10 10 10 10 10	.11719 .11733 .11746 .11760 .11774 .11787 .11801 .11815 .11828 .11842	.13257 .13275 .13292 .13310 .13327 .13345 .13362 .13380 .13398 .13415 .13433	.12538 .12552 .12566 .12580 .12595 .12699 .12623 .12637 .12651 .12665 .12679	.14335 .14354 .14372 .14391 .14409 .14428 .14446 .14465 .14483 .14502 .14521	.13397 .13412 .13427 .13441 .13456 .13470 .13485 .13499 .13514 .13529 .18543	.15470 .15489 .15509 .15528 .15548 .15567 .15587 .15606 .15626 .15645 .15665	.14283 .14298 .14313 .14328 .14343 .14358 .14373 .14388 .14403 .14418 .14433	.16663 .16684 .16704 .16725 .16745 .16766 .16786 .16827 .16848 .16868	0 1 2 3 4 5 6 7 8 9
11 12 13 14 15 16 17 18 19 20	.11883 .11897 .11911 .11925 .11938 .11952 .11966	.13451 .13468 .13486 .13504 .13521 .13539 .13577 .13575 .13593 .13610	.12694 .12708 .12722 .12736 .12750 .12765 .12779 .12793 .12807 .12822	.14539 .14558 .14576 .14595 .14614 .14632 .14651 .14670 .14689 .14707	.13558 .13573 .13587 .13602 .13616 .13631 .13646 .13660 .13675 .13690	.15684 .15704 .15724 .15743 .15763 .15782 .15802 .15822 .15841 .15861	.14449 .14464 .14479 .14494 .14509 .14524 .14539 .14554 .14569 .14584	.16889 .16909 .16930 .16950 .16971 .16992 .17012 .17033 .17054 .17075	11 12 13 14 15 16 17 18 19 20
21 22 23 24 25 26 27 28 29 30	.12035	.13628 .13646 .13664 .13682 .13700 .13718 .13735 .13773 .13771 .13789	.12936 .12850 .12864 .12879 .12893 .12907 .12921 .12936 .12950 .12964	.14726 .14745 .14764 .14782 .14801 .14820 .14839 .14858 .14877 .14896	.13705 .13719 .13734 .13749 .13763 .13778 .13793 .13608 .13822 .13837	.15881 .15901 .15920 .15940 .15960 .15980 .16000 .16019 .16039 .16059	.14599 .14615 .14630 .14645 .14660 .14675 .14690 .14706 .14721 .14736	.17095 .17116 .17137 .17158 .17178 .17199 .17220 .17241 .17262 .17283	21 22 23 24 25 26 27 28 29 30
31 32 33 34 35 36 37 38 39 40	.12244 .12257	.13807 .13825 .13843 .13861 .13879 .13897 .13916 .13934 .13952 .13970	.12979 .12993 .13007 .13022 .13036 .13051 .13065 .13079 .13094 .13108	.14914 .14933 .14952 .14971 .14990 .15009 .15028 .15047 .15066 .15085	.13852 .13867 .13881 .13896 .13911 .13926 .13941 .13955 .13970 .13985	.16079 .16099 .16119 .16139 .16159 .16179 .16199 .16219 .16239 .16259	.14751 .14766 .14782 .14797 .14812 .14827 .14843 .14858 .14873 .14888	.17304 .17325 .17346 .17367 .17388 .17409 .17430 .17451 .17472 .17493	31 32 33 34 35 36 37 38 39 40
41 42 43 44 45 46 47 48 49 50	.12299 .12313 .12327 .12341 .12355 .12369 .12383	.13988 .14006 .14024 .14042 .14061 .14079 .14097 .14115 .14134 .14152	.13129 .13137 .13151 .13166 .13180 .13195 .13209 .13233 .13238 .13252	.15105 .15124 .15143 .15162 .15181 .15200 .15219 .15239 .15258 .15277	.14000 .14015 .14030 .14044 .14059 .14074 .14089 .14104 .14119 .14134	.16279 .16299 .16319 .16339 .16359 .16380 .16400 .16420 .16440 .16460	.14904 .14919 .14934 .14949 .14965 .14980 .14995 .15011 .15026 .15041	.17514 .17535 .17556 .17577 .17598 .17620 .17641 .17662 .17683 .17704	41 42 43 44 45 46 47 48 49 50
51 52 53 54 55 56 -57 58 59 60	.12411 .12425 .12439 .12454 .12468 .12482 .12496 .12510 .12524 .12538	.14170 .14188 .14207 .14225 .14243 .14262 .14280 .14299 .14317 .14335	.13267 .13281 .13296 .13310 .13325 .13339 .13354 .13368 .13383 .13397	.15296 .15315 .15385 .15354 .15373 .15393 .15412 .15431 .15451 .15470	.14149 .14164 .14179 .14194 .14208 .14223 .14238 .14253 .14268 .14283	.16481 .16501 .16521 .16541 .16562 .16582 .16602 .16623 .16643 .16663	.15057 .15072 .15087 .15103 .15118 .15134 .15149 .15164 .15180	.17726 .17747 .17768 .17790 .17811 .17832 .17854 .17875 .17896 .17918	51 52 53 54 55 56 57 58 59 60

	,	3:	2°	3	3°	3	4°	3	5°	١,
		Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	
F	0	.15195	.17918	,16133	.19236	.17096	.20622	.18085	.22077	0
	1	.15211	.17939	.16149	.19259	.17113	.20645	.18101	.22102	1
	2 3	.15226	.17961	.16165	.19281	.17129	.20669	.18118	.22127	2 3
	3	.15241	.17982	.16181	.19304	.17145	.20693	.18135	.22152	3
8	4	.15257	.18004	.16196	.19327	.17161	.20717	.18152	.22177	4
Н	5	.15272	.18025	.16212	.19349	.17178	.20740	.18168	22227	5
	6	.15288	.18047	.16228	.19372	.17194	.20764	.18202	.22252	7
	7 8	.15303	.18090	.16260	.19417	.17227	.20812	.18218	.22277	5678
	9	.15334	.18111	.16276	.19440	.17243	.20836	.18235	.22302	9
	10	.15350	.18133	.16292	.19463	.17259	.20859	.18252	.22327	10
	11	.15365	.18155	.16308	.19485	.17276	.20883	.18269	.22352	11
	12	.15381	.18176	.16324	.19508	.17292	.20907	.18286	.22377	12
	13	.15396	.18198	.16340	.19531	.17308	.20931	.18302	.22402	13
	14	.15412	.18220	.16355	.19554	.17325	.20955	.18319	.22428	14
	15	.15427	.18241	.16371	.19576	.17341	.20979	.18336	.22453	15
	16	.15443	.18263	.16387	.19599	.17357	.21003	.18353	.22478	16
	17 18	.15458	.18307	.16419	.19645	17200	.21051	.18386	.22528	18
	19	.15489	.18328	.16435	.19668	17407	.21075	.18403	.22554	19
	20	.15505	.18350	.16451	.19691	.17390 .17407 .17423	.21099	.18420	.22579	20
	21	.15520	.18372	.16467	.19713	.17439	.21123	.18437	.22604	21
	22	.15536	.18394	.16483	.19736	.17456	.21147	.18454	.22629	22
	23	.15552	.18416	.16499	.19759	.17472	.21171	.18470	.22655	23
	24	.15567	.18437	.16515	.19782	.17489	.21195	.18487	.22680	24
	25 26	.15583	.18459	.16531	.19805 .19828	.1750 5 .17522	.21220	.18504	.22706	25 26
	27	.15598 .15614	.18503	.16563	.19851	.17538	.21268	.18538	.22756	27
	28	.15630	.18525	.16579	.19874	.17554	.21292	.18555	.22782	28
	29	.15645	.18547	.16595	.19897	.17571	.21316	.18572	.22807	29
	30	.15661	.18569	.16611	.19920	.17587	,21341	.18588	.22833	30
-	31	.15676	.18591	.16627	.19944	.17604	.21365	.18605	.22858	31
	32	.15692	.18613	.16644	.19967	.17620	.21389	.18622	.22884	32
	33 34	.15708	.18635	.16660	.19990	.17637	.21414	.18639	.22909	33 34
	35	.15723	.18679	.16692	.20036	.17670	.21462	.18673	.22960	35
	36	.15755	.18701	16708	.20059	.17686	.21487	.18690	.22986	36
	37	.15770	.18723	.16708 .16724	.20083	.17703	.21511	.18707	,23012	37
	38	.15786	.18745	.16740	.20106	.17719	.21535	.18724	.23037	38
	39	.15802	.18767	.16756	.20129	.17736	.21560	.18741	.23063	39
-	40	.15818	.18790	.16772	.20152	.17752	.21584	.18758	.23089	40
1	41	.15833	.18812	.16788	.20176	.17769	.21609	.18775	.23114	41
	42	.15849	.18834	.16805	.20199	.17786	.21633 .21658	.18792	.23140 .23166	42 43
1	43	.15865	.18878	.16821	.20222	.17802	.21682	.18809	.23192	43
	45	.15896	.18901	.16853	20269	.17835	.21707	.18843	.23217	45
1	46	.15912	.18923	.16869	.20292	.17852	.21731	.18860	.23243	46
-	47	.15928	.18945	.16885	.20316	.17868	.21756	.18877	.23269	47
	48	.15943	.18967	.16902	.20339	.17885	.21781	.18894	.23295	48
1	49 50	.15959	.18990	.16918	.20363	.17902	.21805 .21830	.18911	.23321	49 50
	51	.15991	.19034	.16950	.20410	.17935	.21855	.18945	.23373	51
1	52	.16006	.19057	.16966	.20433	.17952	.21879	.18962	.23399	52
	53	.16022	.19079	.16983	.20457	.17952 .17968	.21904	.18979	.23424	53
	54	.16038	.19102	.16999	.20180	.17985	.21929	.18996	.23450	54
	55 56	.16054	.19124	.17015	.20504	.18001	.21953	.19013	.23476	55
1	57	.16070	.19146	.17031	.20527	.18018	.21978	.19030	,23529	56 57
1	58	.16101	.19191	.17064	.20575	.18051	.22028	.19064	.23555	58
1	59	.16117	.19214	.17080	.20598	.18068	.22053	.19081	.23581	59
-	60	.16133	.19236	.17096	.20622	.18085	.22077	.19098	.23607	60

TABLE XIII.—VERSINES AND EXSECANTS.

	la de la							1	
,	3	6°	3	70	3	8°	3	9°	,
	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	
0	.19098	.23607	.20136	.25214	.21199	.26902	.22285	.28676	0
1 2	.19115	.23633	.20154	.25241	.21217	.26931 .26960	.22304	.28706	1
3	.19150	.23685	.20189	.25296	.21253	.26988	.22340	.28737	2 3
4	.19167	.23711	.20207	.25324	.21271	.27017	.22359	.28797	4
5	.19184	.23738	.20224	.25351	.21289	.27046	.22377	.28828	4 5 6 7
6	.19201	.23764	.20242	.25379	.21307	.27075	.22395	.28858	6
7 8	.19218	.23790 .23816	.20259	.25406 .25434	.21324	.27104 .27133	.22414	.28889	8
9	.19252	.23843	.20294	.25462	.21342	.27162	.22450	.28919	9
10	.19270	.23869	.20312	.25489	.21378	.27191	.22469	28980	10
11	.19287	.23895	.20329	.25517	.21396	.27221	.22487	.29011	11
12	.19304	.23922	.20347	.25545	.21414	.27250	.22506	.29042	12
13	.19321	.23948	.20365	.25572	.21432	.27279	.22524	.29072	13
14 15	.19338 .19356	.23975	.20382	.25600	.21450	.27308	.22542	.29103	14
16	.19373	.24028	.20400	.25628 .25656	.21468	.27337 .27366	.22561	.29133	15 16
17	.19390	.24054	.20435	.25683	.21504	.27396	.22598	.29195	17
18	.19407	.24081	.20453	.25711	.21522	.27425	.22616	.29226	18
19	.19424	.24107	.20470	.25739	.21540	.27454	.22634	.29256	19
20	.19442	.24134	.20488	.25767	.21558	.27483	.22653	.29287	20
21	.19459	.24160	.20506	.25795	.21576	.27513	.22671	.29318	21
22	.19476	.24187	.20523	.25823	.21595	.27542	.22690	.29349	22
23 24	.19493	.24213	.20541	.25851	.21613	.27572	.22708	.29380	23
25	.19528	.24267	.20559	.25879	.21649	.27601 .27630	.22727	.29411	25
26	.19545	.24293	.20594	.25935	.21667	.27660	.22764	.29473	26
27	.19562	.24320	.20612	.25963	.21685	.27689	.22782	.29504	27
28	.19580	.24347	.20629	.25991	.21703	.27719	.22801	.29535	28
29	.19597	.24373	.20647	.26019	.21721	.27748	.22819	.29566	29 30
(350)		The state of the s		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	The state of the s	.27778	The state of the s	.29597	
31	.19632	.24427	.20682	.26075 .26104	.21757	.27807 .27837	.22856	.29628 .29659	31
33	.19666	.24481	20718	.26132	.21794	.27867	.22893	.29690	33
34	.15684	.24508	.20736	.26160	.21812	.27896	.22912	.29721	31
35	.19701	.24534	.20753	.26188	.21830	.27926	.22930	.29752	35
36	.19718	.24561	.20771	.26216	.21848	.27956	.22949	.29784	36
37	.19736 .19753	.24588	.20789	.26245 .26273	.21866	.27985 .28015	.22967	.29815	87 33
39	.19770	.24613	.20824	26301	.21902	.28045	.23004	.29877	39
40	.19788	.24669	.20842	.26330	.21921	.28075	.23023	.29909	40
41	.19805	.24696	.20860	,26358	.21939	.28105	.23041	.29940	41
42	.19822	.24723	.20878	.26387	.21957	.28134	.23060	.29971	4:2
43	.19840	.24750	.20895	.26415	.21975	.28164	.23079	.30003	43
44 45	.19857	.24777	.20913	.26443	.21993	.28194	.23097	.30034	41 45
46	.19892	.24804 .24832	.20949	.26500	.22012	.28254	.23134	.30097	46
47	.19909	.24859	.20967	.26529	.22048	.28284	.23153	30129	47
48	.19927	.24886	.20985	.26557	.22066	.28314	.23172	.30160	48
49	.19944	.24913	.21002	.26586	.22084	.28344	.23190	.30192	49
50	.19962	.24940	.21020	.26615	.22103	.28374	.23209	.30223	50
51	.19979	.24967	.21038	.26643	.22121	.28404	.23228	.30255	51
52 53	.19997	.24995	.21056 .21074	.26672 .26701	.22139	.28434	.23246	.30287	52 53
54	.20032	.25049	.21092	.26729	.22176	.28495	.23283	.30350	54
55	.20049	.25077	.21109	.26758	,22194	.28525	.23302	.30382	55
56	.20066	.25104	.21127	.26787	.22212	.28555	.23321	.30413	56
57	.20084	.25131	.21145	.26815	.22231	.28585	.23339	.30445	57 58
58	.20101	.25159	.21163	.26844	.22249	.28615	.23358	.30477	59
60	.20136	.25214	.21181	.26902	.22285	.28676	23396	.30541	60

Г									39	
	,	4	.0°	4	1°	4	2°	4	3°	,
		Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	
1	0	.23396	.30541	.24529	.32501	.25686	.34563	.26865	.36733	C
1	1	.23414	.30573	.24548	.32535	.25705	.34599	.26884	.36770	1
1	2 3	.23452	.30636	.24586	.32602	.25744	.34669	.26924	.36844	3
1	4	.23470	.30668	.24605	.32636	.25763	.34704	.26944	.36881	4
	5	.23489	.30700	.24625	.32669	.25783	.34740	.26964	.36919	4 5 6 7 8
1	6	.23508	.30732	.24644	.32703	.25822	.34775 .34811	.26984 .27004	.36956	7
1	8	.23545	.30796	.24682	.32770	.25841	.34846	.27024	.37030	8
1	9	.23564	.30829	.24701	.32804	.25861	.34882 .34917	.27043	.37068	9
1	11	.23602	.30893	.24739	.32872	.25900	.34953	.27083	.37143	11
	12	.23620	.30925	.24759	.32905	.25920	.34988	.27103	.37180	12
1	13	.23639	.30957	.24778	.32939	.25939	.35024	.27123	.37218	13
1	14 15	.23658	.30989	.24797	.32973	.25959 .25978	.35060	.27143	.37255	14 15
1	16	.23696	.31054	.24835	.33041	25998	.35131	.27183	.37330	16
1	17	.23714	.31086	.24854	.33075	.26017	.35167	.27203	.37368	17
1	18 19	.23733	.31119	.24874	.33109	.26037	.35203	.27223 .27243	.37406	18
	20	.23771	.31183	.24912	.33177	.26076	.35274	.27263	.37481	20
	21	.23790	.31216	.24931	.33211	.26096	.35310	.27283	.37519	21
	22 23	.23808	.31248	.24950	.33245 .33279	.26115	.35346	.27303	.37556	22
1	24	.23846	.31313	.24970	.33314	.26135 .26154	.35382	.27323	.37594 .37682	23 24
1	95	.23865	.31346	.25008	.33348	.26174	.35454	.27363	.37670	25
	26 27	.23884	.31378	.25027	.33382	.26194	.35490	.27383	.37708	26
	28	.23903	.31411	.25047	.33416	.26213	.35526 .35562	.27403	.37746	27 28
1	29	.23941	.31476	.25085	.33485	.26253	.35598	.27443	.37822	29
1	30	.23959	.31509	.25104	.33519	.26272	.35634	.27463	.37860	30
1	31 32	.23978	.31541	.25124	.33554	.26292	.35670	.27483	.37898	31 32
	33	.24016	.31607	25162	.33622	.26331	.35743	.27523	.37974	33
1	34	.24035	.31640	.25182	.33657	.26351	.35779	.27543	.38012	34
	35 36	.24054	.31672	.25201	.33691 .33726	.26371	.35815	.27563 .27583	.38051	25 36
1	37	.24092	.31738	.25240	.33760	.26410	.35888	.27603	.38127	37
	38	.24111	.31771	.25259	.33795	.26430	.35924	.27623	.38165	33
	39 40	.24130	.31804	.25278	.33830	.26449	.35961	.27643	.38204	39 40
1	41	.24168	.31870	.25317	.33899	.26489	.36034	.27683	.38280	41
-	42	.24187	.31903	.25336	,33934	.26509	.36070	.27703	.38319	42
1	43 44	.24206 .24225	.31936	.25356	.33968	.26528	.36107 .36143	.27723	.38357	43
	45	.24244	.32002	.25394	.34038	.26568	.36180	.27764	.38434	44 45
	46	.24262	.32035	.25414	.34073	.26588	.26217	.27784	.38473	46
1	47	.24281	.32068	.25453	.34108	.26607	.36253	.27804	.38512	47 48
1	49	.24320	.32134	.25172	.34177	.26647	.36327	.27844	.38589	49
1	50	.24339	.32168	.25491	.34212	.26667	.36363	.27864	.38628	50
1	51 52	.24358	.32201	.25511	.34247	.26686	.36400	.27884	.38666	51 52
1	53	.24396	.32267	.25549	.34317	.26726 .26746	.36474	.27925	.38744	53
1	54 55	.24415	.32301	.25569	.34352	.26746	.36511	.27945	.38783	54
1	56	.24453	.32368	.25588	.34387	.26766 .26785	.36548	.27965	.38822	55
-	57	.24172	.32401	.25627	.34458	.26805	.36622	.28005	.38899	57
1	58 59	.24491 .24510	.32434	.25647	.34493 .34528	.26825	.36659 .36696	.28026 .28046	.38938 .38977	58 59
-	60	.24529	.32501	.25686	.34563	.26865	.36733	.28046	.39016	60
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Vers. Exsec. Vers. 0 .28066 .39016 .29289 1 .28066 .39055 .29310 2 .28106 .39095 .29330 3 .28127 .39134 .29351 4 .28147 .39173 .29372 5 .28167 .39251 .29413 7 .28208 .39251 .29413 8 .28228 .39330 .20454 9 .28218 .39330 .20454 9 .28218 .39330 .20457	Exsec. 41421 .41463 .41504 .41545 .41586 .41627 .41669	Vers. .30534 .30555 .30576 .30597 .30618 .30639	Exsec. -43956 -43999 -44042 -44086	Vers. -31800 -31821 -31843	Exsec. -46628 -46674	,
0 .28066 .39016 .29289 1 .28086 .39055 .29310 2 .28106 .39095 .29330 3 .28127 .39134 .29351 4 .28147 .39173 .29372 5 .28167 .39212 .29392 6 .28187 .39251 .29413 7 .28208 .39291 .29433 8 .2828 .39330 .29454	.41421 .41463 .41504 .41545 .41586 .41627	.30534 .30555 .30576 .30597 .30618	.43956 .43999 .44042	.31800 .31821 .31843	.46628 .46674	0
1 .28086 .39055 .29310 2 .28106 .39095 .29330 3 .28127 .39134 .29351 4 .28147 .39173 .29372 5 .29167 .39212 .29392 6 .28187 .39251 .29413 7 .28208 .39291 .29433 8 .28228 .39330 .29454	.41463 .41504 .41545 .41586 .41627	.30555 .30576 .30597 .30618	.43999 .44042	.31821	.46674	0
2 .28106 .39095 .29330 3 .28127 .39134 .29351 4 .28147 .39173 .29372 5 .28167 .39212 .29392 6 .28187 .39251 .29413 7 .28208 .39291 .29433 8 .28228 .39330 .29454	.41504 .41545 .41586 .41627	.30576 .30597 .30618	.44042	.31843		
4 .28147 .39173 .29372 5 .29167 .39212 .29392 6 .28187 .39251 .29413 7 .28208 .39291 .29453 8 .28228 .39330 .29454	.41545 .41586 .41627	.30597				1
4 .28147 .39173 .29372 5 .29167 .39212 .29392 6 .28187 .39251 .29413 7 .28208 .39291 .29453 8 .28228 .39330 .29454	.41586 .41627	.30618	.44086		.46719	2 3
5 .28167 .39212 .29302 6 .28187 .39251 .29413 7 .28208 .39291 .29493 8 .28228 .39330 .29454	.41627			.31864	.46765	3
6 .28187 .39251 .29413 7 .28208 .39291 .29433 8 .28228 .39330 .29454			.44129	.31885	.46811	4
7 .28208 .39291 .29433 8 .28228 .39330 .29454			.44173	.31907	.46857	5
8 .28228 .39330 .29454	.41710	.30660	.44217	.31928	.46903	6 7
	.41752	.30702	.44304	.31971	.46995	8
	.41793	30723	.41347	.31992	.47041	9
10 .28268 .39409 .29495	.41835	.30744	.44391	.32013	.47087	10
11 .28289 .39448 .29516	.41876	.30765	.44435	.32035	.47134	11
12 .28309 .39487 .29510	.41918	.30786	.44479	.32056	.47180	12
13 .28329 .39527 .29557	.41959	.30807	.44523	.32077	.47226	13
14 .28350 .39566 .29578	.42001	.30828	.44567	.32099	.47272	14
15 .28370 .39606 .29599	.42042	.30849	.44610	.32120	.47319	15
16 .28390 .39646 .29619	.42084	.30870	.44654	.32141	.47365	16
17 .28410 .39685 .29640	.42126	.30891	.44698	.32163	.47411	17
18 .28431 .39725 .29661	.42168	.30912	.44742 .44787	.32184	.47458	18
19 .28451 .39764 .29681 20 .28471 .39804 .29702	.42210 .42251	.30933	.44831	.32227	.47504	19 20
			Constant I			1
21 .28492 .39844 .29723	.42293	.30975	.44875	.32248	.47598	21
22 .28512 .39884 .29743 23 .28532 .39924 .29764	.42335	.30996	.44919	.32270	.47644	22 23
23 .28532 .39924 .29764 24 .28553 .39963 .29785	.42377	.31017	.44963	.32312	.47691	24
25 .28573 .40003 .29805	.42461	.31059	.45052	.32334	47784	25
26 .28593 .40043 .29826	.42503	.31080	.45096	.32355	.47831	26
27 .28614 .40083 .29847	.42545	.31101	.45141	.32377	.47878	27 28
28 .28634 .40123 .29868	.42587	.31122	.45185	.32398	.47925	28
29 .28655 .40163 .29888	.42630	.31143	.45229	.32420	.47972	29
30 .28675 .40203 .29909	.42672	.31165	.45274	.32441	.48019	30
31 .28695 .40243 .29930	.42714	.31186	.45319	.32462	.48066	31
32 .28716 .40283 .29951	.42756	.31207	.45363	.32484	.48113	32
33 .28736 .40324 .29971	.42799	.31228	.45408	.32505	.48160	33
34 .28757 .40364 .29992	.42841	.31249	.45452	.32527	.48207	34
35 .28777 .40404 .30013 36 .28797 .40414 .30034	.42885	.31270	.45497	.32570	.48301	35 36
37 .28818 .40485 .30054	.42968	.31312	.45587	.32591	.48349	37
38 .28838 .40525 .30075	.43011	.31334	.45631	.32613	.48396	38
39 .28859 .40565 .30096	.43053	.31355	.45676	.32634	.48443	39
40 .28879 .40606 .30117	.43096	.31376	.45721	.32656	.48491	40
41 .28900 .40646 .30138	.43139	.31397	.45766	.32677	.48538	41
42 .28920 .40687 .30158	.43181	.31418	.45811	.32699	.48586	42
43 .28941 .40727 .30179	.43224	.31439	.45856	.32720	.48633	43
44 .28961 .40768 .30200	.43267	.31461	.45901	.32742	.48681	44
45 .28981 .40808 .30221	.43310	.31482	.45946	.32763	.48728	45
46 .29002 .40849 .30242 47 .29022 .40890 .30263	.43352	.31503	.45992	.32785	.48776	46 47
48 .29043 .40930 .30283	.43438	.31545	.46082	32828	48871	48
49 .29063 .40971 .30304	.43481	.31567	46127	.32849	.48919	49
50 .29084 .41012 .30325	.43524	.31588	.46173	.32871	.48967.	50
51 .29104 .41053 .30346	.43567	.31609	.46218	.32893	.49015	51
52 .29125 .41093 .30367	.43610	.31630	.46263	.32914	.49063	52
53 .29145 .41134 .30388	.43653	.31651	.46309	.32936	.49111	53 54
54 .29166 .41175 .30409 55 .29187 .41216 .30430	.43696	.31673	.46354	.32957	.49109	55
56 .29207 .41257 .30451	.43739	31715	.46445	.33001	.49255	56
57 .29228 .41298 .30471	.43826	.31715 .31736	.46491	.33022	.49303	57
-58 .29248 .41339 .30492	.43869	.31758	.46537	.33044	.49351	58
59 .29269 .41380 .30513	.43912	.31779	.46582	.33065	.49399	59
60 .29289 .41421 .30534	.43956	.31800	.46628	.33087	.49148	60

Vers. Exsec. Vers. Exsec. Vers. Exsec. Vers. Exsec. Vers. Exsec. Vers.						4					
0 .33087 .49448		,	4	8°	4	9°	5	0°	- 5	1°	,
1 .33109 .49496 .34416 .592476 .35746 .55626 .37091 .58959 1 2 .33130 .49544 .34489 .52579 .35768 .55680 .37113 .59016 .2 3 .33152 .49593 .34400 .52579 .35768 .55734 .37136 .59073 .3 4 .33173 .49641 .34482 .52630 .35718 .55789 .37158 .59130 .4 5 .33195 .49680 .34504 .52681 .35833 .55843 .37181 .59188 .5 6 .33217 .49738 .34596 .52732 .35855 .55897 .37294 .59245 .5 7 .33238 .49787 .34548 .52784 .35875 .55951 .37296 .59302 .7 8 .33290 .49885 .34570 .52855 .35900 .59005 .37210 .55360 .7 8 .33292 .49884 .34502 .52886 .35922 .56060 .37272 .55418 .9 10 .33303 .49983 .34614 .52988 .35944 .56114 .37294 .59475 .10 11 .33325 .49981 .34698 .52989 .35907 .56169 .37317 .59533 .10 12 .33347 .50030 .34685 .53041 .35089 .56223 .37340 .59590 .12 13 .33308 .50079 .34680 .53902 .50011 .56278 .37362 .59540 .12 13 .33308 .50079 .34680 .53902 .50011 .56278 .37362 .59540 .12 14 .33390 .50128 .34702 .53144 .36034 .56322 .37385 .59706 .14 15 .33412 .50177 .34724 .53196 .30666 .56322 .37385 .59706 .14 15 .33412 .50177 .34724 .53196 .30666 .56322 .37385 .59706 .14 15 .33413 .50025 .34768 .53299 .30101 .56278 .37362 .59684 .10 17 .33455 .500275 .34768 .53299 .30101 .50677 .34765 .59989 .18 19 .33499 .50373 .34814 .53453 .36108 .56610 .37321 .60054 .20 19 .33520 .50422 .34834 .53455 .36168 .50661 .37521 .60054 .20 20 .33520 .50422 .34834 .53455 .36168 .50661 .37521 .60054 .20 21 .33542 .50471 .34826 .53507 .36190 .56716 .37544 .60112 .21 22 .3364 .50527 .34785 .53509 .30213 .56771 .37567 .60171 .22 23 .33564 .50527 .3489 .53603 .36235 .56861 .37521 .60054 .20 24 .33607 .50619 .3490 .53614 .36039 .56037 .37898 .50090 .19 25 .33520 .50422 .34834 .53455 .36168 .50661 .37521 .60054 .20 25 .33629 .50069 .3495 .53658 .53607 .36990 .50937 .37899 .50029 .23 24 .33607 .50619 .3490 .53663 .36025 .50697 .37699 .50039 .20 25 .33520 .50066 .35077 .54029 .36455 .56861 .37724 .60059 .20 26 .33521 .50718 .3490 .5368 .36684 .57047 .37690 .60462 .27 28 .33694 .50067 .3499 .53809 .36325 .57047 .37690 .60462 .27 28 .33694 .50066 .33025 .53677 .36698 .37799 .50			Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	
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10		7	.33238	.49787	.34548	.52784	.35877	.55951	.37226	.59302	7
10		8	.33260	.49835	.34570	.52835			.37249		8
11				49933				56114	37204		
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16 .34434 .50226 .34746 .53247 .36078 .56442 .37430 .59820 17 18 .33455 .50275 .34768 .53299 .36101 .56407 .37453 .59880 17 19 .33499 .50373 .34812 .53403 .36146 .56606 .37493 .59986 18 20 .33520 .50423 .34834 .53455 .36606 .37493 .59996 19 21 .33542 .50471 .34856 .53507 .36190 .56716 .37544 .60112 21 22 .33554 .50521 .34878 .53659 .36213 .56771 .37567 .60171 22 23 .33550 .50619 .34923 .53663 .36213 .56771 .37567 .60171 22 23 .33560 .50718 .34967 .53768 .36022 .56937 .37635 .60229 23 24 .336071											
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18 33477 50924 34790 5.3851 36123 5.56551 .37476 5.9988 18 19 33499 50373 34812 5.5355 36168 .56666 .37498 5.9996 19 20 33520 50422 34834 5.3557 36168 .56661 .37544 .60112 21 21 33548 50521 .34878 5.3559 36160 .56711 .37547 .60171 21 22 33564 .50521 .34878 .53559 .36213 .56771 .37547 .60171 21 23 .33580 .50570 .34900 .58611 .36235 .56881 .37612 .60287 22 24 .33607 .50699 .34923 .53820 .56909 .37680 .60462 25 25 .33621 .50717 .34980 .53820 .36932 .57047 .37680 .60464 25 28 .33644 .50617 <td></td> <td>17</td> <td>33455</td> <td>50275</td> <td>34768</td> <td>53299</td> <td>.36101</td> <td>56497</td> <td>37453</td> <td></td> <td>17</td>		17	33455	50275	34768	53299	.36101	56497	37453		17
20		18		.50324	.34790		.36123	.56551	.37476		18
21 .33542 .50471 .34856 .53507 .36190 .56716 .37544 .60112 21 22 .33564 .50521 .34878 .53559 .90213 .50771 .37567 .60171 22 23 .33586 .50570 .34900 .53611 .36285 .37589 .60229 23 24 .33607 .50619 .34923 .53683 .38238 .56881 .37612 .60287 24 25 .33629 .50609 .34945 .53715 .36290 .56937 .37635 .60346 25 27 .33673 .50718 .34967 .58708 .36325 .57047 .37680 .60462 27 28 .33694 .50817 .35011 .58872 .36325 .57047 .37680 .60463 29 29 .33716 .50866 .35037 .54029 .36415 .57213 .37749 .60639 30 31 .33760				.50373	.34812	.53403	.36146	.56606	.37498	.59996	19
92 33564 50521 34878 53559 36213 56771 37567 60171 22 23 33586 50570 34900 53611 36235 56826 37589 60229 23 24 33607 50619 34923 53663 36228 56836 37612 60287 24 25 33629 50669 34945 58715 36280 56937 37635 60346 25 26 33671 50718 34967 58768 36025 50992 33768 60404 26 27 33673 50767 34980 53820 36925 57047 37680 60463 29 28 33694 50617 35011 53872 36370 57168 37736 60680 29 30 33788 50916 35057 54029 36415 57138 37794 60639 0 31 33760 50966 35077			.33520	.50422	.34834	.53455	.36168	.56661	.37521	.60054	20
23 ,33586 ,50570 ,34900 ,56611 ,36225 ,56826 ,37589 ,60229 23 24 ,33607 ,50619 ,34932 ,53668 ,36258 ,56831 ,37612 ,60287 24 25 ,33629 ,50669 ,34945 ,58715 ,36280 ,56937 ,37636 ,60404 25 26 ,33673 ,50707 ,34980 ,53820 ,56932 ,57886 ,60404 26 28 ,33694 ,50617 ,35011 ,5872 ,36376 ,57733 ,60821 28 29 ,33716 ,50866 ,35033 ,5394 ,36370 ,57188 ,37726 ,6089 29 30 ,33780 ,50016 ,35077 ,54082 ,36415 ,57369 ,37771 ,60698 30 31 ,33780 ,51015 ,35122 ,54134 ,36492 ,57324 ,37794 ,60756 33 33 ,38255 ,51115 <t< td=""><td>1</td><td></td><td></td><td></td><td>.34856</td><td></td><td></td><td></td><td></td><td></td><td>21</td></t<>	1				.34856						21
24 ,33607 ,50619 ,34923 ,53668 ,36239 ,50609 ,34945 ,53715 ,36230 ,50609 ,34945 ,53715 ,36230 ,56937 ,37635 ,60346 25 26 ,33671 ,50718 ,34967 ,58768 ,36932 ,56937 ,37635 ,60404 26 27 ,33673 ,50717 ,34980 ,58820 ,36835 ,57047 ,37680 ,60463 22 ,33604 ,50817 ,35011 ,58872 ,36335 ,57047 ,37680 ,604621 28 ,33604 ,50817 ,35091 ,38373 ,50966 ,35055 ,53077 ,36392 ,57213 ,37749 ,60639 39 31 ,33760 ,50966 ,35077 ,54029 ,36415 ,57394 ,37794 ,60756 33 ,33783 ,51015 ,35099 ,54184 ,36490 ,57380 ,37817 ,60698 91 32 ,33782 ,51115 ,35166 ,51240 ,36504 ,57491	1	22	.33564	.50521	.34878		.36213				22
25 .33629 .50609 .34945 .53715 .36290 .560987 .37635 .60464 .25 26 .33671 .50718 .34907 .53788 .36302 .56099 .37658 .60404 .25 27 .33673 .50707 .34989 .53820 .36325 .57047 .37880 .60464 27 28 .33674 .50666 .35033 .53924 .36370 .57138 .37703 .60580 29 30 .33738 .50916 .35055 .53977 .86392 .57213 .37749 .60639 30 31 .33760 .50966 .35075 .54029 .36415 .57269 .37771 .60698 31 32 .33782 .51015 .35109 .54082 .36437 .57380 .37817 .60615 32 33 .33895 .51115 .35144 .54147 .3640 .57380 .37817 .60615 32 35	1										23
26 33651 50718 34967 55708 36302 56009 37658 .60404 27 27 33673 50707 34989 .53809 36325 .57047 37703 .60821 28 28 33694 .50817 .35011 .58872 .36370 .57138 .37703 .60821 28 39 .33788 .50916 .35055 .53977 .36302 .57138 .37726 .60580 29 31 .33760 .50966 .35077 .54029 .36415 .57269 .37771 .60639 30 33782 .51015 .35099 .54082 .36437 .57394 .37794 .60756 33 338303 .51055 .35144 .54187 .36482 .57436 .37840 .60874 34 35 .33847 .51165 .35166 .54240 .36504 .57491 .37885 .60933 33 3509312 .51314 .35292	1										
28 33694 50817 35011 55872 36347 57168 37703 .60921 28 29 33716 50866 35033 53924 36370 57158 37726 .6080 29 30 33788 50916 35055 53977 36302 57213 37749 .60639 30 31 .33760 50966 .35077 54029 .36415 .57269 .37771 .60639 30 32 .33782 .51015 .35099 .54082 .36437 .57384 .37794 .60756 33 33 .33803 .51005 .35122 .54134 .3649 .57496 .37817 .60615 33 35 .33847 .51155 .35188 .54292 .36527 .57547 .3785 .60992 .36 37 .33891 .51265 .35210 .5445 .36449 .57603 .37931 .61111 38 39 .33934 <	1	26	.33651	.50718	.34967	.53768	.36302	.56992	.37658	.60404	26
31 .33760 .50966 .35077 .54029 .84415 .57369 .37771 .60698 31 32 .33782 .51015 .35099 .54082 .36437 .57324 .37794 .60756 33 33 .33803 .51065 .35122 .54134 .36400 .57380 .37817 .60615 33 34 .33825 .51115 .35144 .54187 .36548 .57496 .37802 .60932 .35 36 .33860 .51215 .35188 .54292 .36527 .57547 .37885 .60992 .36 37 .33891 .51265 .35210 .514345 .38649 .57603 .37931 .61111 .38 39 .33934 .51304 .35254 .54451 .36594 .57715 .37996 .61029 40 33935 .51415 .35277 .54504 .36617 .57711 .37976 .61229 40 40 .33936					.34989	.53820	.36325	.57047	.37680		27
31 .33760 .50966 .35077 .54029 .84415 .57369 .37771 .60698 31 32 .33782 .51015 .35099 .54082 .36437 .57324 .37794 .60756 33 33 .33803 .51065 .35122 .54134 .36400 .57380 .37817 .60615 33 34 .33825 .51115 .35144 .54187 .36548 .57496 .37802 .60932 .35 36 .33860 .51215 .35188 .54292 .36527 .57547 .37885 .60992 .36 37 .33891 .51265 .35210 .514345 .38649 .57603 .37931 .61111 .38 39 .33934 .51304 .35254 .54451 .36594 .57715 .37996 .61029 40 33935 .51415 .35277 .54504 .36617 .57711 .37976 .61229 40 40 .33936			.33694	.50817	.35011		.36347	.57103	.37703	.60521	28
31 .33760 .50966 .35077 .54029 .84415 .57369 .37771 .60698 31 32 .33782 .51015 .35099 .54082 .36437 .57324 .37794 .60756 33 33 .33803 .51065 .35122 .54134 .36400 .57380 .37817 .60615 33 34 .33825 .51115 .35144 .54187 .36548 .57496 .37802 .60932 .35 36 .33860 .51215 .35188 .54292 .36527 .57547 .37885 .60992 .36 37 .33891 .51265 .35210 .514345 .38649 .57603 .37931 .61111 .38 39 .33934 .51304 .35254 .54451 .36594 .57715 .37996 .61029 40 33935 .51415 .35277 .54504 .36617 .57711 .37976 .61229 40 40 .33936		30	33738	.50916	.35055	.53924	36392	57213	37749		30
32 33788 51015 35099 54082 36437 57394 37794 60756 32 33 33808 51065 35192 54134 36400 57380 37817 60874 34 34 33825 51115 35144 54187 36482 57436 37840 60874 34 35 33891 51165 35168 54392 36527 57547 37882 60992 36 37 33891 51314 35232 54398 36527 57669 37938 61051 37 3932 51314 35232 54398 36572 57669 37938 61111 38 39 33934 51364 35274 54451 36594 57715 37934 61171 38 40 33936 51416 35299 5457 36693 57827 37999 61229 40 41 33978 51466 35299 5457		-									1
33 .33803 .51005 .35122 .54134 .36440 .57380 .37817 .60815 38 34 .33825 .51115 .35144 .54187 .36482 .57436 .37840 .60874 84 35 .33847 .51165 .35166 .54240 .86504 .57431 .37883 .60932 35 36 .33869 .51215 .35186 .54329 .36527 .57630 .37908 .60932 35 37 .33891 .51205 .35210 .54345 .36549 .57669 .37908 .60513 37 38 .33912 .51314 .35294 .54451 .36567 .57669 .37931 .61111 39 40 .33936 .51415 .35277 .54504 .36617 .57711 .37976 .61229 40 41 .33778 .51465 .35291 .54574 .36637 .57827 .37996 .61289 4 41									37794		32
35 33847 51165 35166 51240 38504 57491 37862 60932 35 36 33860 51215 35188 54292 36527 57547 37885 60992 36 37 33891 51265 35210 54345 38649 57603 37908 61051 37 38 33912 51314 35232 54398 36572 57669 37931 61111 39 40 33936 51304 35254 54515 36567 57765 37931 611170 39 40 33936 51461 35277 54504 36617 57715 37954 61170 39 41 33778 51465 35299 54557 36639 57827 37999 61288 42 42 34000 51515 35321 54661 36684 57999 38045 61407 44 43 34022 51565 35343			.33803	.51065	.35122	.54134	.36460	.57380	.37817		33
36 39860 51215 35188 5.5292 36527 57547 37885 .60992 36 37 33891 .51265 35210 .54345 .36549 .57603 .37908 .61051 37831 .61111 38 39 .33934 .51304 .35254 .54451 .36594 .57715 .37954 .61170 39 40 .33936 .51415 .35277 .54504 .36617 .57771 .37976 .61229 40 41 .33078 .51465 .35299 .54557 .36639 .57827 .37999 .61288 41 42 .34000 .51515 .35213 .54663 .36662 .57883 .38022 .61348 42 43 .34022 .51565 .35343 .54663 .36684 .57939 .38045 .61407 43 44 .3405 .51665 .35343 .54663 .36729 .58051 .39001 .61526 .447 </td <td></td> <td></td> <td></td> <td>.51115</td> <td>.35144</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td>				.51115	.35144						
37 33891 51265 35210 51245 3849 57669 37908 61051 37831 383931 51314 35232 54398 36572 57659 37931 61111 3833 39334 51364 35232 54398 36572 57659 37931 611170 3940 40 33936 51445 35277 54504 36617 57711 37976 61229 40 41 33978 51465 35299 54557 36639 57827 37999 61288 41 42 34000 51515 35321 54610 36662 57883 38922 61348 42 43 34022 51565 35343 54663 36684 57999 38045 61407 44 43 34055 51665 35388 54769 36729 58051 38061 61467 44 45 34067 51766 35432 5476 36775 58164											
38 33012 51314 35232 51398 36572 57659 37931 61111 38 39 33034 51304 35254 54451 36594 57715 37954 61117 38 40 33936 51415 35254 55457 36617 57771 37976 61229 40 41 33078 51465 35299 54557 36639 57827 37999 61288 41 42 34000 51515 35343 54663 36662 57883 389022 61348 42 43 34022 51565 35343 54663 36684 57999 38045 61407 43 44 34044 51615 35388 54709 36707 57995 38068 61467 44 45 34065 51665 35388 54709 36729 58018 38113 61586 46 47 34109 51766 35432								.57603			
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41 .33378 .51465 .35299 .54557 .36639 .57827 .37999 .61288 41 42 .34000 .51515 .35343 .54663 .36662 .57883 .38922 .61348 42 43 .34022 .51565 .35343 .54663 .36684 .57999 .38045 .61407 43 44 .34044 .51615 .35385 .54716 .36707 .57995 .38068 .61467 44 45 .34065 .51665 .35388 .54709 .36729 .58108 .38113 .61586 46 47 .34109 .51766 .35432 .54876 .36775 .58108 .38113 .61586 46 47 .34109 .51867 .35476 .54982 .36820 .58277 .38182 .61705 48 49 .34153 .51867 .35476 .54982 .36820 .58277 .38182 .61705 49 50				.51364				.57715	.37954	.61170	
42 34000 51515 35321 54610 36602 57883 38922 61548 42 43 34022 51565 35343 54663 36684 57939 38045 61407 43 44 34044 51615 35365 54716 36707 57995 38068 61467 44 45 34055 51716 35410 54822 36782 58061 38001 61586 46 46 34087 51716 35410 54822 36782 58108 38113 61586 46 47 34109 51766 35432 54876 36775 58164 38136 61646 47 48 34131 51817 35434 54992 36707 58221 38182 61765 49 49 34175 51918 35499 55036 36842 58333 38305 61825 50 51 34197 51996 35543				.51415		.54504	.36617	.57771	.37976	.61229	40
43 34022 51565 35343 54663 36644 57999 38045 61407 43 44 34044 51615 35365 54716 36707 57995 38068 61467 44 45 34065 51665 35388 54709 36729 58051 38091 61526 45 46 34087 51716 35410 54822 36752 58108 38113 61586 47 47 34109 51766 35422 54876 36757 58164 38136 61046 47 48 34131 51817 35454 54929 36797 58221 38159 61705 48 49 34153 51918 35499 55036 36820 58277 38182 61765 49 50 34175 51918 35499 55036 3685 5830 38228 61885 51 52 34219 52019 35565					.35299						
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		42	34000					.57883			42
45 .34065 .51665 .35288 .54769 .36729 .58051 .38091 .61526 45 46 .34087 .51716 .35410 .54822 .36732 .58108 .38113 .61586 44 47 .34109 .51766 .35432 .54876 .30775 .58261 .38136 .61646 47 48 .34131 .51817 .35454 .54929 .36797 .58221 .38130 .61765 49 49 .34133 .51867 .35476 .54982 .36820 .58277 .38182 .61765 49 50 .34175 .51918 .35499 .55036 .36842 .58333 .38205 .61825 50 51 .34197 .51968 .35521 .55089 .36865 .58300 .38228 .61885 51 52 .34214 .52099 .35563 .55166 .36910 .58503 .38274 .62005 53 53			.34044	.51615		.54716	36707				
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	1			.51665	.35388	.54769	.36729				
48 .34181 .51817 .35454 .54929 .36707 .58221 .38159 .61705 48 49 .34153 .51867 .35476 .54982 .36820 .58277 .38182 .61765 49 50 .34175 .51918 .35499 .55036 .36842 .58333 .38305 .61825 50 51 .34197 .51968 .35521 .55089 .36865 .58300 .39228 .61885 51 52 .34219 .52009 .35565 .55143 .36887 .58447 .38251 .61945 52 53 .34214 .52009 .35565 .55196 .36910 .58503 .38274 .62005 53 54 .34262 .52120 .35588 .55250 .36932 .58500 .38296 .62065 54 56 .34306 .52222 .35632 .55373 .36975 .58674 .38319 .62125 56 57				.51716	.35410	.54822	.36752	.58108	.38113	.61586	46
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52 .34219 .52019 .35543 .55143 .36887 .58447 .38951 .61945 .52 53 .34211 .52069 .35565 .55196 .36910 .58503 .38274 .62005 .53 54 .34262 .52120 .35588 .55250 .36932 .58500 .38296 .30065 .54 55 .34294 .52171 .35610 .55303 .36955 .58617 .38319 .62125 .56 56 .34306 .52223 .35632 .55357 .36978 .58674 .38342 .62185 .56 57 .34328 .52273 .35654 .55411 .27000 .58731 .38365 .62246 57 58 .34350 .52323 .35677 .55465 .37023 .58788 .38388 .63306 .58 59 .34372 .52374 .35690 .55518 .37045 .5845 .38411 .62266 59						.55089	.36865	.58390	The second of	The second second	
54 .34262 .52120 .35588 .55250 .36932 .58560 .38296 .62065 54 55 .34294 .52171 .35610 .55303 .36955 .58617 .38319 .62125 .56 56 .34306 .52223 .35632 .55857 .36978 .59674 .33312 .62185 .56 57 .34328 .52273 .35654 .55411 .27000 .58731 .38365 .62246 .57 58 .34350 .52323 .35677 .55465 .37023 .58788 .33388 .63306 .58 59 .34372 .52374 .35699 .55518 .37045 .5845 .38411 .62266 .59			.34219	.52019		.55143	.36887	.58447	.38251	.61945	52
50 .34254 .52171 .35610 .55303 .36955 .58617 .38319 .62125 .56 56 .34306 .52222 .35637 .36978 .58674 .38342 .62185 .56 57 .34328 .52273 .35654 .55411 .27000 .58731 .38365 .62246 .57 58 .34350 .52323 .35677 .55465 .37023 .58788 .38388 .63306 .58 59 .34372 .52374 .35699 .55518 .37045 .5845 .3411 .62266 .59					.35565	.55196		.58503	.38274		
56 .34306 .52222 .35632 .55357 .36978 .58674 .38342 .62185 56 57 .34328 .52273 .35654 .55411 .37000 .58731 .38365 .62246 57 58 .34350 .52323 .35677 .55465 .37023 .58788 .38388 .62306 58 59 .34372 .52374 .35699 .55518 .37045 .5845 .38411 .62366 59		55	34284	.52171		55303	36055				
57 34328 52273 35654 55411 57000 58731 38365 62246 58 58 34350 52323 35677 55465 37023 58788 38388 63306 58 59 34372 52374 35699 55518 37045 58945 38411 62266 59	1	56	.34306	59999		.55357				.62185	56
58 .34350 .52323 .35677 .55465 .37023 .58788 .38388 .62306 58 59 .34372 .52374 .35699 .55518 .37045 .5845 .38411 .62366 59	1			.52273	.35654	.55411	.37000	.58731	.38365	.62246	57
	1		.34350				.37023				58
	1		.34394	.52425	.35721	.55572	37068		38434		

1	535	1			1					
-	,	52°		53°		54°		55°		,
		Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	
	0	.38434	.62427	.39819	.66164	.41221	.70130	42642	.74345	0
	2 3	.38480	. 62548	.39865	.66292	.41269	.70267	.42690	.74490	1 2 3 4 5 6 7 8
	3	.38503	.62609	.39888	.66357	.41292	.70335	.42714	.74562	3
	4 5 6	.38549	.62730	.39935	.66486	.41339	.70472	42762	.74708	5
	6 7	.38571	.62791	.39958	.66550	.41363	.70540 .70609	.42785	.74781 .74854	6
	7 8	.38617	.62913	.40005	.66679	.41410	.70677	.42833	.74927	8
	9	.38640	.62974	.40028	.66744	.41433	.70746 .70815	.42857	.75000 .75073	9
	11	.38686	.63096	.40074	.66873	.41481	.70884	.42905	.75146	11
	12	.38709	.63157	.40098	.66938	.41504	.70953	.42929	.75219	12
	13 14	.38732	.63218	.40121	.67003	.41528	.71022 .71091	.42953	.75293 .75366	13 14
	15	.38778	.63341	.40168	.67133	.41575	.71160	.43000	.75440	15
4	16 17	.38801	.63402	.40191	.67199	.41599	.71229	.43024	.75513	16
i	18	.38847	.63525	.40214	.67264 .67329	.41622	.71298 .71368	.43048	.75587	17 18
	19	.38870	.63587	.40261	.67394	.41670	.71437	.43096	.75734	19
	20 21	.38893	.63648	.40284	.67460	.41693	.71506	.43120	.75808	20
	22	.38916	.63710	.40307	.67525 .67591	.41717	.71576 .71646	.43144	.75882 .75956	21 22
	23	.38962	.63834	.40354	.67656	.41764	.71715	.43192	.76031	23
	24 25	.38985	.63895	.40378	.67722 .67788	.41788	.71785 .71855	.43216	.76105	24 25
	26	.39032	.64019	.40424	.67853	.41835	.71925	.43264	.76253	26
	27 28	.39055	.64081	.40448	.67919 .67985	.41859	.71995 .72065	.43287	.76328	27 28
	29	.39101	.64206	.40471	.68051	.41906	.72135	.43335	.76477	29
	30	.39124	.64268	.40518	.68117	.41930	.72205	.43359	.76552	30
	31 32	.39147	.64330	.40541	.68183	.41953	.72275	.43383	.76626 .76701	31 32
1	33	.39193	.64455	.40588	.68316	.42001	.72416	.43431	.76776	33
1	34 35	.39216	.64518	.40611	.68382	.42024	.72487	.43455	.76851	34
	36	.39239	.64580	.40635	.68449	.42048	.72557 .72628	.43479	.76926 .77001	35 36
1	37	.39286	.64705	.40682	.68582	.42096	.72698	.43527	.77077	37
-	38	.39309	.64768	.40705	.68648	.42119	72769	.43551	.77152 .77227	38 39
	40	.39355	.64894	.40752	68782	.42167	.72840 .72911	.43599	.77303	40
	41	.39378	.64957	.40775	.68848	.42191	.72982	.43623	.77378	41
1	42 43	.39401	.65020 .65083	.40799	.68915	.42214	.73053 .73124	.43647	.77454 .77530	42 43
	44	.39447	.65146	.40846	.69049	.42262	.73195	.43695	.77606	44
-	45 46	.39471	.65209	.40869	.69116	.42285	.73267	.43720 .43744	.77681 .77757	45 46
	47	.39517	.65336	.40916	.69250	.42333	.73409	.43768	.77833	47
	48	.39540	.65399	.40939 .40963	.69318 .69385	.42357	.73481 .73552	.43792 .43816	.77910	48 49
-	50	.39586	.65526	.40986	.69452	.42404	.73624	.43840	.77986 .78062	50
-	51	.39610	.65589	.41010	.69520	.42428	.73696	.43864	.78138	51
-	52 53	.39633 .39656	.65653 .65717	.41033	.69587 .69655	.42452 .42476	.73768	.43888	.78215 .78291	52 53
	54	.39679	.65780	.41080	.69723 .69790	.42499	.73911	.43936	.78368	54
	55 56	.39702 .39726	.65844 .65908	.41104	.69790 .69858	.42523	73983	.43960 .43984	.78445 .78521	55 56
	57	.39749	.65972	.41151	.69926	.42571	.74128	.44008	.78598	57
	-58 59	.39772	.66036 .66100	.41174	.69994 .70062	.42595	.74200	.44032	.78675	58 59
	60	.39819	.66164	.41198	.70130	.42619	.74272	.44081	.78752 .78829	60

	1 7 %		11		1				
	5	6°	5	7°	5	8°	5	9°	,
	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	
1		.78829	.45536	.83608	.47008	.88708	.48496	.94160	0
	.44105	.78906	.45560	.83690	.47033	.88796	.48521	.94254	1
97.00	.44129	.78984	.45585	.83773 .83855	.47057	.88884	.48546	.94349	3
1 3	.44177	79138	.45634	.83938	.47107	.89060	,48596	.94537	4
	.44201	.79216	.45658	.84020	.47131	.89148	.48621	.94632	4 5 6 7 8
(.44225	.79293	.45683	.84103	.47156	.89237	.48646	.94726	6
	44250	.79371	.45707	.84186 .84269	.47181	.89325 .89414	.48671	.94821	7
8	44295	.79449 .79527	.45756	.84352	.47230	.89503	.48721	.94916 .95011	9
10		.79604	.45780	.84435	.47255	.89591	.48746	.95106	10
11		.79682	.45805	.84518	.47280	.89680	.48771	.95201	11
1:	.44370	.79761	.45829	.84601	.47304	.89769	.48796	.95296	12
13		.79839	.45854	.84685	.47329	.89858	.48821	.95392	13
14		. 79917	.45878	.84768	.47354	.89948	.48846	.95487	14 15
13		.79995 .80074	.45903	.84852 .84935	.47379	.90126	.48871	.95583 .95678	16
17		.80152	.45951	.85019	.47428	.90216	.48921	.95774	17
18	.44516	.80231	.45976	.85103	.47453	.90305	.48946	.95870	18
19		.80309	.46000	.85187	.47478	.90395	.48971	.95966	19
20		.80388	.46025	.85271	.47502	.90485	.48996	.96062	20
21		.80467 .80546	.46049	.85355 .85439	.47527	.90575	.49021	.96158	21
2		.80625	.46098	.85523	.47552	.90665	.49046	.96255	22 23
2	.44661	.80704	.46123	.85608	.47601	.90845	.49096	.96448	24
2	.44685	.80783	.46147	.85692	.47601 .47626	.90935	.49121	.96544	25
26	.44709 .44734	.80862	.46172	.85777	.47651	.91026	.49146	.96641	26
20	.44758	.80942 .81021	.46196 .46221	.85861 .85946	.47676 .47701	.91116	.49171	.96738	27 28
20	.44782	.81101	.46246	.86031	47725	.91297	.49221	.96932	29
30		.81180	.46270	.86116	.47750	.91388	.49246	.97029	30
31		.81260	.46295	.86201	.47775	.91479	.49271	.97127	31
35		.81340	.46319	.86286	.47800	.91570	.49296	.97224	33
33		.81419	.46344	.86371 .86457	.47825	.91661 .91752	.49321	.97322	33
3.5		.81579	.46393	.86542	.47874	.91844	.49372	.97517	35
36	.44952	.81659	.46417	.86627	.47899	.91935	.49397	.97615	36
37	.44976	.81740	.46142	.86713	.47924	.92027	.49422	.97713	37
38		.81820 .81900	.46466	.86799 .86885	.47949	.92118	.49447	.97811 .97910	38
40		.81981	.46516	.86990	.47998	,92302	.49497	.98008	40
41	The second second	.82061	.46540	.87056	.48023	.92394	.49522	.98107	41
43	.45098	.82142	.46565	.87142	.48048	.92486	.49547	.98205	42
43		.82222	.46589	.87229	.48073	.92578	.49572	.98304	43
44		.82303 .82384	.46614	.87315 .87401	.48098	.92670	.49597	.98403	44 45
46		.82465	.46663	.87488	.48123	.92702	.49623	.98502	46
47	.45219	.82546	.46688	.87574	.48172	92947	.49673	.98700	47
48		.82627	.46712	.87661	.48197	.93040	.49698	.98799	48
49		.82709 .82790	.46737	.87748 .87834	.48222	.93133	.49723	.98899	49 50
51	.45317	.82871	.46786	.87921	.48272	.93319	.49773	.99098	51
52	.45341	.82953	.46811	.88008	.48207	.93412	.49799	.99198	52
53	.45365	.83034	.46836	.88095	.48322	.93505	.49824	.99298	53
54		.83116	.46860	.88183	.48347	.93598	.49849	.99398	54
56	.45414	.83280	.46885	.88270 .88357	.48372	.93692	.49874	.99498	55 56
57	.45463	.83362	.46934	.88445	.48421	.93879	.49924	.99698	57
58	.45487	.83444	.46959	.88532	.48446	.93973	.49950	.99799	58
59		.83526	.46983	.88620	.48471	.94066	.49975	.99899	59 60
00	. 40000	.00000	.41000	.88708	.48496	.94160	.50000	1.00000	00

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	1,	-	80°	6	81°	(32°	(33°	
		Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	
	0 1	.50000	1.00000	.51519	1.06267	.53053	1.13005	.54601	1.20269	0
	2	.50050	1.00202	.51570	1.06375	.53079	1.13122	.54627	1.20395	1 2
	3	.50076	1.00303	.51595	1.06592	.53130	1.13356	.54679	1.20647	3
	5	.50101	1.00404	.51621	1.06701	.53156	1.13473	.54705	1.20773	4
	6	.50126	1.00505	.51646	1.06809	.53181	1.13590	.54731	1.20900	5
	7	.50176	1.00708	.51697	1.07027	.53233	1.13825	.54757	1.21026 1.21153	6
	8	.50202	1.00810	.51723	1.07027 1.07137	.53258	1.13942	.54808	1.21280	8
	9	.50227	1.00912	.51748	1.07246	.53284	1.14060	.54834	1.21407	9
	11		1.01014	.51774	1.07356	.53310	1.14178	.54860	1.21535	10
	12	.50277	1.01116	.51799	1.07465	.53336	1.14296	.54886	1.21662 1.21790	11 12
	13	.50328	1.01320	.51850	1.07685	.53387	1.14533	.54938	1.21918	13
	14	.50353	1.01422	.51876	1.07795	.53413	1.14651	.54964	1.22045	14
	15 16	.50378	1.01525 1.01628	.51901	1.07905 1.08015	.53439	1.14770	.54990	1.22174 1.22302	15
	17	.50429	1.01730	.51952	1.08013	.53490	1.14889	.55042	1.22430	16
	18	.50454	1.01833	.51978	1.08236	.53516	1.15127	.55068	1.22559	18
	19 20	.50479	1.01936	.52003	1.08347	.53542	1.15246	.55094	1.22688	19
		.50505	1.02039	.52029	1.08458	.53567	1.15366	.55120	1.22817	20
	21 22	.50530	1.02143	.52054 .52080	1.08569 1.08680	.53593	1.15485 1.15605	.55146	1.22946 1.23075	21 22
	23	.50581	1.02349	.52105	1.08791	.53645	1.15725	.55172	1.23205	23
	24	.50606	1.02453	.52131	1.08903	.53670	1.15845	.55224	1.23334	24
	25	.50631	1.02557	.52156	1.09014	.53696	1.15965	.55250	1.23464	25
	26 27	.50656	1.02661	.52182	1.09126 1.09238	.53722	1.16085 1.16206	.55276	1.23594 1.23724	26 27
	28	.50707	1.02869	.52233	1.09350	.53774	1.16326	.55328	1.23855	28
3	29	.50732	1.02973	.52259	1.09462	.53774	1.16447	.55354	1.23985	29
ì	30	.50758	1.03077	.52284	1.09574	.53825	1.16568	.55380	1.24116	30
1	31	.50783	1.03182	.52310 .52335	1.09686	.53851	1.16689 1.16810	.55406	1.24247 1.24378	31 32
	33	.50834	1.03391	.52361	1.09911	.53903	1.16932	.55458	1.24509	33
	34	.50859	1.03496	.52386	1.10024	.53928	1.17053	.55484	1.24640	34
	35	.50884	1.03601	.52412	1.10137	.53954	1.17175	.55510	1.24772	35
	37	.50935	1.03706	.52438	1.10250 1.10363	.53980 .54006	1.17297	.55536	1.24903	36 37
1	38	.50960	1.03916	.52489	1.10477	.54032	1.17541	.55589	1 25167	38
1	39	.50986	1.04022	.52514	1.10590	.54058	1.17663	.55615	1.25300	39
	40	.51011	1.04128	.52540	1.10704	.54083	1.17786	.55641	1.25432	10
	41 42	.51036	1.04233	.52566	1.10817 1.10931	.54109 .54135	1.17909	.55667	1.25565 1.25697	41 42
1	43	.51087	1.04445	.52617	1.11045	.54161	1.18051	.55719	1.25830	43
-	44	.51113	1.04551	.52642	1.11159	.54187	1.18277	.55745	1.25963	44
1	45	.51138	1.04658	.52668	1.11274	.54213	1.18401	.55771	1.26097	45
1	46 47	.51163	1.04764	.52694	1.11388	.54238 .54264	1.18524	.55797	1,26230 1,26364	46 47
1	48	.51214	1.04977	.52745	1.11617	.54290	1.18772	.55849	1.26498	48
1	49	.51239	1.05084	.52771	1.11732	.54316	1.18895	.55876	1.26632	49
1	50	.51265	1.05191	.52796	1.11847	.54342	1.19019	.55902	1.26766	50
-	51 52	.51290	1.05298	.52822	1.11963	.54368	1.19144	.55928 .55954	1.26900 1.27035	51 52
1	53	.51341	1.05512	.52873	1.12193	.54420	1.19393	.55980	1.27169	53
1	54	.51366	1.05619	.52899	1.12309	.54446	1.19517	.56006	1.27304	54
1	55 56	.51392	1.05727	.52924	1.12425	.54471	1.19642	.56032	1.27439 1.27574	55 56
1	57	.51443	1.05835	.52950	1.12540 1.12657	.54497	1.19767	.56084	1.27710	57
1	58	.51468	1.06050	.53001	1.12773	.54549	1.20018	.56111	1.27845	58
1	59 60	.51494	1.06158	.53027	1.12889	.54575	1.20143	.56137	1.27981 1.28117	59 60
1	001	.51519	1.06267	.53053	1.13005	.54601	1.20269	.56163	1.00111	W

	6	40	6	55°	6	66°	6	7°	
'	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	
0	.56163	1.28117	.57738	1.36620	.59326	1.45859	.60927	1.55930	-
1	.56189	1.28253	.57765	1.36768	.59353	1.46020	.60954	1.56106	1
2	.56215	1.28390	.57791	1.36916	.59379	1.46181	.60980	1.56282	1
3	.56241	1.28526	.57817	1.37064	.59406	1.46342	.61007	1.56458	1
4	.56267	1.28663	.57844	1.37212	.59433	1.46504	.61034	1.56634	1
5	.56294	1.28800	.57870	1.37361	.59459	1.46665	.61061	1.56811	
6	.56320	1.28937	.57896	1.37509	.59486	1.46827	.61088	1.56988	1
7	.56346	1.29074	.57923	1,37658	.59512	1.46989	.61114	1.57165	1
8	.56372	1.29211	.57949	1.37808	.59539	1.47152	.61141	1.57342	1
9	.56398	1.29349	.57976	1.37957	.59566	1.47314	.61168	1.57520	1
10	.56425	1.29487	.58002	1.38107	.59592	1.47477	.61195	1.57698	1
	Survivor in	No. of Concession, Name of Street, or other party of the Concession, Name of Street, or other pa		-	The same of the sa			1.57876	
11	.56451	1.29625	.58028 .58055	1.38256	.59619	1.47640	.61222	1.57876	1
13	.56503	1.29763	.58055	1.38406	.59645	1.47804	.61248	1.58233	
14	.56529	1.30040	.58108	1.38556	.59699	1.48131	.61302	1.58412	1
15	.56555	1.30179	.58134	1.38707	.59699	1.48131	.61329	1.58591	1
16	.56582	1.30318	.58160	1.38857	.59752	1.48295	.61356	1.58771	1
17	.56608	1.30318	.58187	1.39008	.59779	1.48459	.61383	1.58950	
18	.56634	1.30596	.58213	1.39311	.59805	1.48789	.61409	1.59130	1
19	.56660	1.30735	.58240	1.39462	.59832	1.48954	.61436	1.59311	1
20	.56687	1.30875	.58266	1.39614	.59859	1.49119	.61463	1.59491	1
- 1	STATES IN	The same of the same of	and the same of	The State of the S	and the same of	The same of the sa		1	
21	.56713	1.31015	.58293	1.39766	.59885	1.49284	.61490	1.59672	1
22 23	.56739	1.31155	.58319	1.39918	.59912	1.49450	.61517	1.59853	
23	.56765	1.31295	.58345	1.40070	.59938	1.49616	61544	1.60035	
24 25	.56791	1.31436	.58372	1.40222	.59965	1.49782	61570	1.60217	
26	.56818	1.31576	.58398	1.40375	.59992	1.49948	.61597	1.60599	
20 27	.56870	1.31717	.58425	1,40528	.60018	1.50115	.61651	1.60763	
28	.56896	1.31858	.58478	1.40681	.60045	1.50282	.61678	1.60763	
29	.56923	1.32140	58504	1.40988	.60098	1.50449	.61705	1.61129	
30	.56949	1.32282	.58531	1.41142	.60125	1.50784	.61732	1.61313	1
30	CALLED ST.	Trends II							
31 32	.56975	1.32424	.58557	1.41296	.60152	1.50952	.61759	1.61496	1
33	.57028	1.32708	.58610	1.41450 1.41605	.60178	1.51120	.61785	1.61864	
34	.57054	1.32708	.58637	1.41760	.60232	1.51289	.61839	1.62049	1
35	.57080	1.32993	.58663	1.41700	.60259	1.51626	.61866	1.62234	1
36	.57106	1.33135	.58690	1.42070	.60285	1.51020	.61893	1.62419	
37	.57133	1.33278	.58716	1.42225	.60312	1.51965	.61920	1.62604	1
38	.57159	1.33422	.58743	1.42380	.60339	1.52134	.61947	1.62790	-
39	.57185	1.33565	.58769	1.42536	.60365	1.52304	.61974	1.62976	1
40	.57212	1.33708	.58796	1.42692	60392	1.52474	.62001	1.63162	
41	.57238	1.33852	.58822	1.42848	.60419	1.52645	.62027	1.63348	1
42	.57264	1.33996	.58849	1.42040	.60419	1.52815	.62054	1.63535	
43	.57291	1.34140	.58875	1.43162	.60472	1.52986	.62081	1.63722	1
44	.57317	1.34284	.58902	1.43318	.60499	1.53157	.62108	1.63909	
45	.57343	1.34429	.58928	1.43476	.60526	1.53329	.62135	1.64097	
46	.57369	1.34573	.58955	1.43633	.60552	1 53500	.62162	1.64285	
47	.57396	1.34718	.58981	1.43790	.60579	1.53500 1.53672	.62189	1.64473	1
48	.57422	1.34863	.59008	1.43730	.60606	1.53845	.62216	1.64662	1
49	.57448	1.35009	.59034	1.44106	.60633	1.54017	.62243	1.64851	-
50	.57475	1.35154	.59061	1.41264	.60659	1.54190	.62270	1.65040	1
51	,57501	1.35300	.59087	1.44423			.62297	1.65229	1
52	.57527	1.35446	.59087	1.44423	.60686	1.54363 1.54536	62324	1.65229	1
53	.57554	1.35592	.59140	1.44582	.60740	1.54709	62351	1.65609	1
54	.57580	1.35738	.59140	1.44741	.60766	1.54883	.62378	1.65799	
55	.57606	1.35885	.59194	1.45059	60793		.62405	1.65989	1
56	.57633	1.36031	.59220	1.45039	.60820	1.55057	.62431	1.66180	1
57	.57659	1.36178	.59247	1.45378	.60820		.62458	1.66371	
58	.57685	1.36325	.59247	1.45539	.60847	1.55405 1.55580	.62485	1.66563	
59	.57712	1.36473	.59300	1.45699	.60900	1.55755	.62512	1.66755	1
60	.57738	1.36620	.59326	1.45859	60927	1.55930	.62539	1.66947	1

Vers. Exsec. Vers. Exsec. Vers. Exsec. Vers.	
0 .62539 1.66947 .64163 1.79043 .65798 1.92380 6744 1 1.62566 1.67139 .64190 1.79254 .65825 1.92614 .6742 2 .62503 1.67332 .64248 1.79466 .65853 1.92849 .6744 3 .62620 1.67525 .64245 1.73079 .65890 1.9083 .6755 4 .62647 1.67718 .64272 1.79891 .65997 1.93318 .6755 5 .62674 1.67911 .64299 1.80104 .65935 1.93554 .6766 6 .62701 1.68105 .64326 1.80318 .65969 1.93554 .6767 7 .62728 1.68499 .64331 1.80541 .65989 1.94203 .6766 8 .62755 1.68494 .64381 1.80746 .66017 1.94203 .6766 8 .62755 1.68689 .64408 1.80746 .66017 1.94203 <th></th>	
1 1 62566 1.67139 64190 1.79254 65825 1.92614 6742 2 62593 1.67332 64218 1.79466 65853 1.92849 6744 3 62620 1.67325 64245 1.79079 65880 1.93083 6752 4 62647 1.67718 64272 1.79991 65907 1.93318 6755 5 62674 1.67911 64299 1.80104 65993 1.93534 6756 6 62701 1.68105 .64326 1.80318 65962 1.93790 6766 7 62728 1.68299 .64333 1.80531 .65980 1.93790 6766 8 62755 1.88494 .64381 1.80746 .66017 1.94263 .6766 9 62782 1.68893 .644381 1.80960 .66044 1.94500 .6766 10 62899 1.68884 .64435 1.81175 .66017 1.94277 .6771 11 62836 1.69079 .64462 1.81390 .66099	2 9 07155
2	
4 62847 1.67718 64272 1.79991 65907 1.93318 6725 5 6.2674 1.67911 64299 1.80104 65935 1.93554 6726 6 62701 1.88105 .64326 1.80318 65962 1.93790 6766 7 .62728 1.68299 .64353 1.80531 .65989 1.94206 .6766 8 .62755 1.68494 .64881 1.80746 .66017 1.94500 .6769 9 .62782 1.68689 .64408 1.80960 .66044 1.94500 .6769 10 .62809 1.68884 .64435 1.80960 .66071 1.94737 .6771 11 .628363 1.60275 .64489 1.81605 .66126 1.95213 .6777 12 .62863 1.60275 .64489 1.81605 .66126 1.95213 .6777 13 .628963 1.69271 .64517 1.81821 .66154 1.95452	8 2.07675
5 62674 1.67911 64299 1.80104 65935 1.93554 6776 6 62701 1.68105 64326 1.80318 65962 1.93790 6766 7 62728 1.68299 64333 1.80521 65089 1.94026 6766 8 62752 1.68889 64408 1.80960 66017 1.94203 5766 10 62809 1.68884 64408 1.80960 66041 1.9420 6766 11 68286 1.69079 64462 1.81375 66071 1.94737 6777 12 62863 1.69275 64489 1.81390 66099 1.94975 6774 13 62890 1.69471 .46517 1.81821 66154 1.9513 6777 13 628963 1.69647 .46457 1.88254 .66206 1.95213 6777 13 62917 1.70664 .45571 1.88254 .66236 1.95313 6777	
6 62701 1.68105 .64326 1.80318 6.5962 1.93790 6766 7 62728 1.68299 .64353 1.80531 .65080 1.94026 .6766 8 62755 1.68494 .64381 1.80746 .66017 1.94263 .6766 9 .62782 1.68689 .64408 1.80960 .66044 1.94500 .6764 10 .62899 1.68884 .64435 1.81175 .66071 1.94377 .6777 11 .68286 1.69079 .64462 1.81390 .66099 1.94975 .6774 12 .62863 1.69275 .64480 1.81605 .66126 1.95213 .6771 14 .62917 1.09667 .64451 1.81605 .66126 1.95213 .6778 15 .62914 1.96867 .64544 1.82037 .66181 1.95691 .6783 16 .62917 1.70061 .64598 1.82254 .66236 1.96171<	$\begin{bmatrix} 3 & 2.08197 \\ 1 & 2.08459 \end{bmatrix}$
8 62755 1.68494 64281 1.80746 66017 1.94263 5706 9 62782 1.68689 64408 1.80900 66044 1.94500 6770 1.062809 1.68884 6.4435 1.81175 66071 1.94737 6777 11 62896 1.69670 64462 1.81390 66099 1.94975 6774 12 62863 1.69275 64489 1.81605 66126 1.95213 6774 13 62890 1.69471 6.4517 1.81821 66154 1.95452 6786 14 62917 1.09667 64544 1.82027 66181 1.95601 6784 15 62944 1.69864 64571 1.82254 66208 1.95031 6785 15 62944 1.69864 64571 1.82254 66208 1.95031 6785 16 62971 1.70661 64598 1.82471 66236 1.95031 6785 17 62995 1.70253 64625 1.82685 66203 1.96171 6788 18 63025 1.70455 64625 1.82688 66203 1.96171 6788 18 63025 1.70455 64625 1.82906 66230 1.9652 6702 19 63052 1.70653 64680 1.83124 66318 1.96893 6706 20 63079 1.70851 64070 1.83124 66318 1.96893 6706 22 63133 1.71249 64761 1.83780 66400 1.97619 6804 22 63183 1.71249 64761 1.83780 66400 1.97619 6804 22 63133 1.71249 64761 1.83780 66400 1.97619 6804 22 6325 1.71487 64816 1.84129 66425 1.98349 6812 25 63215 1.71847 64896 1.84890 66427 1.97862 6807 27 63269 1.72447 64898 1.84890 66337 1.98849 6818 22 63326 1.72447 64898 1.84890 66337 1.98849 6818 22 63326 1.72447 64898 1.84890 66337 1.9888 6818 22 63323 1.72449 64952 1.85303 66564 1.99083 6829 1.90339 1.90483	8 2.08721
9	6 2.08983
10 62809 1.68884 .64435 1.81175 .66071 1.94737 .6771 11 62863 1.69079 .64462 1.81390 .66099 1.94975 .6771 12 62863 1.69275 .64489 1.81605 .66126 1.95213 .6777 13 62890 1.69471 .64517 1.81821 .66154 1.95452 .6780 14 62917 1.99667 .44544 1.82037 .66181 1.95691 .6781 15 62944 1.99684 .44571 1.82254 .66208 1.95313 .6785 16 62971 1.70661 .64598 1.82471 .66236 1.96171 .6781 17 62998 1.70455 .64653 1.82906 .66230 1.96171 .6791 19 63052 1.70653 .64680 1.83124 .66318 1.97937 .6792 21 63106 1.71050 .64734 1.83561 .66357 1.97377 <td>$\begin{bmatrix} 3 & 2.09246 \\ 1 & 2.09510 \end{bmatrix}$</td>	$\begin{bmatrix} 3 & 2.09246 \\ 1 & 2.09510 \end{bmatrix}$
12 62863 1.69275 .64489 1.81605 .66126 1.95213 .6778 13 .62890 1.69471 .64517 1.81821 .66154 1.95452 .6784 14 .62917 1.90667 .64544 1.82037 .66181 1.95691 .6782 15 .62944 1.99864 .64571 1.82254 .66208 1.95931 .6782 16 .62971 1.70051 .64598 1.82471 .66236 1.96171 .6788 17 .62998 1.70255 .64653 1.82906 .66290 1.96652 .6793 18 .63052 1.70455 .64653 1.82906 .66290 1.96652 .6792 19 .63052 1.70533 .64880 1.83124 .66318 1.99893 .6790 20 .63079 1.70861 .64707 1.83361 .66345 1.97377 .6802 22 .63183 1.71249 .64761 1.83760 .66400 1	
13 63890 1.69471 64517 1.81821 66154 1.95452 6782 14 62917 1.69667 64544 1.82037 66181 1.95691 6782 15 62944 1.69864 64571 1.82254 66208 1.95031 6785 16 62971 1.70061 64598 1.82471 66236 1.96171 .6785 17 62998 1.70258 64625 1.82471 ,66236 1.96171 .6793 18 63025 1.70455 64653 1.82906 .66290 1.96652 .6793 19 63052 1.70653 .64680 1.83124 .66318 1.98893 .6792 20 63079 1.70851 .64707 1.83342 .66318 1.97377 .6802 21 .63106 1.71249 .64761 1.83780 .66400 1.97619 .6804 22 .63133 1.71249 .64761 1.83999 .66427 1.97802	
14 62917 1.96667 64544 1.82027 66181 1.95691 6785 15 62944 1.69864 64571 1.82254 66208 1.95031 6785 16 62971 1.70061 64598 1.82471 66236 1.96171 6785 17 62998 1.70238 64625 1.82968 66203 1.96171 6785 18 63025 1.70555 64653 1.82996 66230 1.9652 6702 19 63052 1.70533 64680 1.83124 66318 1.96893 6706 20 63079 1.70851 64707 1.83342 66345 1.97135 6798 21 63106 1.71050 64734 1.83561 66353 1.9737 6802 22 63133 1.71249 64761 1.83780 66400 1.97619 6804 23 63161 1.71449 64761 1.83780 66400 1.97619 6804 </td <td></td>	
16 62971 1.70061 .64598 1.82471 .66236 1.96171 .6781 17 .62998 1.70258 .64625 1.82088 .60203 1.96411 .6791 18 .63025 1.70455 .64653 1.82906 .66290 1.96652 .6792 19 .63052 1.70653 .64680 1.83124 .66318 1.96893 .6792 20 .63079 1.70851 .64707 1.83342 .66345 1.97135 .6799 21 .63106 1.71050 .64734 1.83561 .66373 1.97377 .6802 22 .63163 1.71449 .64761 1.83780 .66400 1.97619 .6807 24 .63188 1.71647 .64816 1.84129 .66427 1.97802 .6807 25 .63215 1.71847 .64846 1.84439 .66482 1.98849 .6813 26 .63242 1.72947 .64896 1.84890 .66377 1	9 2.10834 1
17 62998 1.70258 64625 1.83688 66203 1.94411 6791 18 63025 1.70455 64653 1.82906 66290 1.96652 6793 19 63052 1.70533 64680 1.8124 66318 1.96893 6.706 20 63079 1.70861 64707 1.83342 66345 1.97135 6798 21 63106 1.71050 64734 1.83561 66373 1.97377 6802 22 63133 1.71249 64761 1.83780 66400 1.97619 6804 23 63161 1.71449 64761 1.83999 66427 1.97802 6807 24 63188 1.71647 64816 1.84219 66427 1.97803 6804 25 63215 1.71847 64846 1.84439 66482 1.98349 6813 26 63242 1.72047 64870 1.84659 66510 1.9554 6815 <	
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21 .63106 1.71050 .64734 1.83561 .66373 1.97377 .6802 22 .63133 1.71249 .64761 1.83780 .66400 1.97619 .6804 23 .63161 1.71448 .64789 1.83999 .66427 1.97862 .6807 24 .63188 1.71647 .64816 1.84219 .66455 1.98106 .6810 25 .63215 1.71847 .64843 1.84439 .66482 1.98849 .6813 26 .63242 1.72947 .64870 1.84659 .66510 1.95594 .6815 27 .63269 1.72447 .64898 1.84890 .66377 1.98838 .6818 28 .63326 1.72448 .64925 1.55102 .66564 1.90083 .6827 29 .63323 1.72649 .64952 1.83323 .66592 1.9329 .6329 1.9329 .6329 1.9329 .6329 1.9329 .6329 .63296 1.9329 .6329 .6328 1.9329 .6329 1.9329 .6329 1.9329 .6329 .63296 1.9329 .6329 .6328 .63296 1.9329 .6329 .6328 .63296	
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24 63188 1.71647 64816 1.84219 66455 1.98106 6810 25 63215 1.71847 64843 1.84439 66482 1.98349 6813 26 63242 1.72047 64870 1.84659 66510 1.98594 6813 27 63369 1.72247 64898 1.84890 66537 1.98838 6818 28 63296 1.72448 64925 1.85102 66564 1.90083 6824 29 63323 1.72649 64952 1.83323 66592 1.90329 6824	2.12979 2
25 63215 1.71847 64843 1.84490 66482 1.98349 6813 26 63242 1.72047 64870 1.84659 66510 1.98594 6815 27 63269 1.72247 64898 1.84880 66537 1.98598 6818 28 63296 1.72448 64925 1.85102 66564 1.90083 6821 29 63323 1.72649 64952 1.85323 66592 1.99329 6824	
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30 .63350 1.72850 .64979 1.85545 .66619 1.99574 .6827	2 2.14881 2
	AND DESCRIPTION OF THE PERSON
31 .63377 1.73052 .65007 1.85767 .66647 1.99821 .6829 32 .63404 1.73254 .65034 1.85990 .66674 2.00067 .6832	
32 .63404 1.73254 .65034 1.85990 .66674 2.00067 .6832 .63431 1.73456 .65061 1.86213 .66702 2.00315 .6835	
34 .63458 1.73659 .65088 1.86437 .66729 2.00562 .6838	2.16255 3
35 .63485 1.73862 .65116 1.86661 .66756 2.00810 .6840 36 .63512 1.74065 .65143 1.86885 .66784 2.01059 .6843	
37 .63539 1.74269 .65170 1.87109 .66811 2.01308 .6846	2.17085 37
38 .63566 1.74473 .65197 1.87334 .66839 2.01557 .6849	
39 .63594 1.74677 .65225 1.87560 .66866 2.01807 .6851 .63621 1.74881 .65252 1.87785 .66894 2.02057 .6854	
41 .63648 1.75086 .65279 1.88011 .66921 2.02308 .68573	
42 .63675 1.75292 .65306 1.88238 .66949 2.02559 .6860	
43 .63702 1.75497 .65334 1.88465 .66976 2.02810 .6862 44 .63729 1.75703 .65361 1.88692 .67003 2.03062 .6865	
45 .63756 1.75909 .65388 1.88920 .67031 2.03315 .6868	2.19322 45
46 .63783 1.76116 .65416 1.89148 .67058 2.03568 .6871	2.19604 46 2.19886 47
47 .63810 1.76323 .65443 1.89376 .67086 2.03821 .6873 48 .63838 1.76530 .65470 1.89605 .67113 2.04075 .6876	2.19886 46
49 .63865 1.76737 .65497 1.89834 .67141 2.04329 .6879	2.20453 49
50 .63892 1.76945 .65525 1.90063 .67168 2.04584 .68825	
51 .63919 1.77154 .65552 1.90293 .67196 2.04839 .68849 52 .63946 1.77362 .65579 1.90524 .67223 2.05094 .68877	2.21021 51 2.21306 52
53 .63973 1.77571 .65607 1.90754 .67251 2.05350 .68905	2.21592 53
54 .64000 1 77780 .65634 1.90986 .67278 2.05607 .68938	2.21878 54
55 .64027 1.77990 .65661 1.91217 .67306 2.05864 .68960 56 .64055 1.78200 .65689 1.91449 .67333 2.06121 .68988	2.22165 55 2.22452 56
57 .64082 1.78410 .65716 1.91681 .67361 2.06379 .69015	2.22740 57
58 .64109 1.78621 .65743 1.91914 .67388 2.06637 .69043	
59 .64136 1.78832 .65771 1.92147 .67416 2.06896 .69071 60 .64163 1.79043 .65798 1.92380 .67443 2.07155 .69098	2.23028 58 2.23317 59

,	7	2°	7	3°	7	4°	7	5°	
'	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	-
0	.69098	2.23607	.70763	2.42030	.72436	2,62796	.74118	2.86370	-
1	.69126	2.23897	.70791	2.42356	.72464	2.63164	.74146	2.86790	-
23	.69154	2.24187	.70818	2.42683	.72492	2 63533	.74174	2.87211	-
4	.69181	2.24478 2.24770	.70846	2.43010 2.43337	.72520	2.63903 2.64274	.74202 .74231	2.87633 2.88056	1
5	.69237	2.25062	70902	2.43666	.72576	2.64645	.74259	2.88479	
6	69264	2.25355	.70930	2.43995	.72604	2.65018	.74287	2.88904	1
7	.69292	2.25648	.70958	2.44324	.72632	2.65391	.74315	2.89330	1
8	.69320	2.25942	.70985	2.44655	.72660	2.65765	.74343	2.89756	ı
10	.69347 .69375	2 26237 2.26531	.71013	2.44986 2.45317	.72688 .72716	2.66140 2.66515	.74371	2.90184 2.90613	
11									
12	.69403	2.26827	.71069	2.45650 2.45983	.72744	2.66892 2.67269	.74427	2.91042 2.91473	-
13	.69458	2.27420	.71125	2.46316	.72800	2.67647	.74484	2.91904	-
14	.69486	2.27717	.71153	2.46651	.72828	2.68025	.74512	2.92337	1
15	.69514	2.28015	.71180	2.46986	.72856	2.68405	.74540	2.92770	
16	.69541	2.28313 2.28612	.71208	2.47321 2.47658	.72884	2.68785 2.69167	.74568	2.93204 2.93640	
18	.69597	2.28912	.71264	2.47995	.72940	2.69549	.74624	2.94076	-
19	.69624	2.29212	.71292	2.48333	.72968	2.69931	.74652	2.94514	1
30	.69652	2.29512	.71320	2.48671	.72996	2.70315	.74680	2.94952	1
21	.69680	2.29814	.71348	2.49010	.73024	2.70700	.74709	2.95392	1
22	.69708	2.30115	.71375	2.49350	.73052	2.71085	.74737	2.95832	1
23	.69735	2.30418 2.30721	.71403	2.49691 2.50032	.73080	2.71471 2.71858	.74765	2.96274 2.96716	
25	.69791	2.31024	.71459	2.50374	.73108	2.72246	.74821	2.97160	-
26	.69818	2.31328	.71487	2.50716	.73164	2.72635	.74849	2.97604	1
27	.69846	2.31633	.71515	2.51060	.73192	2.73024	.74878	2.98050	1
28	.69874	2.31939	.71543	2.51404	.73220	2.73414 2.73806	.74906 .74934	2.98497 2.98944	
30	.69929	2.32551	.71571	2.51748 2.52094	.73248	2.74198	.74962	2.99393	1
31	.69957	2.32858	.71626	2.52440	73304	2.74591	.74990	2.99843	1
32	.69985	2.33166	.71654	2.52787	.73332	2.74984	.75018	3.00293	1
33	.70013	2.33474	.71682	2.53134	.73360	2.75379	.75047	3.00745	1
34	.70040	2.33783	.71710	2.53482	.73388	2.75775	.75075	3.01198	1
35	.70068 .70096	2.34092 2.34403	.71738	2.53831 2.54181	.73416	2.76171 2.76568	.75103	3.01652 3.02107	
37	.70124	2.34713	.71794	2.54531	.73472	2.76966	.75159	3.02563	1
38	.70151	2.35025	.71822	2.54883	.73500	2.77365	.75187	3.03020	1
39	.70179	2.35336	.71850	2.55235	.73529	2.77765	.75216	3.03479	1
10	.70207	2.35649	.71877	2.55587	.73557	2.78166	.75244	3.03938	1
11	.70235	2.35962	.71905	2.55940	.73585	2.78568	.75272	3.04398	1
13	.70263 .70290	2.36276 2.36590	.71933	2.56294 2.56649	.73613	2.78970 2.79374	.75300	3.04860 3.05322	-
11	.70318	2.36905	.71989	2.57005	.73669	2.79778	.75356	3.05786	-
15	.70346	2.37221	.72017	2.57361	.73697	2.80183	.75385	3.06251	1
46	.70374	2.37537	.72045	2.57718	.73725	2.80589	.75413	3.06717	1
17 18	.70401 .70429	2.37854	.72073	2.58076	.73753	2.80996	.75441	3.07184 3.07652	
19	.70457	2.38171 2.38489	.72101	2.58434 2.58794	.73781	2.81404 2.81813	.75409	3.08121	
50	.70485	2.38808	.72157	2.59154	.73837	2.82223	.75526	3.08591	
51	.70513	2.39128	.72185	2.59514	.73865	2.82633	.75554	3.09063	1
52	.70540	2.39448	.72213	2.59876	.73893	2.83045	.75582	3.09535	1
53	.70568	2.39768	.72241	2.60238	.73921	2.83457	.75610	3.10009	-
54	.70596 .70624	2.40089 2.40411	.72269	2.60601 2.60965	.73950 .73978	2.83871 2.84285	.75639	3.10484 3.10960	1
56	.70652	2.40734	.72324	2.61330	.74006	2.84700	.75695	8.11437	
57	.70679	2.41057	.72352	2.61695	.74034	2.85116	.75723	3.11915	1
8	.70707	2.41381	.72380	2.62061	.74062	2.85533	.75751	3.12394	
59	.70735 .70763	2.41705 2.42030	.72408 .72436	2.62428 2.62796	.74090 .74118	2.85951 2.86370	.75780	3.12875 3.13357	1

									1
,	7	′6°	7	70	7	8°	7	′9°	,
	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	
0	.75808	3.13357	.77505	3.44541	.79209	3.80973	.80919	4.24084	0
	.75836 .75864	3.13839 3.14323	.77533 .77562	3.45102 3.45664	.79237 .79266	3.81633 3.82294	.80948	4.24870 4.25658	1 2
3	.75892	3.14809	.77590	3.46228	.79294	3.82956	.81005	4.26448	3
4	.75921	3.15295	.77618	3.46793	.79323	3.83621	.81033	4.27241	4
5	.75949 .75977	3.15782	.77647 .77675	3.47360 3.47928	.79351	3.84288 3.84956	.81062 .81090	4.28036 4.28833	5
7	.76005	3.16761	.77703	3.48498	79408	3.85627	.81119	4.29634	7
8	.76034	3.17252	.77732	3.49069	.79437	3.86299	.81148	4.30436	8
9	.76062	3.17744	.77760	3.49642	.79465	3.86973	.81176	4.31241	9
10	.76090	3.18238	.77788	3.50216	.79493	3.87649	.81205	4.32049	10
11	.76118	3.18733	.77817	3.50791	.79522	3.88327	.81233	4.32859	11
12 13	.76147 .76175	3.19228 3.19725	.77845	3.51368 3.51947	.79550	3.89007	.81262 .81290	4.33671 4.34486	12
14	.76203	3.20224	.77902	3.52527	.79579	3.89689 3.90373	.81319	4.35304	14
15	.76231	3.20723	.77930	3.53109	.79636	3.91058	.81348	4.36124	15
16	.76260	3.21224	.77959	3.53692	.79664	3.91746	.81376	4.36947	16
17	.76288	3.21726	.77987	3.54277	.79693	3.92436	.81405	4.37772	17
18	.76316	3.22229 3.22734	.78015	3.54863 3.55451	.79721	3.93128 3.93821	.81433	4.38600	18
20	.76373	3.23239	.78072	3.56041	.79778	3.94517	.81491	4.40263	20
21	.76401	3.23746	.78101	3,56632	.79807	3.95215	.81519	4.41099	21
22	.76429	3.24255	.78129	3.57224	.79835	3.95914	.81548	4.41937	22
23	.76458	3.24764	.78157	3.57819	.79864	3.96616	.81576	4.42778	23
24	.76486	3.25275	.78186	3.58414	.79892	3.97320	.81605	4.43622	24
25 26	.76514 .76542	3.25787 3.26300	.78214	3.59012 3.59611	.79921	3.98025	.81633 .81662	4.44468 4.45317	25 26
27	.76571	3.26814	.78271	3.60211	.79978	3.98733 3.99443	.81691	4.46169	27
28	.76599	3.27330	.78299	3.60813	.80006	4.00155	.81719	4.47023	28
29	.76627	3.27847	.78328	3.61417	.80035	4.00869	.81748	4.47881	29
30	.76655	3.28366	.78356	3.62023	.80063	4.01585	.81776	4.48740	30
31	.76684	3.28885	.78384	3.62630	.80092	4.02303	.81805	4.49603	31
32	.76712 .76740	3.29406 3.29929	.78413	3.63238 3.63849	.80120	4.03024	.81834 .81862	4.50468	32
34	.76769	3.30452	.78470	3.64461	.80149 .80177	4.03746 4.04471	.81891	4.51337	34
35	.76797	3.30977	.78498	3.65074	.80206	4.05197	.81919	4.53081	35
36	.76825	3.31503	.78526	3.65690	.80234	4.05926	.81948	4.53958	36
37 38	.76854	3.32031	.78555	3.66307	.80263	4.06657	.81977	4.54837	37
39	.76882 .76910	3.32560 3.33090	.78583 .78612	3.66925 3.67545	.80291 .80320	4.07390 4.08125	.82005 .82034	4.55720 4.56605	38
40	.76938	3.33622	.78640	3.68167	.80348	4.08863	.82063	4.57493	40
41	.76967	3.34154	.78669	3,68791	.80377	4.09602	.82091	4.58383	41
42	.76995	3.34689	78697	3.69417	.80405	4.10344	.82120	4.59277	42
43	.77023	3.35224	.78725	3.70044	.80434	4.11088	.82148	4.60174	43
44	.77052	3.35761	.78754	3.70673	.80462	4.11835	.82177	4.61073	44
45	.77080 .77108	3.36299 3.36839	.78782	3.71303 3.71935	.80491 .80520	4.12583 4.13334	.82206	4.61976	45
47	.77137	3.37380	.78839	3.72569	.80548	4.13334	.82263	4.63790	47
48	.77165	3,37923	.78868	3.72569 3.73205	.80577	4.14842	.82292	4.64701	48
49	.77193	3.38466	.78896	3.73843	.80605	4.15599	.82320	4.65616	49
50	.77222	3.39012	.78924	3.74482	.80634	4.16359	.82349	4.66533	50
51	.77250	3.39558	.78953	3.75123	.80662	4.17121	.82377	4.67454	51
52 53	.77278	3.40106 3.40656	.78981	3.75766	.80691	4.17886	.82406 .82435	4.68377	52 53
54	.77335	3,41206	.79010 .79038	3.76411 3.77057	.80719	4.18652 4.19421	.82463	4.70234	54
55	.77363	3.41759	.79067	3.77705	.80776	4.20193	.82492	4.71166	55
56	.77392	3.42312	.79095	3.78355	.80805	4.20966	.82521	4.72102	56
57	.77420	3.42867	.79123	3.79007	.80833	4.21742	82549	4.73041	57
58	.77448	3.43424 3.43982	.79152 .79180	3.79661 3.80316	.80862	4.22521 4.23301	.82578	4.73983	58 59
60	.77505	3.44541	79209	3.80973	80919	4.24084	.82635	4.75877	60

_				- VERSIN		E-11-11-15			
,		80°		81°		82°	138	83°	,
	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	
0	.82635	4.75877	.84357	5.39245	.86083	6.18530	.87813	7.20551	0
1 2	.82664 .82692	4.76829	.84385	5.40422 5.41602	.86112	6.20020	.87842	7.22500 7.24457	1 9
3	.82721	4.78742	.81143	5.42787	.86169	6.23019	.87900	7.26425	3
4	.82750	4.79703	.84471	5.43977	.86198	6.24529	.87929	7.28402	4
5 6	.82778	4.81635	.84529	5.45171 5.46369	.86256	6.26044 6.27566	.87957	7.30388 7.32384	5
7	.82836	4.82606	.84558	5.47572	.86284	6.29095	.88015	7.34390	6 7 8
8 9	.82864	4.83581 4.84558	.84586	5.48779 5.49991	.86313	6.30630	.88044	7.36405	8
10	.82922	4.85539	.84644	5.51208	.86371	6.32171	.88102	7.38431 7.40466	9
11	.82950	4.86524	.84673	5.52429	.86400	6.35274	.88131	7.42511	11
12 13	.82979	4.87511 4.88502	.84701 .84730	5.53655 5.54886	.86428 .86457	6.36835	.88160	7.44566 7.46632	12
14	.83036	4.89497	.84759	5.56121	.86486	6.39978	.88217	7.48707	14
15	.83065	4.90495	.84788	5.57361	.86515	6.41560	.88246	7.50793	15
16	.83094	4.91496 4.92501	.84816	5.58606	.86544	6.43148	.88275	7.52889 7.54996	16 17
18	.83151	4.93509	.84874	5.61110	.86601	6.46346	.88333	7.57113	18
19 20	.83180	4.94521	.84903 .84931	5.62369	.86630	6.47955	.88362	7.59241	19
21	.83237	4.95536	.84960	5.63633	.86659	6.49571	.88391	7.61379	20
22	.83266	4.97577	.84989	5.66176	.86717	6.51194	.88448	7.65688	21 22
23	.83294	4.98603	.85018	5.67454	.86746	6.54462	.88477	7.67859	23
24 25	.83323	4.99633 5.00666	.85046	5.68738 5.70027	.86774	6.56107	.88506	7.70041	24 25
26	.83380	5.01703	.85104	5.71321	.86832	6.57759 6.59418	.88535	7.72234 7.74438	26
27	.83409	5.02743	.85133	5.72620	.86861	6.61085	.88593	7.76653	27
28 29	.83438 .83467	5.03787 5.04834	.85162 .85190	5.73924 5.75233	.86890	6.62759	.88623	7.78880 7.81118	28 29
30	.83495	5.05886	.85219	5.76547	.86947	6.66130	.88680	7.83367	30
31	.83524	5.06941	.85248	5.77866	.86976	6.67826	.88709	7.85628	31
33	.83553	5.08000 5.09062	.85277	5.79191 5.80521	.87005	6.69530	.88737	7.87901	32
34	.83610	5.10129	.85334	5.81856	.87034	6.71242 6.72962	.88766	7.90186 7.92482	33
35	.83639	5.11199	.85363	5.83196	.87092	6.74689	.88824	7.94791	35
36 37	.83667 $.83696$	5.12273 5.13350	.85392 .85420	5.84542 5.85893	.87120 .87149	6.76424 6.78167	.88853	7.97111 7.99444	36
38	.83725	5.14432	.85449	5.87250	.87178	6.79918	.88911	8.01788	38
39	.83754	5.15517	.85478	5.88612	.87207	6.81677	.88940	8.04146	39
40	.83782	5.16607	.85507	5.89979	.87236	6.83443	.88969	8.06515	40
41 42	.83811	5.17700 5.18797	.85536 .85564	5.91352 5.92731	.87265 .87294	6.85218 6.87001	.88998	8.08897 8.11292	41 42
43	.83868	5.19898	.85593	5.94115	.87322	6.88792	.89055	8.13699	43
44	.83897	5.21004	.85622	5.95505	.87351	6.90592	.89084	8.16120	41
45 46	.83926 .83954	5.22113 5.23226	.85651	5.96900 5.98301	.87380 .87409	6.92400	.89113	8.18553 8.20999	45
47	.83983	5.24343	.85708	5.99708	.87438	6.96040	.89171	8.23459	47
48 49	.84012 .84041	5.25464 5.26590	.85737	6.01120 6.02538	.87467 .87496	6.97873 6.99714	.89200	8.25931 8.28417	48
50	.84069	5.27719	.85795	6.03962	.87524	7.01565	.89258	8.30917	50
51	.84098	5.28853	.85823	6.05392	.87553	7.03423	.89287	8.33430	51
52 53	.84127 .84155	5.29991 5.31133	.85852 .85881	6.06828 6.08269	.87582 .87611	7.05291 7.07167	.89316 .89345	8.35957 8.38497	52 53
54	.84184	5.32279	.85910	6.09717	.87640	7.09052	.89374	8.41052	54
55	.84213	5.33429	.85939	6.11171	.87669	7.10946	.89403	8.43620	55
56 57	.84242 .84270	5.34584 5.35743	.85967	6.12630 6.14096	.87698 .87726	7.12849 7.14760	.89431	8.46203	56
58	.84299	5.36906	.86025	6,15568	.87755	7.16681	.89489	8.51411	58
59	.84328	5.38073	.86054	6.17046	.87784	7.18612	.89518	8.54037	59
60	.84357	5.39245	.86083	6.18530	.87813	7,20551	.89547	8.56677	1

	15	84°		85°		36°	
,	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	1.
0 1 2 3 4 5 6 7 8 9	.89547 .89576 .89605 .89634 .89663 .89692 .89721 .89750 .89779 .8988 .8988	8.59677 8.59332 8.62002 8.64687 8.67387 8.70103 8.72833 8.75579 8.78341 8.81119 8.83912	.91284 .91313 .91342 .91371 .91400 .91429 .91458 .91487 .91516 .91545 .91574	10.47871 10.51199 10.55052 10.58932 10.62837 10.66769 10.70728 10.74714 10.78727 10.882768 10.86837	.93024 .93053 .93082 .93111 .93140 .93169 .93198 .93297 .93257 .93256 .93315	13.33559 13.39547 13.45586 13.51676 13.57817 13.64011 13.70258 13.76558 13.82918 13.8933 13.95788	0 1 2 3 4 5 6 7 8 9
11 12 13 14 15 16 17 18 19 20	.89865 .89894 .89923 .89952 .89981 .90010 .90039 .90068 .90097 .90126	8.86722 8.89547 8.92389 8.95248 8.98123 9.01015 9.03923 9.06849 9.09792 9.12752	.91603 .91632 .91661 .91690 .91719 .91748 .91777 .91806 .91835 .91864	10.90934 10.95060 10.99214 11.03397 11.07610 11.11852 11.16125 11.20427 11.24761 11.29125	.93344 .93373 .93402 .93431 .93460 .93489 .93518 .93547 .98576 .93605	14.02310 14.08890 14.15527 14.2223 14.28979 14.35795 14.42672 14.49611 14.56614 14.63679	11 12 13 14 15 16 17 18 19 20
21 22 23 24 25 26 27 28 29 30	.90155 .90184 .90213 .90242 .90271 .90300 .90329 .90358 .90366	9.15730 9.18725 9.21739 9.24770 9.27819 9.30887 9.33973 9.37077 9.40201 9.43343	.91893 .91922 .91951 .91980 .92009 .92038 .92067 .92096 .92125 .92154	11.33521 11.37948 11.42408 11.40300 11.51424 11.55982 11.60572 11.65197 11.69856 11.74550	.93634 .93663 .93692 .93721 .93750 .93779 .93808 .93837 .93866 .93895	14.70810 14.78005 14.85268 14.92597 14.99995 15.07462 15.14999 15.22607 15.30287 15.38041	21 22 23 24 25 26 27 28 29 30
31 32 33 34 35 36 37 38 39 40	.90444 .90473 .90502 .90531 .90560 .90589 .90618 .90647 .90676	9.46505 9.49685 9.52886 9.56106 9.59346 9.62605 9.65885 9.69186 9.75507 9.75849	.92183 .92212 .92241 .92270 .92299 .92328 .92357 .92386 .92415 .92444	11.79278 11.84042 11.88841 11.98677 11.98549 12.08458 12.08040 12.13388 12.18411 12.23472	.93924 .93953 .93982 .94011 .94040 .94069 .94098 .94127 .94156 .94186	15.45869 15.53772 15.61751 15.69808 15.77944 15.86159 15.94456 16.02835 16.11297 16.19843	31 32 33 34 35 36 37 38 39 40
41 42 43 44 45 46 47 48 49 50	.90734 .90763 .90792 .90821 .90850 .90879 .90908 .90937 .90966 .90995	9.79212 9.82596 9.86001 9.89428 9.92677 9.96348 9.99841 10.03356 10.06894 10.10455	.92473 .92502 .92531 .92560 .92589 .92618 .92647 .92676 .92705 .92734	12.28572 12.33712 12.38891 12.44112 12.49373 12.54676 12.60021 12.65408 12.70838 12.70812	.94215 .94244 .94273 .94302 .94381 .94360 .94389 .94418 .94477	16.28476 16.37196 16.46005 16.54903 16.63893 16.72975 16.82152 16.91424 17.00794 17.10262	41 42 43 41 45 46 47 48 49 50
51 52 53 54 55 56 57 58 59 60	.91024 .91053 .91082 .91111 .91140 .91169 .91197 .91226 .91255 .91284	10.14039 10.17646 10.21277 10.24932 10.28610 10.32313 10.36040 10.39792 10.43569 10.47371	.92763 .92792 .92821 .92850 .92879 .92908 .92987 .92966 .92995 .93024	12.81829 12.87391 12.92999 12.98651 13.04350 13.10096 13.15889 13.21730 13.27620 13.3559	.94505 .94534 .94563 .94592 .94621 .94650 .94679 .94708 .94737 .94766	17,19830 17,29501 17,39274 17,49153 17,59139 17,69233 17,79438 17,89755 18,00185 18,10732	51 52 53 54 55 56 57 58 59 60

,	0.00	37°	8	88°	8	9°	1
	Vers.	Exsec.	Vers.	Exsec.	Vers.	Exsec.	
0	.94766	18.10732	.96510	27.65371	.98255	56.29869	0
1	.94795	18.21397	.96539	27.89440	.98284	57.26976	1
2 3	.94825	18 32182 18 43088	.96568	28.13917 28.38812	.98313	58.27431 59.31411	2 3 4 5 6 7
4	.94883	18.54119	.96626	28.64137	.98371	60.39105	4
5	.94912	18.65275	.96655	28.89903	.98400	61.50715	5
5 6	.94941	18.76560	.96684	29.16120	.98429	62.66460	6
7	.94970	18.87976	.96714	29.42802	.98458	63.86572	7
8 9	.94999	18.99524	.96743	29.69960	.98487	65.11304	8
10	.95028	19.11208 19.23028	.96772	29.97607 30.25758	.98517 .98546	66.40927 67.75736	10
11	.95086	19.34989	.96830	30.54425	.98575	69.16047	11
12	.95115	19.47093	.96859	30.83623	.98604	70.62285	12
13	.95144	19.59341	.96888	31.13366	.98633	72.14583	13
14	.95173	19.71737	.96917	31.43671	.98662	73.73586	14
15 16	.95202	19.84283 19.96982	.96946	31.74554 32.06030	.98691	75.39655	15
17	.95260	20.09838	.97004	32.38118	.98720	77,13274 78,94968	17
18	.95289	20.22852	.97033	32.70835	.98778	80.85315	18
19	.95318	20.36027	.97062	33.04199	.98807	82.84947	19
20	.95347	20.49368	.97092	33.38232	.98836	84.94561	20
21	.95377	20.62876	.97121	33.72952	.98866	87.14924	21
22 23	.95406	20.76555	.97150	34.08380	.98895	89.46886	22
24	.95435	20.90409 21.04440	.97179	34.44539 34.81452	.98924	91.91387	23
25	.95493	21.18653	.97237	35.19141	.98953	94.49471 97.22303	25
26	.95522	21,33050	.97266	35.57633	.99011	100.1119	26
27	.95551	21.47635	.97295	35.96953	.99040	103.1757	27
28	.95580	21.62413	.97324	36.37127	.99069	106.4311	28
29 30	.95609	21.77386 21.92559	.97353	36.78185 37.20155	.99098	109.8966 113.5930	29 30
31	.95667	22.07935	.97411	37.63068	.99156	117.5444	31
32	.95696	22.23520	.97440	38.06957	.99186	121.7780	32
33	.95725	22.39316	.97470	38.51855	.99215	126.3253	33
34	.95754	22.55329	.97499	38.97797	.99244	131.2223	34
35 36	.95783 .95812	22.71563	.97528	39.44820	.99273	136.5111	35
37	.95812	22.88022 23.04712	.97557 .97586	39.92963 40.42266	.99302	142.2406 148.4684	36
38	.95871	23.21637	.97615	40.92772	.99360	155 2623	38
39	.95900	23.38802	.97644	41.44525	.99389	155.2623 162.7033	39
40	.95929	23.56212	.97673	41.97571	.99418	170.8883	40
41	.95958	23.73873	.97702	42.51961	.99447	179.9350	41
42 43	.95987 .96016	23.91790	.97731	43.07746	.99476	189.9868	42
44	.96045	24.09969 24.28414	.97760	43.64980 44.23720	.99505	201.2212 213.8600	43
45	.96074	24.47134	.97819	44.84026	.99564	228.1839	45
46	.96103	24.66132	.97848	45.45965	.99593	244.5540	46
47	.96132	24.85417	.97877	46.09596	.99622	263.4427	47
48 49	.96161	25.04994 25.24869	.97906	46.74997	.99651	285.4795	48
50	.96219	25.24869 25.45051	.97935	47.42241 48.11406	.99680	311,5230 342,7752	49 50
51	.96248	25.65546	.97993	48.82576	.99738	380,9723	51
52	.96277	25.86360	.98022	49.55840	.99767	428.7187	52
53	.96307	26.07503	.98051	50.31290	.99796	490.1070	53
54 55	.96336	26.28981	.98080	51.09027	.99825	571.9581	54
56	.96394	26.50804 26.72978	.98109	51.89156 52.71790	.99855	686,5496 858,4369	55
57	.96423	26.95513	,98168	53.57046	.99913	1144.916	57
58	.96452	27.18417	.98197	54.45053	.99942	1717.874	58
60	.96481	27.41700 27.65371	.98226	55.35946 56.29869	1.00000	3436.747 Infinite	59

Depth	Base	Base						
	12	14	16	18	22	24	26	28
-		-		20	00	00	0.04	105
1 2	45 93	53 107	122	68	82 167	90 181	97 196	105 211
2 3	142	163	186	208	253	275	297	319
4	193	222	252	281	341	370	400	430
5	245 300	282 344	319	356	431	468	505	542
7	356	408	389 460	433 512	522 616	567 668	611 719	656
7 8	415	474	533	593	711	770	830	889
9	475	542	608	675	808	875	942	1008
10	537	611	685	759	907	981	1056	1130
11	601	682	764	845	1008	1090	1171	1253
12 13	667 734	756 831	844 926	933 1023	1111 1216	1200 1312	1289 1408	1378 1505
14	804	907	1010	1115	1322	1426	1530	1633
15	875	986	1096	1208	1431	1542	1653	1764
16	948	1067	1184	1304	1541	1659	1778	1896
17 18	1023 1100	1149 1233	1274 1366	1401 1500	1653 1767	1779 1900	1905 2033	2031 2167
19	1179	1319	1460	1601	1882	2023	2164	2305
20	1179 1259	1407	1555	1704	2000	2148	2296	2414
21	1342	1497	1653	1808	2119	2275	2431	2586
22 23	1426	1589	1752	1915	2241	2404	2567	2730
23 24	1512 1600	1682 1778	1853 1955	2023 2133	2364 2489	2534 2667	2705 2844	2875 3022
25	1690	1875	2060	2245	2616	2801	2986	3171
25 26 27	1781	1974	2166	2359	2744	2937	3130	3322
27	1875	2075	2274	2475	2875	3075	3275	3475
28 29	1970 2068	2178 2282	2384 2496	2593 2712	3007 3142	3215 3356	3422 3571	3630 3786
30	2167	2389	2610	2833	3278	3500	3722	3944
31	2268	2497	2726	2956	3416	3645	3875	4105
32	2370	2607	2844	3081	3556	3793	4030	4267
33 34	2475 2581	2719 2833	2964 3085	3208	3697 3841	3942	4186 4344	4431
35	2690	2949	3208	3337 3468	3986	4093 4245	4505	4596 4764
36	2800	3067	3333	3600	4133	4400	4667	4933
37	2912	3186	3460	3734	4282	4556	4831	5105
38 39	3026 3142	3307 3431	3589 3719	3870 4008	4433 4586	4715 4875	4996 5164	5278 5453
40	3259	3556	3852	4148	4741	5037	5333	5630
41	3379	3682	3986	4290	4897	5201	5505	5808
42	3500	3811	4122	4433	5056	5367	5678	5989
43	3623	3942	4260	4579	5216	5534	5853	6171
44 45	3748 3875	4074 4208	4400 4541	4726 4875	5378 5542	5704 5875	6030 6208	6356 6542
46	4004	4344	4684	5026	5707	6048	6389	6730
47	4134	4482	4830	5179	5875	6223	6571	6919
48 49	4267	4622 4764	4978 5127	5333 5490	6044 6216	6400	6756	7111 7305
50	4537	4907	5278	5648	6389	6579 6759	694 2 7130	7500
51	4675	5053	5430	5808	6564	6942	7319	7697
52	4815	5200	5584	5970	6741	7126	7511	7896
53	4956	5349	5741	6134	6919	7312	7705	8097
54 55	5100 5245	5500 5653	5900 6060	6300 6468	7100 7282	7500 7690	7900 8097	8300 8505
56	5393	5807	6222	6637	7467	7881	8296	8711
57	5542	5964	6386	6808	7653	8075	8497	8919
58	5693	6122	6552	6981	7841	8270	8700	9130
59 60	5845 6000	6282 6444	6719 6889	7156 7333	8031 8222	8468 8667	8905 9111	9342 9556
- 00	0000	OXII	0000	1000	CARR	0001	3111	0000

TABLE XIV.-CUBIC YARDS PER 100 FEET. SLOPES 1/2: 1.

Depth	Base	Base						
	12	14	16	18	22	24	26	28
1	46	54	61	69	83	91	98	106
2	96	111	126	141	170	185	200	215
3	150	172	194	217	261	283	306	328
4	207	237	267	296	356	385	415	444
5	269	306	343	380	454	491	528	563
5	333	378	422	467	556	600	644	689
77	402	454	506	557	661	713	765	817
7 8	474	533	593	652	770	830	889	948
9	550	617	683	750	883	950	1017	108
10	630	704	778	852	1000	1074	1148	122
11	713	794	876	957	1120	1202	1283	1363
12	800	889	978	1067	1244	1333	1422	151
13	891	987	1083	1180	1372	1469	1565	166
14	985	1089	1193	1296	1504	1607	1711	181
15	1083	1194	1306	1417	1639	1750	1861	1979
16	1185	1304	1422	1541	1779	1896	2015	213
17	1291	1417	1543	1669	1920	2046	2172	2298
18	1400	1533	1667	1800	2067	2200	2333	246
19	1513	1654	1794	1935	2217	2357	2498	2639
20	1630	1778	1926	2074	2370	2519	2667	281
21	1750	1906	2061	2217	2528	2683	2839	299
22 23	1874	2037	2200	2363	2689	2852	3015	3178
23	2002 2133	2172 2311	2343	2513	2854	3024	3194	3363
			2489	2667	3022	3200	3378	3556
25	2269	2454	2639	2824	3194	3380	3565	3750
26	2407	2600	2793	2985	3370	3563	3756	3948
27 28	2550 2696	2750 2904	2950	3150	3550	3750	3950	415
29		3061	3111	3319	3733	3941	4148	4356
30	2846 3000	3222	3276 3444	3491 3667	3920 4111	4135	4350 4556	4568
31	3157	3387	3617	3846	4306	4535	4765	499
32	3319	3556	3793	4030	4504	4741	4978	5213
33	3483	3728	3972	4217	4706	4950	5194	5439
34	3652	3904	4156	4407	4911	5163	5415	5667
35	3824	4083	4343	4602	5120	5380	5639	5898
36	4000	4267	4533	4800	5333	5600	5867	6133
37	4180	4454	4728	5002	5550	5824	6098	6372
38	4363	4644	4926	5207	5770	6052	6333	6613
39	4550	4839	5128	5417	5994	6283	6572	6861
40	4741	5037	5333	5630	6222	6519	6815	7111
41	4935	5239	5543	5846	6454	6757	7061	7365
43	5133 5335	5444	5756	6067	6689	7000	7311	7622
44	5541	5654 5867	5972	6291	6928	7246	7565	7888
45	5750	6083	6193	6519	7170	7496	7822	8148
46	5963	6304	6417 6644	6750 6985	7417	7750	8083	8417
47	6180	6528	6876	7224	7667 7920	8007 8269	8348	8689
48	6400	6756	7111	7/107	0170	8533	8617 8889	896
49	6624	6987	7350	7467 7713	8178 8439	8802	9165	9244
50	6852	7222	7593	7963	8764	9074	9444	9815
51	7083	7461	7839	8217	8972	9350	9728	10106
52	7319	7704	8089	8474	9244	9630	10015	10400
53	7557	7950	8343	8735	9520	9913	10306	10698
54	7800	8200	8600	9000	9800	10200	10600	11000
55	8046	8454	8861	9269	10083	10491	10898	11306
56	8296	8711	9126	9541	10370	10785	11200	11615
57	8550	8972	9394	9817	10661	11083	11506	11928
58	8807	9237	9667	10096	10956	11385	11815	12244
59	9069	9506	9943	10380	11254	11691	12128	12565
60	9333	9778	10222	10667	11556	12000	12444	12889

Depth	Base	Base	Base	Base	Base	Base	Base	Base
e#	12	14	16	18	20	28	30	32
1 2 3 4 5 6 7 8 9	48 104 167 237 315 400 493 593 700 815	56 119 189 267 352 444 544 652 767 889	63 133 211 296 389 489 596 711 833 963	70 148 233 326 426 533 648 770 900 1037	78 163 256 356 463 578 700 830 967 1111	107 223 344 474 611 756 907 1067 1233 1407	115 237 367 504 648 800 959 1126 1300 1481	122 252 389 533 685 844 1011 1185 1367 1556
11 12 13 14 15 16 17 18 19	937 1067 1204 1348 1500 1659 1826 2000 2181 2370	1019 1156 1300 1452 1611 1778 1952 2133 2322 2519	1100 1244 1396 1556 1722 1896 2078 2267 2463 2667	1181 1333 1493 1659 1833 2015 2204 2400 2604 2815	1263 1422 1589 1763 1944 2133 2330 2533 2744 2963	1589 1778 1974 2178 2389 2607 2833 3067 3307 3556	1670 1867 2070 2281 2500 2726 2959 3200 3448 3704	1752 1956 2167 2385 2611 2844 3085 3333 3589 3852
21	2567	2722	2878	3033	3189	3811	3967	4122
22	2770	2933	3096	3259	3422	4074	4237	4144
23	2981	3152	3322	3493	3663	4344	4515	4685
24	8200	3378	3556	3733	3911	4622	4800	4978
25	8426	3611	3796	3981	4167	4907	5093	5278
26	3659	3852	4044	4237	4430	5200	5393	5585
27	3900	4100	4300	4500	4700	5500	5700	5900
28	4148	4356	4563	4770	4978	5807	6015	6222
29	4404	4619	4833	5048	5263	6122	6337	6552
30	4667	4889	5111	5333	5556	6444	6667	6889
31	4937	5167	5396	5626	5856	6774	7004	7233
32	5215	5452	5689	5926	6163	7111	7348	7585
33	5500	5744	5989	6233	6478	7456	7700	7944
34	5793	6044	6296	6548	6800	7807	8059	8311
35	6093	6352	6611	6870	7130	8167	8426	8685
36	6400	6667	6933	7200	7467	8533	8800	9067
37	6715	6989	7263	7537	7811	8907	9181	9456
38	7037	7319	7600	7881	8163	9289	9570	9852
39	7367	7656	7944	8233	8522	9678	9967	10256
40	7704	8000	8296	8593	8889	10074	10370	10667
41	8048	8352	8656	8959	9263	10478	10781	11085
42	8400	8711	9022	9333	9644	10889	11200	11511
43	8759	9078	9396	9715	10033	11307	11626	11944
44	9126	9452	9778	10104	10430	11733	12059	12385
45	9500	9833	10167	10500	10833	12167	12500	12893
46	9881	10222	10563	10904	11244	12607	12948	13289
47	10270	10619	10967	11315	11663	13056	13404	13752
48	10667	11022	11378	11733	12089	13511	13867	14222
49	11070	11433	11796	12159	12522	13974	14337	14700
50	11481	11852	12222	12593	12963	14444	14815	15185
51	11900	12278	12656	13033	13411	14922	15300	15678
52	12326	12711	13096	13481	13867	15407	15793	16178
53	12759	13152	13544	13937	14330	15900	16293	16685
54	13200	13600	14000	14400	14800	16400	16800	17200
55	13648	14056	14463	14870	15278	16907	17315	17722
56	14104	14519	14933	15348	15763	17422	17837	18252
57	14567	14989	15411	15833	16256	17944	18367	18789
58	15037	15467	15896	16326	16756	18474	18904	19333
59	15515	15952	16389	16826	17263	19011	19448	19885
60	16000	16444	16889	17333	17778	19556	20000	20444

Depth	Base 12	Base 14	Base 16	Base 18	Base 20	Base 28	Base 30	Base 32
1	50	57	65	72	80	100	117	124
2 3	111	126	141	156	170	230	244	259
3	183	206	228	250	272	361	383	400
4	267	296	326	356	385	504	533	568
5	361	398	435	472	509	657	694	731
6	467	511	556	600	644	822	867	917
7	583	635	687	739	791	998	1050	110%
8 9	711	770	830	889 1050	948 1116	1185 1383	1244 1450	1304
10 .	850 1000	917 1074	983	1222	1296	1593	1667	174
11	1161	1243	1324	1406	1487	1813	1894	1970
12	1333	1422	1511	1600	1689	2044	2133	222
13	1517	1613	1709	1806	1902	2287	2383	248
14	1711	1815	1919	2022	2126	2541	2644	274
15	1917	2028	2139	2250	2361	2806	2917	302
16	2133	2252	2370	2489	2607	3081	3200	3319
17	2361	2487	2613	2739	2865	3369	3494	362
18	2600	2733	2867	3000	3133	3667	3800	393
19	2850	2991	3131	3272	3413	3976	4117	425
20	3111	3259	3407	3556	3704	4296	4444	459
21	3383	3539	3694	3850	4005	4628	4783	493
22 23	3667	3830	3993	4156	4318	4970	5133	529
23	3961	4131	4302	4472	4642	5324	5494	566
24	4267	4111	4622	4800	4978	5689 6065	5867	604
25	4583	4769	4954	5139 5489	5324 5681	6452	6250 6644	683
26 27	4911 5250	5104 5450	5296 5650	5850	6050	6850	7050	725
28	5600	5807	6015	6222	6430	7259	7467	767
29	5961	6176	6391	6606	6820	7680	7894	810
30	6333	6556	6778	7000	7222	8111	8333	855
31	6717	6946	7176	7406	7635	8554	8783	901
32	7111	7348	7585	7822	8059	9007	9244	948
33	7517	7761	8006	8250	8494	9472	9717	996
34	7933	8185	8437	8689	8941	9948	10200	1045
35	8361	8620	8880	9139	9398	10435	10694	1095
36	8800	9067	9333	9600	9867	10933	11200	1146
37 38	9250 9711	9524 9993	9798	10072 10556	10346 10837	11443 11963	11717 12244	1199
39	10183	10472	10274 10761	11050	11339	12494	12783	1307
40	10667	10963	11259	11556	11852	13037	13333	1363
41	11161	11465	11769	12072	12376	13591	13894	1419
42	11667	11978	12289	12600	12911	14156	14467	1477
43	12183	12502	12820	13139	13457	14731	15050	1536
44	12711	13037	13363	13689	14015	15319	15644	1597
45	13250	13583	13917	14250 14822	14583	15917	16250	1658
46	13800	14141	14481	14822	15163	16526	16867	1720
47	14361	14709	15057	15406	15754	17146	17494	1784
48	14933	15289	15644	16000	16356	17778	18133	1848
49	15517	15880	16243	16606	16968	18420	18783	1914
50	16111	16481	16852	17222	17592	19074	19444	1981
51 52	16717 17333	17094 17719	17472	17850 18489	18228 18874	19739	20117 20800	20494
53	17961	18354	18104 18746	19139	19531	20415 21102		2118
54	18600	19000	19400	19800	20200	21800	21494 22200	2188° 22600
55	19250	19657	20065	20472	20880	22509	22917	2332
56	19911	20326	20741	21156	21570	23230	23644	24059
57	20583	21006	21428	21850	22272	23961	24383	2480
58	21267	21696	22126	22556	22985	24704	25133	25563
59	21961	22398	22835	23272	23709	25457	25894	26332
60	22667	23111	23556	24000	21111	26222	26667	27117

		ī	1	1	1	1		
Depth	Base	Base	Base	Base	Base	Base	Base	Base
	12	14	16	18	20	28	30	32
1	52	59	67	74	81	111	119	126
2	119	133	148	163	178	237	959	267
2 3	119 200	222	244	267	289	237 378 533	252 400	422
4	296	222 326	244 356	267 385	289 415	533	563	593
5 6	407	444	481	519	556	704	741	778
6	533	578	622	697 830 1007	711 881 1067	889 1089	933	978
7	674	726	778	830	881	1089	1141	1193
7 8 9	674 830 1000	889	948	1007	1067	1304	1363 1600	1422
10	1185	889 1067 1259	778 948 1133 1333	1200 1407	1267 1481	1533 1778	1600	1667
	1	1				1	1852	1926
11 12	1385	1467	1548	1630	1711	2037	2119	2200
13	1600	1689	1778	1867 2119	1956 2215	2311 2600	2400	2489
14	1830 2074 2333	1926 2178	2022 2281	2385	2489	2904	2696 3007	2793 3111
15	2333	2444	2556	2667	2778	3222	9999	3111
16	2607	2726	2844	2963	3081	3556	3333 3674	3793
17	2896	3022	3148	3274	3400	3904	4030	4156
18	3200	5333	3467	3274 3600	3733	4267	4400	4533
19	3519	3659	3800	3941	4081	4644	4785	4926
20	3852	4000	4148	4296	3733 4081 4444	5037	5185	5333
21	4200	4356	4511	4667	4822	5444	5600	5756
22	4563	4730	4889 5281	5052	5215	5867	6030	6193
23 24 25	4941 5333	5111	5689	5452	5622 6044	6304	6474	6644
95	5741	5511 5926	6111	5867	6491	6756 7222 7704 8200	6933	7111 7593 8089
26	6163	6356	6548	6296 6741	6481 6933 7400	2704	7407 7896	1099
27	6163	6800	7000	7200	7400	8200	8400	8600
28	7052	7259	7467	7674	7881	8711	8919	9126
26 27 28 29	7519	6356 6800 7259 7783	7948	7674 8163	8378	9237	9452	9667
30	8000	8222	8111	8667	8389	9778	10000	10222
31	8496	8726	8956	9185	9415	10333	10563 11141 11733 12341	10793
32	9007	9244	9481	9719 10267 10830	9956 10511 11081	10904 11489	11141	11378
33	9533	9778 10326	10022 10578	10267	10511	11489	11733	11978
34	10074	10326	10578	10830	11081	12089	12341	12593 13222
35	10630 11200	10889 11467	11148 11733	11407 12000	11667 12267	12704 13333 13978	12963 13600	13867
36 37	11785	12059	12333	12607	19391	19079	14252	14526
38	12385	12667	12948	13230	13511	14637	14919	15200
39	13000	13289	13578	13230 13867	12381 13511 14156	14637 15311	15600	15889
40	13630	13926	14222	14519	14815	16000	16296	16593
41	14274	14578	14881	15185	15489	16704	17007	17311
42	14933	15244	15516	15867	16178	17422	17733 18474	18044
43	15607	15926	16224	16563	16881	18156	18474	18793
44	16296	16622	16948	17274	17000	18904	19230	19556
45 46	17000	17333 18059	17667 18400	17274 18000 18741	17600 18333 19081	19667	20000	20333 21126
47	17719 18452	18800	19148	19496	19844	20444 21237	20785 21585	21933
48	19200	19556	19911	20267	20622	22044	22400	22756
49	19963	20326	20689	21052	21415	22867	23230	23593
50	20741	20711	21481	21852	22222	23704	24074	24444
51	21:33	21911	22289	22667	23044	24556	24933	25311
52	22341	22726	23111	23496	23881 24733	25422 26304	25807	26193
53	23163	23556	23948	24341	24733	20304	26696 27600	27089 28000
54 55	24000 24852	24400 25259	24800 25667	25200 26074	25600 26481	27200 28111	28519	28926
56	25719	26133	26548	26963	27378	29037	29452	29867
57	23600	27022	27444	27867	28289	29978	30400	29867 30822
58	27496	27926	28356	28785	29215	30933	31363	31793
58 59 60	28407	28844	29281	29719	30156	31904	32341	32778 33778
_ 60	29333	29778	30222	30667	31111	32889	33333	33778
The State of the S	San	The State of the Local Division in the	The same of the same of	The Paris of the latest the lates				

Depth	Base	Base						
	12	14	16	18	20	28	30	32
1	56	63	70	78 178	85	115	122	130
2	133	148	163	178	193	252	267	281
3.	233	256	278	300	322	411	433	456
4	356	385	415	444	474	593	622	65%
5	500	537	574	611	648	796 1022	833	870
6	667	711	756	800	844 1063	1270	1322	1374
7 8	856 1067	907	959 1185	1244	1304	1541	1600	1659
9	1300	1367	1433	1500	1567	1833	1900	196
10	1556	1630	1704	1778	1852	2148	2222	229
11	1833	1915	1996	2078	2159	2485	2567	2648
12	-2133	2222	2311	2400	2489	2844 3226	2933 3322	302
13	2456	2552 2904	2648 3007	2744 3111	2841 3215	3630	3733	383
14 15	2800 3167	3278	3389	3500	3611	4056	4167	427
16	3556	3674	3793	3911	4030	4504	4622	474
17	3967	4093	4219	4344	4470	4974	5100	522
18	4400	4533	4667	4800	4933	5467	5600	573
19	4856	4996	5137	5278	5419	5981	6122	626
20	5333	5481	5630	5778	5926	6519	6667	681
21	5833	5989	6144 6681	6300 6844	6456	7078 7659	7233 7822	738
22 23	6356 6900	6519 7070	7241	7411	7581	8263	8433	850
24	7467	7644	7822	8000	8178	8889	9067	914
25	8056	8241	8426	8611	8796	9537	9722	980
25 26	8667	8859	9052	9244	9437	10207	10400	1059
27	9300	9500	9700	9900	10100	10900	11100	1130
28	9956	10163	10370	10578	10785	11615	11822	1203
29 30	10633 11333	10848 11556	11063	11278 12000	11493 12222	12352 13111	12567 13333	1278 1355
31	12056	12285	12515	12744	12974	13893	14122	1435
32	12800	13037	13974	13511	13748	14696	14933	1517
33	13567	13811	14056	14300	14544	15522	15767 16622	1601
34	14356	14607	14859	15111	15363	16370	16622	1687
35	15167	15426	15685	15944	16204	16370 17241	17500	1775
36	16000	16267	16533	16800	17067	18133	18400	1866
37 38	16856 17733	17130 18015	17404 18296	17678 18578	17952 18859	19048 19985	19322 20267	1959
39	18633	18922	19211	19500	19789	20944	21233	2152
40	19556	19852	20148	20444	20741	21926	22222	2251
41	20500	20804	21107	21411	21715	22930	23233	2353
42	21467	21778	22089	22400	22711	23956	24267	2457
43 44	22456 23467	22774 23793	23093	23411 21444	23730	25004 26074	25322 26400	2564
45	24500	24833	24119 25167	25500	24770 25833	27167	27500	2783
46	25556	25896	26237	26578	26919	28281	28622	2896
47	26633	26981	27330	27678	28026	29419	29767	3011
48	27733 28856	28089	28444 29581	98800	29156	30578 31759	30933	3128
49	28856	29219	29581	29944	30307	31759	32122	3248
50 .	30000	30370	30741	31111	31481	32963	33333	3370
51 52	31167 32356	31544 32741	31922 33126	32300 33511	32678 33896	34189 35437	34567 35822	3494
53	33567	33959	34352	34744	35137	36707	37100	3749
54	34800	35200	35600	36000	36400	38000	38400	3880
55	36056	36463	36870	37278	37685	39315	39722	4013
56	37333	37748	38163	38578	38993	40652	41067	4148
57	38633	39056	39478	39900	40322	42011	42433	4285
58 59	39956	40385	40815	41244	41674	43393	43822	4425
204	41300	41737	42174	42611	43048	44796	45233	4567

TABLE XV.—CUBIC YARDS IN 100 FEET LENGTH.

Area. Sq.	Cubic Yards.	Area. Sq.	Cubic Yards.	Area.	Cubic Yards.	Area. Sq. Ft.	Cubic Yards.	Area. Sq.	Cubic Yards.
Ft.	TO CHEE	Ft.		Ft.	E TE B	Ft.		Ft.	
1	3.7	51	188.9	101	374.1	151	559.3	201	744.4
2	7.4	52	192.6	102	377.8	152	563.0	202	748.2
3	11.1	53	196.3	103	381.5	153	566.7	203	. 751.9
4	14.8	54	200.0	104	385.2	154	570.4	204	755.6
5	18.5	55	203.7	105	388.9	155	574.1	205	759.3
6	22.2	56	207.4	106	392.6	156	577.8	206	763.0
7	25.9	57	211.1	107	396.3	157	581.5	207	766.7
8 9	29.6	58 59	214.8	108	400.0	158 159	585.2 588.9	208	770.4
10	37.0	60	222.2	110	407.4	160	592.6	210	774.1
11	40.7	61	225.9	111	411.1	161	596.3	211	781.5
12	44.4	62	229.6	112	414.8	162	600.0	212	785.2
13	48.1	63	233.3	113	418.5	163	603.7	213	788.9
14	51.9	64	237.0	114	422.2	164	607.4	214	792.6
15	55.6	65	240.7	115	425.9	165	611.1	215	796.3
16	59.3	66	244.4	116	429.6	166	614 8	216	800.0
17	63.0	67	248.2	117	433.3	167	618.5	217	803.7
18 19	66.7	68	251.9	118	437.0	168	622.2	218	807.4
20	74.1	70	255.6 259.3	120	444.4	170	625.9	219	811.1
21	77.8	71	263.0	121	448.2	171	633.3	221	818.5
22	81.5	72	266.7	122	451.9	172	637.0	222	822.2
23	85.2	73	270.4	123	455.6	173	640.7	223	825.9
24	88.9	74	274.1	124	459.3	174	644.4	224	829.6
25	92.6	75	277.8	125	463.0	175	648.2	225	833.3
26	96.3	76	281.5	126	466.7	176	651.9	226	837.0
27	100.0	77	285 2	127	470.4	177	655.6	227	840.7
28 29	103.7	78 79	288.9	128 129	474 1 477.8	178	659.3	228	844.4
30	107.4	80	292.6	130	481.5	179	663.0	230	851.9
31	114.8	81	300.0	131	485.2	181	670.4	231	855.6
32	118.5	82	303.7	132	488 9	182	674.1	232	859.3
33	122.2	83	307.4	133	492.6	183	677.8	233	863.0
34	125.9	84	311.1	134	496.3	184	681.5	234	866.7
35	129 6	85	314.8	135	500.0	185	685.2	235	870.4
36	133.3	86	318.5	136	503.7	186	688.9	236	874.1
37	137.0	87	322.2	137	507.4	187	692.6	237	877.8
38	140.7	88	325.9 329.6	138	511.1 514.8	188 189	696.3	238	881.5
40	148.2	90	333.3	140	518.5	190	703.7	240	888.9
41	151.9	91	337.0	141	522.2	191	707.4	241	892.6
42	155.6	92	340.7	142	525.9	192	711.1	242	896.3
43	159.3	93	344.4	143	529.6	193	714.8	243	900.0
44	163.0	94	348.2	144	533.3	194	718.5	244	903.7
45	166.7	95	351.9	145	537.0	195	722.2	245	907.4
46	170.4	96	355.6	146	540.7	196	725.9	246	911.1
47	174.1	97	359.3 363.0	147	544.4 548.2	197	729.6	247	914.8
49	181.5	99	366.7	149	551.9	199	737.0	249	922.2
50	185.2	100	370.4	150	555.6	200	740.7	250	925.9

TABLE XV.—CUBIC YARDS IN 100 FEET LENGTH.

Area. Sq. Ft.	Cubic Yards.	Area. Sq. Ft.	Cubic Yards.	Area. Sq. Ft.	Cubic Yards.	Area. Sq. Ft.	Cubic Yards.	Area. Sq. Ft.	Cubic Yards.
251	929.6	301	1114.8	351	1300.0	401	1485.2	451	1670.4
252	933.3	302	1118.5	352	1303.7	402	1488.9	452	1674.1
253	937.0	303	1122.2	353	1307.4	403	1492.6	453	1677.8
254	940.7	304	1125.9	354	1311.1	404	1496.3	454	1681.5
255	944.4	305	1129.6	355	1314.8	405	1500.0	455	1685.2
256	948.2	306	1133.3	356	1318.5	406	1503.7	456	1688.9
257	951.9	307	1137.0	357	1322.2	407	1507.4	457	1692.6
258	955.6	308	1140.7	358	1325.9	408	1511.1	458	1696.3
259	959.3	309	1144.4	359	1329.6	409	1514.8	459	1700.0
260	963.0	310	1148.2	360	1333.3	410	1518.5	460	1703.7
261	966.7	311	1151.9	361	1337.0 1340.7	411	1522.2	461	1707.4
262	970.4 974.1	313	1155.6 1159.3	363	1344.4	412	1525.9 1529.6	462	1711.1
263 264	977.8	314	1163.0	364	1348.2	414	1533.3	464	1714.8 1718.5
265	981.5	315	1166.7	365	1351.9	415	1537.0	465	1722.2
266	985.2	316	1170.4	366	1355.6	416	1540.7	466	1725.9
267	988.9	317	1174.1	367	1359.3	417	1544.4	467	1729.6
268	992.6	318	1177.8	368	1363.0	418	1548.2	468	1733.3
269	996.3	319	1181.5	369	1366.7	419	1551.9	469	1737.0
270	1000.0	320	1185.2	370	1370.4	420	1555.6	470	1740.7
271	1003.7	321	1188.9	371	1374.1	421	1559.3	471	1744.4
272	1007.4	322	1192.6	372	1377.8	422	1563.0	472	1748.2
273	1011.1	323	1196.3	373	1381.5	423	1566.7	473	1751.9
274	1014.8	324	1200.0	374	1385.2	424	1570.4	474	1755.6
275	1018.5	325	1203.7	375	1388.9	425	1574.1	475	1759.3
276 277	1022.2	326 327	1207.4	376	1392.6	426	1577.8	476	1763.0
278	1025.9	328	1214.8	378	1400.0	427	1581.5 1585.2	477	1766.7
279	1033.3	329	1218.5	379	1403.7	429	1588.9	479	1770.4 1774.1
280	1037.0	330	1222.2	380	1407.4	430	1592.6	480	1777.8
281	1040.7	331	1225.9	381	1411.1	431	1596.3	481	1781.5
282	1044.4	332	1229.6	382	1414.8	432	1600.0	482	1785.2
283	1048.2	333	1233.3	383	1418.5	433	1603.7	483	1788.9
284	1051.9	334	1237.0	384	1422.2	434	1607.4	484	1792.6
285	1055.6	335	1240.7	385	1425.9	4:35	1611.1	485	1796.3
286	1059.3	336	1244.4	386	1429.6	436	1614.8	486	1800.0
287	1063.0	337	1248.2	387	1433.3	437	1618.5	487	1803.7
288	1066.7	338	1251.9	388	1437.0	438	1622.2	488	1807.4
289	1070.4	339	1255.6	389	1440.7	439	1625.9	489	1811.1
290	1074.1	340	1259.3	390 391	1444.4	440	1629.6	490	1814.8
291 292	1081.5	342	1263.0 1266.7	392	1448.2	441	1633.3	491	1818.5
293	1085.2	343	1270.4	393	1451.9	442	1637.0	492	1822.2
294	1088.9	344	1274.1	394	1459.3	444	1644.4	493	1825.9 1829.6
295	1092.6	345	1277.8	395	1463.0	445	1648.2	494	1833.3
296	1096.3	346	1281.5	396	1466.7	446	1651.9	496	1837.0
297	1100.0	347	1285.2	397	1470.4	447	1655.6	497	1840.7
298	1103.7	348	1288.9	398	1474.1	448	1659.3	498	1844.4
299	1107.4	349	1292.6	399	1477.8	449	1663.0	499	1818.2
300	1111.1	350	1296.3	400	1481.5	450	1666.7	500	1851.9

TABLE XV.—CUBIC YARDS IN 100 FEET LENGTH.

Area. Sq. Ft.	Cubic Yards.								
501	1855.6	551	2040.7	601	2225.9	651	2411.1	701	2596.3
502	1859.3	552	2044.4	602	2229.6	652	2414.8	702	2600.0
503	1863.0	553	2048.2	603	2233.3	653	2418.5	703	2603.7
504	1866.7	554	2051.9	604	2237.0	654	2422.2	704	2607.4
505	1870.4	555	2055.6	605	2240.7	655	2425.9	705	2611.1
506	1874.1	556	2059.3	606	2244.4	656	2429.6	706	2614.8
507	1877.8	557	2063.0	607	2248.2	657	2433.3	707	2618.5
508	1881.5	558	2066.7	608	2251.9	658	2437.0	708	2622.2
509	1885.2	559	2070.4	609	2255.6	659	2440.7	709	2625.9
510	1888.9	560	2074.1	610	2259.3	660	2444.4	710	2629.6
511	1892.6	561	2077.8	611	2263.0	661	2448.2	711	2633.3
512	1896.3	562	2081.5	612	2266.7	662	2451.9	712	2637.0
513	1900.0	563	2085.2	613	2270.4	663	2455.6	713	2640.7
514	1903.7	564	2088.9	614	2274.1	664	2459.3	714	2644.4
515	1907.4	565	2092.6	615	2277.8	665	2463.0	715	2648.2
516	1911.1	566	2096.3	616	2281.5	666	2466.7	716	2651.9
517	1914.8	567	2100.0	617	2285.2	667	2470.4	717	2655.6
518	1918.5	568	2103.7	618	2288.9	668	2474.1	718	2659.3
519	1922.2	569	2107.4	619	2292.6	669	2477.8	719	2663.0
520	1925.9	570	2111.1	620	2296.3	670	2481.5	720	2666.7
521	1929 6	571	2114.8	621	2300.0	671	2485.2	721	2670.4
522	1933.3	572	2118.5	622	2303.7	672	2488.9	722	2674.1
523	1937.0	573	2122.2	623	2307.4	673	2492.6	723	2677.8
524	1940.7	574	2125.9	624	2311.1	674	2496.3	724	2681.5
525	1944.4	575	2129.6 2133.3	625	2314.8 2318.5	675	2500.0 2503.7	725	2685.2
526	1948.2	576	2137.0	627	2322.2	677	2507.4	726	2688.9
527	1951.9 1955.6	578	2140.7	628	2325.9	678	2511.1	728	2692.6 2696.3
528 529	1959.3	579	2144.4	629	2329.6	679	2511.1	729	2700.0
530	1963.0	580	2148 2	630	2333.3	680	2518.5	730	2703.7
531	1966.7	581	2151.9	631	2337.0	681	2522.2	731	2707.4
532	1970.4	582	2155.6	632	2340.7	682	2525.9	732	2711.1
533	1974.1	583	2159.3	633	2344.4	683	2529.6	733	2714.8
534	1977.8	584	2163.0	634	2348.2	684	2533.3	734	2718.5
535	1981.5	585	2166.7	635	2351.9	685	2537.0	735	2722.2
536	1985.2	586	2170,4	636	2355.6	686	2540 7	736	2725.9
537	1988.9	587	2174.1	637	2359.3	687	2544.4	737	2729.6
538	1992.6	588	2177.8	638	2363 0	688	2548.2	738	2733.3
539	1996.3	589	2181.5	639	2366.7	689	2551.9	739	2737.0
540	2000.0	590	2185.2	640	2370.4	690	2555.6	740	2740.7
541	2003.7	591	2188.9	641	2374.1	691	2559.3	741	2744.4
542	2007.4	592	2192.6	642	2377.8	692	2563.0	742	2748.2
543	2011.1	593	2196.3	643	2381.5	693	2566.7	743	2751.9
544	2014.8	594	2200.0	644	2385.2	694	2570.4	744	2755.6
545	2018.5	595	2203.7	645	2388.9	695	2574.1	745	2759.3
546	2022.2	596	2207.4	646	2392.6	696	2577.8	746	2763.0
547	2025.9	597	2211.1	647	2396.3	697	2581.5	747	2766.7
548	2029.6	598	2214.8	648	2400.0	698	2585.2	748	2770.4
549	2033.3	599	2218.5	649	2403.7	699	2588.9	749	2774.1
550	2037.0	600	2222.2	650	2407.4	700	2592.6	100	2777.8

TABLE XV.-CUBIC YARDS IN 100 FEET LENGTH.

Area.	Cubic	Area.	Cubic	Area. Sq.	Cubic	Area. Sq.	Cubic	Area. Sq.	Cubic
Ft.	Yards.	Sq. Ft.	Yards.	Ft.	Yards.	Ft.	Yards.	Ft.	Yards.
751	2781.5	801	2966.7	851	3151.9	901	3337.0	951	3522.2
752	2785.2	802	2970.4	852	3155.6	902	3340.7	952	3525.9
753	2788.9	803	2974.1	853	3159.3	903	3344.4	953	3529.6
754	2792.6	804	2977.8	854	3163.0	904	3348.2	954	3533.3
755	2796.3	805	2981.5	855	3166.7	905	3351.9	955	3537.0
756	2800.0	806	2985.2	856	3170.4	906	3355.6	956	3540.7
757	2803.7	807	2988.9	857	3174.1	907	3359.3	957	3544.4
758	2807.4	808	2992.6	858	3177.8	908	3363.0	958	3548.2
759	2811.1	809	2996.3	859	3181.5	909	3366.7	959	3551.9
760	2814.8	810	3000.0	860	3185.2	910	3370.4	960	3555.6
761	2818.5	811	3003.7	861	3188.9	911	3374.1	961	3559.3
762	2822.2	812	3007.4	862	3192.6	912	3377.8	962	3563.0
763	2825.9	813	3011.1	863	3196.3	913	3381.5	963	3566.7
764	2829.6	814	3014.8	864	3200.0	914	3385.2	964	3570.4
765	2833 3	815	3018.5	865	3203.7	915	3388.9	965	3574.1
766	2837.0	816	3022.2	866	3207.4	916	3392.6	966	3577.8
767	2840.7	817	3025.9	867	3211.1	917	3396.3	967	3581.5
768	2844.4	818	3029.6	868	3214.8	918	3400.0	968	3585.2
769	2848.2	819	3033.3	869	3218.5	919	3403.7	969	3588.9
770	2851.9	820	3037.0	870	3222.2	920	3407.4	970	3592.6
771	2855.6	821	3040.7	871	3225.9	921	3411.1	971	3596.3
772	2859.3	822	3044.4	872	3229.6	922	3414.8	972	3600.0
773	2863.0	823	3048.2	873	3233.3	923	3418.5	973	3603.7
774	2866.7	824	3051.9	874	3237.0	924	3422.2	974	3607.4
775	2870.4	825	3055.6	875	3240.7	925	3425.9	975	3611.1
776	2874.1	826	3059.3	876	3244.4	926	3429.6	976	3614.8
777	2877.8	827	3063.0	877	3248.2	927	3433.3	977	3618.5
778	2881.5	828	3066.7	878	3251.9	928	3437.0	978	3622.2
779	2885.2	829	3070.4	879	3255.6	929	3440.7	979	3625.9
780 781	2888.9 2892.6	830	3074.1	880	3259.3	930	3444.4	980	3629.6
782	2896.3	831 832	3077.8 3081.5	881 882	3263.0 3266.7	931	3448.2	981 982	3633.3
783	2900.0	833	3085.2	883	3270.4	932 933	3451.9 3455.6	983	3637.0
784	2903.7	834	3088.9	884	3274.1	934	3459.3	984	3640.7
785	2907.4	835	3092.6	885	3277.8	935	3463.0	985	3644.4 3648.2
786	2911.1	836	3096.3	886	3281.5	936	3466.7	986	3651.9
787	2914.8	837	3100.0	887	3285.2	937	3470.4	987	3655.6
788	2918.5	838	3103.7	888	3288.9	938	3474.1	988	3659.3
789	2922.2	839	3107.4	889	3292.6	939	3477.8	989	3663.0
790	2925.9	840	3111.1	890	3296.3	940	3481.5	990	3666.7
791	2929.6	841	3114.8	891	3300.0	941	3485.2	991	3670.4
792	2933.3	842	3118.5	892	3303.7	942	3488.9	992	3674.1
793	2937.0	843	3122.2	893	3307.4	943	3492.6	993	3677.8
794	2940.7	844	3125.9	894	3311.1	944	3496.3	994	3681.5
795	2914.4	845	3129.6	895	3314.8	945	3500.0	995	3685.2
796	2948.2	846	3133.3	896	3318.5	946	3503.7	996	3688.9
797	2951.9	847	3137.0	897	3322.2	947	3507.4	997	3692.6
798	2955.6	848	3140.7	898	3325.9	948	3511.1	998	3696.3
799	2959.3	849	3144.4	899	3329.6	949	3514.8	999	3700.0
800	2963.0	850	3148.2	900	3333.3	950	3518.5	1000	3703.7

Tins. O		C	CONVE	RSION	OF EN	GLISH	INCH	ES INT	O CE	NTIMI	ETRES	
0 0.000 2.540 5.080 7.620 10.16 12.70 15.24 17.78 20.32 22.86 20 55.40 27.94 30.48 30.28 35.6 88.10 40.64 48.18 45.72 44.26 20 50.50 53.34 55.88 58.42 60.96 63.50 66.04 68.58 71.12 73.66 40 101.60 104.14 106.68 109.22 111.76 114.80 116.84 119.88 121.02 124.46 50 127.70 129.54 132.08 134.62 137.76 113.90 114.9 9.89 65.52 90.66 60 152.40 154.94 157.48 160.02 162.56 165.10 167.64 170.18 172.72 175.26 60 152.40 154.94 157.48 160.02 162.56 165.10 167.64 170.18 172.72 175.26 70 127.75 180 180.34 182.88 185.42 187.90 190.50 193.04 105.58 198.12 20.96 80 223.30 205.74 208.28 210.82 213.86 215.00 218.44 220.98 223.52 235.60 231.14 233.08 230.52 233.76 241.30 243.84 240.28 223.52 235.46 100 256.40 256.44 250.08 261.02 264.10 256.44 250.08 261.02 264.10 256.44 250.08 256.44 250.08 261.02 264.10 256.44 24.50 08 264.25 08 261.02 264.10 256.44 24.50 08 265.45 250.08 261.02 264.10 256.44 250.08 256.45 250.08 261.02 264.10 256.44 250.08 256.44 250.08 265.45 250.08 261.02 264.10 256.44 250.08 265.45 250.08 261.02 264.10 256.45 250.08 261.02 264.10 256.45 250.08 261.02 264.10 256.45 250.08 261.02 264.10 256.45 250.08 261.02 264.10 256.45 250.08 261.02 264.10 256.45 250.08 261.02 264.10 256.45 250.08 261.02 264.10 256.45 250.08 261.08 260.0		Ins.	0	1	2	3	4	5	6	7	8	9
10	ı			Cm.								
20	1			2.540	5.080	7.620	10.16	12.70	15.24	17.78		
30	i		25.40						40.64	43.18	45.72	
10	П				55.88	58.42	60.96	63.50	66.04			
10	ı		76.20	78.74	81.28		86.36	88.90	91.44			
10	H		107.00	100 54	100.08		111.70	114.30	116.84	119.38	121.92	124.40
10	ı			154 04	157 48		160 56	185 10	167 64	144.70	100 00	105 06
80 203.20 205.74 208.28 210.82 213.36 215.90 218.44 220.98 228.52 226.06 201.14 233.68 236.92 238.576 241.30 243.84 246.85 284.25 251.46 206.70 269.24 271.78 274.82 276.85 CONVERSION OF CENTIMETRES INTO ENGLISH INCHES. Cm. 0 1 2 3 4 5 6 7 8 9 Ins. Ins. Ins. Ins. Ins. Ins. Ins. Ins.	ı		177 80	180 34	182 88		187 96	190.50	193 04	195 58	198 19	200 96
90			203.20	205.74	208.28							
CONVERSION OF CENTIMETRES INTO ENGLISH INCHES. CONVERSION OF ENGLISH FEET INTO ENGLISH INCHES. CONVERSION OF ENGLISH FEET INTO ENGLISH FEET. CONVERSION OF METRES INTO ENGLISH FEET. CONVERSION OF METALS CON	H						238.76					
Cm. O		100	254.00	256.54	259.08	261.62						
Ins.		C	ONVE	RSION	OF CE	NTIME	TRES	INTO I	ENGLI	SH II	NCHES	3.
O	-	Cm.	0	1	2	3	4	5	6	7	8.	9
O	1	9.70	Ins	Ins	Ing	Ine	Ine	Inc	Inc	Inc	Ing	Inc
10		0					1.575					
20	1				4.742	5.118	5.512			6.693	7.087	
30	L	20	7.874	8.268	8.662	9.055	9.449	9.843	10.236	10,630	11.024	11,418
40	I		11.811		12.599	12.992	13.386	13.780	14.173	14.567	14.961	15.355
60 23.622 24.016 24.410 24.804 25.197 25.591 25.982 26.387 26.772 27.166 70 27.560 27.953 28.347 28.741 29.134 29.528 29.922 30.316 30.709 31.108 80 31.497 31.390 32.284 32.678 33.071 33.465 38.393 34.253 34.666 35.040 90 35.434 35.827 36.221 36.615 37.009 37.402 37.796 38.109 38.583 38.977 100 39.370 39.764 40.158 40.552 40.945 41.339 41.733 42.126 42.520 42.914 CONVERSION OF ENGLISH FEET INTO METRES. Feet. 0 1 2 3 4 5 6 7 8 9 Met. Met. Met. Met. Met. Met. Met. Met.	1		15.748	16.142	16.536	16.929	17.323	17.717	18.111	18.504	18.898	19.292
Tol. 27.560 27.953 28.347 28.741 29.134 29.528 29.922 30.316 30.700 31.108 80 31.497 31.890 32.284 32.678 33.071 33.465 33.859 34.253 34.646 35.040 90 35.434 35.827 36.221 36.615 37.009 37.402 37.796 38.190 38.583 38.977 100 39.370 39.764 40.158 40.552 40.945 41.339 41.733 42.126 42.520 42.914	1		19.000		20.473	20.867	21.260					
Section Sect	1											
90	ı											
Teet. O	H											
Feet. 0 1 2 3 4 5 6 7 8 9 Met.	I											
Met.			COL	NVERS:	ION OF	ENG	LISH F	EET I	NTO I	METRI	ES.	
0 0.000 0.3048 0.6096 0.9144 1.2192 1.5289 1.8287 2.1385 2.4888 2.7481 20 6.0859 6.4006 6.7055 7.0102 7.3150 7.6198 7.9246 8.2204 8.5342 8.830 30 9.1438 9.4486 9.7534 10.088 10.363 10.668 10.972 11.277 11.582 11.887 40 12.192 12.496 12.801 13.106 13.411 13.716 14.020 14.325 14.630 14.935 50 15.239 15.544 15.849 16.154 16.459 16.763 17.068 17.373 17.678 17.986 60 18.287 18.592 18.897 19.202 19.507 19.811 20.116 20.421 20.726 21.031 70 21.335 21.640 21.945 22.250 22.555 22.859 23.164 23.409 23.774 24.078 90 27.431 27.736 28.041 28.346 28.651 28.955 29.260 29.565 29.870 20.174 100 30.479 30.784 31.089 31.394 31.698 32.008 32.308 32.613 32.918 33.222 CONVERSION OF METRES INTO ENGLISH FEET. Met.		Feet.	0	1	2	3	4	5	6	7	8	9
0 0.000 0.3048 0.6096 0.9144 1.2192 1.5289 1.8287 2.1385 2.4888 2.7481 20 6.0859 6.4006 6.7055 7.0102 7.3150 7.6198 7.9246 8.2204 8.5342 8.830 30 9.1438 9.4486 9.7534 10.088 10.363 10.668 10.972 11.277 11.582 11.887 40 12.192 12.496 12.801 13.106 13.411 13.716 14.020 14.325 14.630 14.935 50 15.239 15.544 15.849 16.154 16.459 16.763 17.068 17.373 17.678 17.986 60 18.287 18.592 18.897 19.202 19.507 19.811 20.116 20.421 20.726 21.031 70 21.335 21.640 21.945 22.250 22.555 22.859 23.164 23.409 23.774 24.078 90 27.431 27.736 28.041 28.346 28.651 28.955 29.260 29.565 29.870 20.174 100 30.479 30.784 31.089 31.394 31.698 32.008 32.308 32.613 32.918 33.222 CONVERSION OF METRES INTO ENGLISH FEET. Met.	1	SELVE	Mot	Mot	Mot	Mot	Mot	Mot	Mat	Mat	Mot	Mot
10	1	0	0 000		0 6096		1 9199	1 5989				
30 9,1438 9,4486 9,7534 10,068 10,363 10,668 10,972 11,277 11,582 11,852 11,552 11,852 11,852 11,552 11,852 11,852 11,552 11,852 11,852 11,552 11,852 11,552 11,852 11,552 11,552 11,852 11,55			3.0479		3.6575	3.9623	4.2671	4 5710	1 8767	5 1815	5 4862	5 7011
30 9,1438 9,4486 9,7534 10,068 10,363 10,668 10,972 11,277 11,582 11,852 11,552 11,852 11,852 11,552 11,852 11,852 11,552 11,852 11,852 11,552 11,852 11,552 11,852 11,552 11,552 11,852 11,55	1	20			6.7055	7.0102	7.3150	7.6198	7.9246	8.2294	8.5342	8.8390
50	1		9.1438	9.4486	9.7534	10.058	10.363	10.668	10.972	11.277	11.582	11.887
60 18.287 18.592 18.897 19.202 19.507 19.811 20.116 20.421 20.726 21.036 21.305 21.640 21.945 22.250 22.555 22.859 23.164 23.469 23.774 24.079 80 24.383 24.688 24.993 25.298 25.5602 25.5907 26.212 26.517 26.822 27.126 90 27.481 27.736 28.041 28.346 28.651 28.955 29.290 29.565 29.870 30.174 100 30.479 30.784 31.089 31.394 31.698 32.003 32.308 32.613 32.918 33.222	1		12.192	12.496		13.106		13.716	14.020	14.325	14.630	14.935
Tol. 21, 335 21, 640 21, 945 22, 250 22, 555 22, 859 23, 164 23, 469 23, 774 24, 079 90 27, 431 27, 736 28, 041 28, 346 28, 651 28, 955 29, 260 29, 565 29, 870 30, 174 100 30, 479 30, 784 31, 089 31, 394 31, 698 32, 003 32, 308 32, 613 32, 918 33, 232	1		15.239	10.544	15.849	16.104	10.459	10.763	17.008	17.373	17.078	17.983
80	1							99 850	93 164	93 460	93 774	24 070
90	1											
Met. O	1			27,736	28.041	28.346	28,651	28.955	29.260	29.565	29.870	30.174
Met. 0 1 2 3 4 5 6 7 8 9 0 0.000 3.2809 6.5618 9.8427 13.123 16.404 19.685 22.966 26.247 29.528 10 32.809 36.090 39.371 42.651 45.932 49.213 52.496 26.247 29.528 20 65.618 68.899 72.179 75.461 78.741 82.022 85.303 88.584 91.865 95.514 40 131.24 134.52 137.80 141.08 144.63 147.64 150.92 154.20 157.48 160.76 50 164.04 167.33 170.61 173.89 177.17 180.45 188.73 187.01 190.29 185.30 60 196.85 200.13 203.42 206.70 209.98 213.26 216.24 219.82 223.10 226.38 70 229.66 232.47 236.22 239.51 242.79 246.	1			30.784			31.698	32.003	32.308	32.613	32.918	33.222
Feet. Feet	-		COL	NVERS	ION OF	F MET	RES IN	TO E	NGLIS	H FE	ET.	PART
0 0 0 3,2809 6,5618 9,8427 18,123 16,40119,685 22,966 26,247(29,528 10 32,809 36,000 39,371 42,651 45,932 49,218 52,494 55,775 59 66 28,387 20 65,618 68,899 72,179 75,461 78,741 82,022 85,303 88,584 91,865 95,146 30 98,427 101,71 104,99 108,27 111,55 114,83 118,11 121,39 124,67 127,64 40 131,24 134,52 137,80 141,08 114,64 36 17,64 150,92 154,20 157,48 160,76 50 164,04 167,33 170,61 178,89 177,17 180,45 183,73 187,01 190,29 198,52 211,17 180,45 183,73 187,01 190,29 198,52 211,17 180,45 183,73 187,01 190,29 198,25 23,18 26,12 290,60 290,98 213,26 249,35 236,28 285		Met.	0	1	2	3	4	5	6	7	8	9
0 0 0 3,2809 6,5618 9,8427 18,123 16,40119,685 22,966 26,247(29,528 10 32,809 36,000 39,371 42,651 45,932 49,218 52,494 55,775 59 66 28,387 20 65,618 68,899 72,179 75,461 78,741 82,022 85,303 88,584 91,865 95,146 30 98,427 101,71 104,99 108,27 111,55 114,83 118,11 121,39 124,67 127,64 40 131,24 134,52 137,80 141,08 114,64 36 17,64 150,92 154,20 157,48 160,76 50 164,04 167,33 170,61 178,89 177,17 180,45 183,73 187,01 190,29 198,52 211,17 180,45 183,73 187,01 190,29 198,52 211,17 180,45 183,73 187,01 190,29 198,25 23,18 26,12 290,60 290,98 213,26 249,35 236,28 285	1		Feet									
10 32,809 36,090 39,371 42,651 45,932 49,213,52,494,55,775,59,056,62,337 066,62,337 065,618 68,899 72,179 75,461 78,741 82,022 85,303 88,584 91,865,95,146 38,427 101,71 104,99 108,27 111,55 114,83 118,11 121,39 124,67 127,96 40 131,24 134,52 137,80 141,08 147,64 150,92 154,20 157,48 160,76 50 164,04 167,33 170,61 173,89 177,17 180,45 187,01 190,219,35 193,59 193,57 193,57 193,59 193,57 193,57 193,52 193,59 <th>-</th> <td>0</td> <td>0.000</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td>	-	0	0.000									
20	1	10	32.809	36.090	39.371	42 651	45.932	49.213	52.494	55.775	59.056	62:337
50 164.04 167.33 170 61 173.89 177.17 180.45 183.73 187.01 190.29 193.57 60 196.85 200.13 203.42 206.70 209.98 213.66 215.42 19.82 223.10 226.38 70 229.66 232.94 236.22 239.51 242.79 246.07 249.85 232.63 255.91 235.19 80 262.47 265.75 269.03 272.81 275.60 278.88 282.16 285.44 288.72 292.00 295.28 298.56 391.84 305.12 308.40 311.69 314.97 318.25 321.53 324.81	1	20		68.899	72 179	75.461	78.741	82.022	85.303	88.584	91.865	95.146
50 164.04 167.33 170 61 173.89 177.17 180.45 183.73 187.01 190.29 193.57 60 196.85 200.13 203.42 206.70 209.98 213.66 215.42 19.82 223.10 226.38 70 229.66 232.94 236.22 239.51 242.79 246.07 249.85 232.63 255.91 235.19 80 262.47 265.75 269.03 272.81 275.60 278.88 282.16 285.44 288.72 292.00 295.28 298.56 391.84 305.12 308.40 311.69 314.97 318.25 321.53 324.81	1		98.427	101.71	104.99	108.27	111.55	114 83	118.11	121.39	124.67	127.96
60 196.83 200.13 203.42 206.70 209.98 213.26 216.54 219.82 223.10 226.38 70 229.66 232.94 236.22 239.51 242.79 246.07 249.35 252.63 252.91 259.19 80 262.47 265.75 269.03 278.31 275.60 278.88 282.16 285.44 288 72 292.00 295.28 298.56 391.84 305.12 308.40 311.69 314.97 318.25 321.53 324.81	1	40	131.24	134.52	137.80	141.08	144.36	147.64	150 92	154,20	100.90	100.76
70 229.66 232.94 236.22 239.51 242.79 246.07 249.35 252 63 255.91 259.19 80 262.47 265.75 269.03 278.81 275.60 278.88 282.16 285.44 285.23 232.00 295.28 298.56 391.84 305.12 308.40 311.69 314.97 318.25 321.53 324.81	1		104.04	200 19	202 40	206 70	200 00	213 96	216 54	210 89	223 10	226 38
80 262.47 265.75 269.03 272.31 275.60 278.88 282.16 285.44 288.72 292.00 -90 295.28 298.56 391.84 305.12 308.40 311.69 314.97 318.25 321.53 324.81	1		229 66	232 94	236.22	239 51	242.79	246.07	249.35	252 63	255.91	259.19
90 295.28 298.56 391.84 305.12 308.40 311.69 314.97 318.25 321.53 324.81	1				269.03	272.31	275.60	278.88	282.16	285.44	288 72	292.00
	1	90	295.28	298.56	391.84	305.12	308.40	311.69	314.97	318.25	321.53	324.81
	1	100		331.37	334.65	337.93	341.21	344.49	347.78	351.06	354.34	357.62

TABLE XVII.

Miles.	0	1	2	3	4	5	6	7	8	9
	Kilo.	Kilo.	Vilo	Kilo.	Kilo.	Kilo.	Kilo.	Kilo.	Kilo.	Kild
0				4.8279					12.8745	
10				20.921		24.139	25.749	27.358		30.5
20				37.014		40.232				
30				53.107		56,325	57.935			
40					70.809					
50				85.293						
60					102.99					
70					119.08					
80				133.57						
90					151.26					
100					167.35					
Kilom.	0	1	2	3	4	5	6	7	8	9
N. Albander	9.5723	Miles	Miles	Miles	Miles.	Miles.	Miles,	Miles.	Miles.	Mile
3 % -										
0			1 2427	1 8641						
0 10	0.0000	0.6214							11,185	
10	0.0000 6.2138	0.6214 6.8352	7.4565	8.0780	8.6994	9.3208	9.9421	10.562		
	0.0000 6.2138 12.427	0.6214 6.8352 13.049	7.4565 13 670		8.6994 14.913	9.3208 15.534	9.9421 16.156	10.562 16.776	17.399	18.
10 20	0.0000 6.2138 12.427 18.641	0.6214 6.8352 13.049 19.263	7.4565 13 670 19.884	8.0780 14.292	8.6994 14.913 21.127	9.3208 15.534	9.9421 16.156 23 370	10.562 16.776 22.990	17.399 23.613	18. 3 24.
10 20 30	0.0000 6.2138 12.427 18.641 24.855	0.6214 6.8352 13.049 19.263 25.477	7.4565 13 670 19.884 26.098	8.0780 14.292 20.506 26.720	8.6994 14.913 21.127	9.3208 15.534 21.748 27.962	9.9421 16.156 23 370 28.584	10.562 16.776 22.990 29.204	17.399 23.613 29.827	18. 324. 30.
10 20 30 40 50 60	0.0000 6.2138 12.427 18.641 24.855 31.069 37.282	0.6214 6.8352 13.049 19.263 25.477 31.690 37.904	7.4565 13 670 19.884 26.098 32.311 38.525	8,0780 14,292 20,506 26,720 32,933 39,147	8.6994 14.913 21.127 27.341 33.554 39.768	9.3208 15.534 21.748 27.962 34.175 40.389	9.9421 16.156 23 370 28.584 34.797 41.011	10.562 16.776 22.990 29.204 35.417 41.631	17.399 23.613 29.827 36.040 42.254	18. 324. 30. 36. 42.
10 20 30 40 50 60 70	0.0000 6.2138 12.427 18.641 24.855 31.069 37.282 43.497	0.6214 6.8352 13.049 19.263 25.477 31.690 27.904 44.118	7.4565 13 670 19.884 26.098 32.311 38.525 44.739	8.0780 14.292 20.506 26.720 32.933 39.147 45.361	8.6994 14.913 21.127 27.341 33.554 39.768 45.982	9.3208 15.534 21.748 27.962 34.175 40.389 46.603	9.9421 16.156 23.370 28.584 34.797 41.011 47.225	10.562 16.776 22.990 29.204 35.417 41.631 47.845	5 17.399 23.613 29.827 36.040 42.254 5 48.468	18. 24. 30. 36. 42. 49.
10 20 30 40 50 60 70 80	0.0000 6.2138 12.427 18.641 24.855 31.069 37.282 43.497 49.711	0.6214 6.8352 13.049 19.263 25.477 31.690 37.904 44.118 50.332	7.4565 13 670 19.884 26.098 32.311 38.525 44.739 50.953	8.0780 14.292 20.506 26.720 32.933 39.147 45.361 51.575	8.6994 14.913 21.127 27.341 33.554 39.768 45.982 52.196	9.3208 15.534 21.748 27.962 34.175 40.389 46.603 52.817	9.9421 16.156 23 370 28.584 34.797 41.011 47.225 53.439	10.562 16.776 22.990 29.204 35.417 41.631 47.845 54.059	17.399 23.613 29.827 36.040 42.254 48.468 9 54.682	18. 24. 30. 36. 42. 42. 49. 55.
10 20 30 40 50 60 70	0.0000 6.2138 12.427 18.641 24.855 31.069 37.282 43.497 49.711 55.924	0.6214 6.8352 13.049 19.263 25.477 31.690 37.904 44.118 50.332 56.545	7.4565 13 670 19.884 26.098 32.311 38.525 44.739 50.953 57.166	8.0780 14.292 20.506 26.720 32.933 39.147 45.361 51.575 57.788	8.6994 14.913 21.127 27.341 33.554 39.768 45.982	9,3208 15,534 21,748 27,962 34,175 40,389 46,603 52,817 59,030	9.9421 16.156 23.370 28.584 34.797 41.011 47.225 53.439 59.652	10.562 16.776 22.990 29.204 35.417 41.631 47.845 54.059 60.272	17.399 23.613 29.827 36.040 42.254 48.468 9 54.682 2 60.895	18. 24. 30. 36. 42. 49. 55. 61.

Lat.	1' Lat.	1' Long.	Lat.	1' Lat.	1' Long.
1°	6045	6085	31°	6061	5222
20	6045	6083	320	6062	5166
30	6045	6078	330	6063	5109
40	6045	6071	340	6064	5051
50	6045	6063	35°	6065	4991
60	6045	6053	36°	6066	4930
70	6046	6041	370	6067	4867
80	6046	6027	380	6068	4802
90	6046	6012	390	6070	4736
10°	6047	5994	40°	6071	4669
110	6047	5975	410	6072	4600
120	6048	5954	420	6073	4530
130	6048	5931	430	6074	4458
140	6049	5907	440	6075	4385
15°	6049	5880	450	6076	4311
160	6050	5852	46°	6077	4235
170	6050	5822	470	6078	4158
180	6051	5790	480	6079	4080
190	6052	5757	490	6080	4001
200	6952	5721	50°	6081	3920
210	6053	5684	51°	6082	3838
220	6(54	5646	520	6084	3755
230	6054	5605	530	6085	3671
240	6055	5563	54°	6086	3586
25°	6056	5519	550	6087	3499
26°	6057	5474	56°	6088	3413
270	6058	5427	570	6089	3323
280	6059	5378	580	6090	3233
290	6060	5327	590	6091	3142
300	6061	5275	600	6092	3051

TABLE XIX.—TO REDUCE MEAN TO SIDEREAL TIME.

Solar	Add	Solar	Add Sec.	Solar	Add	Solar	Add	Solar	Add
Hours.	Min. Sec.	Min.		Min.	Sec.	Sec.	Sec.	Sec.	Sec.
1 2 3 4	0 9.86	1	0.16	31	5.09	1	0.00	31	0.08
	0 19.71	2	0.33	32	5.26	2	0.01	32	0.09
	0 29.57	3	0.49	33	5.42	3	0.01	33	0.09
	0 39.43	4	0.66	34	5.59	4	0.01	34	0.09
5	0 49.28	5	0.82	35	5.75	5 6 7 8	0 01	35	0.10
6	0 59.14	6	0.99	36	5.92		0.02	36	0.10
7	1 9.00	7	1.15	37	6.08		0.02	37	0.10
8	1 18.85	8	1.31	38	6.24		0.02	38	0.10
9	1 28.71	9	1.48	39	6.41	9	0.03	39	0.11
10	1 38.57	10	1.64	40	6.57	10	0.03	40	0.11
11	1 48.42	11	1.81	41	6.74	11	0.03	41	0.11
12	1 58.28	12	1.97	42	6.90	12	0.03	42	0.12
13	2 8.13	13	2.14	43	7.07	13	0.04	43	0.12
14	2 17.99	14	2.30	44	7.23	14	0.04	44	0.12
15	2 27.85	15	2.46	45	7.39	15	0.04	45	0.12
16	2 37.70	16	2.63	46	7.56	16	0.04	46	0.13
17	2 47.56	17	2.79	47	7.72	17	0.05	47	0.13
18	2 57.42	18	2.96	48	7.89	18	0.05	48	0.13
19	3 7.27	19	3.12	49	8.05	19	0.05	49	0.13
20	3 17.13	20	3.29	50	8.22	20	0.06	50	0.14
21	3 26.99	21	3.45	51	8.38	21	0.06	51	0.14
22	3 36.84	22	3.61	52	8.54	22	0.06	52	0.14
23	3 46.70	23	3.78	58	8.71	23	0.06	53	0.15
24	3 56.56	24	3.94	54	8.87	24	0.07	54	0.15
25	4 6.40	25	4.11	55	9.04	25	0.07	55	0.15
26	4 16.26	26	4.27	56	9.20	26	0.07	56	0.15
27	4 26.13	27	4.44	57	9.37	27	0.08	57	0.16
28	4 36.00	28	4.60	58	9.53	28	0.08	58	0.16
29	4 45.86	29	4.76	59	9.69	29	0.08	59	0.16
30	4 55.71	30	4.93	60	9.86	30	0.08	60	0.16

TABLE XIX-Continued .- TO REDUCE SIDEREAL TO MEAN TIME.

1 0 9.83 1 0.16 31 5.08 1 0.00 31 2 0 19.66 2 0.33 32 5.24 2 0.01 33 3 0 29.49 3 0.49 33 5.41 3 0.01 33 4 0 39.32 4 0.66 34 5.57 4 0.01 34 5 0 49.15 5 0.82 35 5.73 5 0.01 34 6 0 58.98 6 0.98 36 5.90 6 0.02 36 7 1 8.14 7 1.15 37 6.06 7 0.02 36 9 1 28.47 9 1.47 39 6.39 9 0.03 39 10 1 38.30 10 1.64 40 6.55 10 0.03 40 11 <th>Sub- tract Sec.</th>	Sub- tract Sec.
2 0 19 66 2 0 .33 32 5.24 2 0 .01 32 3 0 29 49 3 0.49 33 5.41 3 0.01 33 4 0 39.32 4 0.66 34 5.57 4 0.01 34 5 0 49.15 5 0.82 35 5.73 5 0.01 35 6 0 58.89 6 0.98 36 5.90 6 0.02 36 7 1 8.81 7 1.15 37 6.06 7 0.02 37 8 1 18.64 8 1.31 38 6.29 9 0.03 39 10 1 38.30 10 1.64 40 6.55 10 0.03 40 11 1 48.12 11 1.80 41 6.72 11 0.03 42 12 1 57.95 12 1.97 42 6.88 12 0.03	0.08
4 0 39,32 4 0.66 34 5.57 4 0.01 34 5 0 49,15 5 0.82 35 5.73 5 0.01 34 6 0 58,98 6 0.98 36 5.90 6 0.02 36 7 1 8,81 7 1.15 37 6.06 7 0.02 38 8 1 18,64 8 1.31 38 6.23 8 0.02 38 9 1 28,47 9 1.47 39 6.39 9 0.03 39 10 1 38,30 10 1.64 40 6.55 10 0.03 40 11 1 48,12 11 1.80 41 6.72 11 0.03 41 12 1 57.95 12 1.97 42 6.88 12 0.03 42 13 2 7.74 14 1.92 44 7.21 14 0.04	0.09
5 0 49,15 5 0.82 35 5.73 5 0.01 35 6 0 58,98 6 0.98 36 5.90 6 0.02 37 8 1 18,64 8 1.31 38 6.23 8 0.02 38 9 1 28,47 9 1.47 39 6.39 9 0.03 39 10 1 38,30 10 1.64 40 6.55 10 0.03 40 11 1 48,12 11 1.80 41 6.85 12 0.03 42 13 2 7.78 13 2.13 43 7.04 13 0.04 43 14 2 17.61 14 2.29 44 7.21 14 0.04 44 15 2 27.78 13 2.13 43 7.04 13 0.04 44 15 2 27.44 15 2.46 45 7.37 15 <	0.09
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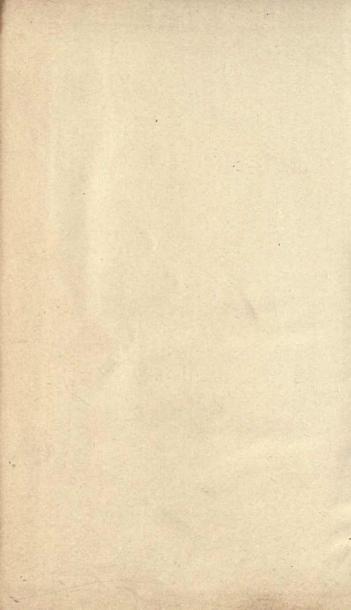


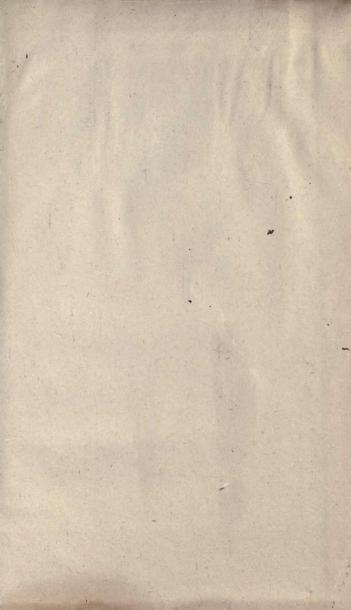
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